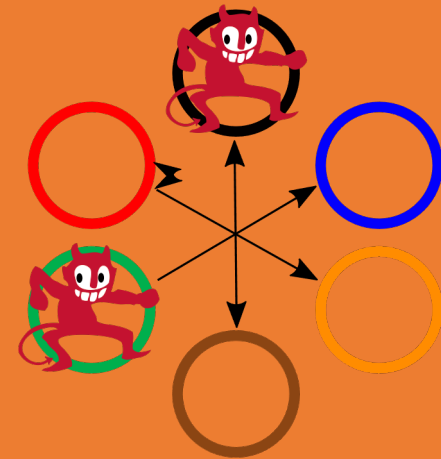


# Overview of NIST PQC Standardization (additional call for signatures)

NIST Workshop on Multi-Party Threshold Schemes  
(MPTS 2023)  
NIST, Gaithersburg, USA



Dr. Maxime Bros  
NIST PQC

# Additional call / Onramp call



 New Standards

# The candidates

- [June 2023] 50 submissions
- [July 2023] 40 accepted

Already 10<sup>+</sup> attacks as of today

Multivariate		MPC in-the-head				Lattice	Code	Symmetric	Isogeny	Other
UOV	Other	MinRank	SD/Rank-SD	PKP	MQ					
Mayo	3wise	Mira	RYDE	Perk	MQOM	EagleSign	Enh. Pqsig-rm	Aimer	SQLsign	Alteq
PROV	DMEsign	MiRith	SDith		Biscuit	EHT	Fuleeca	Ascon-sign		eMLE-Sig 2.0
QR-UOV	HPPC					HAETAE	LESS	FAEST		KAZ
SNOVA						Hawk	MEDS	SPHINCS-alpha		Preon
TUOV						HuFu	Wave			Xifrat
UOV						Raccoon	Cross			
Vox						Squirrels				
7	3	2	2	1	2	7	6	4	1	5
10		7								
40										

# The categories

You know it!



Multivariate

MPC-ith

Lattice

Code

Symmetric

Isogeny

# Multivariate based-crypto

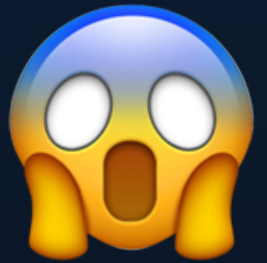
$$\mathbb{F}_q[x_1, x_2, \dots, x_n]$$

$$\begin{cases} x_1 + 2x_3 \\ 2x_1 + 2x_2 \\ x_1 + x_2 \end{cases}$$



$$\begin{cases} f_1(x_1, x_2, \dots, x_n) \\ f_2(x_1, x_2, \dots, x_n) \\ \vdots \\ f_m(x_1, x_2, \dots, x_n) \end{cases}$$

$$\begin{cases} x_1^2 + x_2^2 + x_2x_3 + 2x_3^2 \\ x_1x_2 + x_2^2 + x_2x_3 + x_3^2 \\ x_1^2 + x_1x_2 + x_1x_3 + x_2x_3 \end{cases}$$



Multivariate Quadratic (MQ)

# The categories

System of Quadratic Multivariate Equations

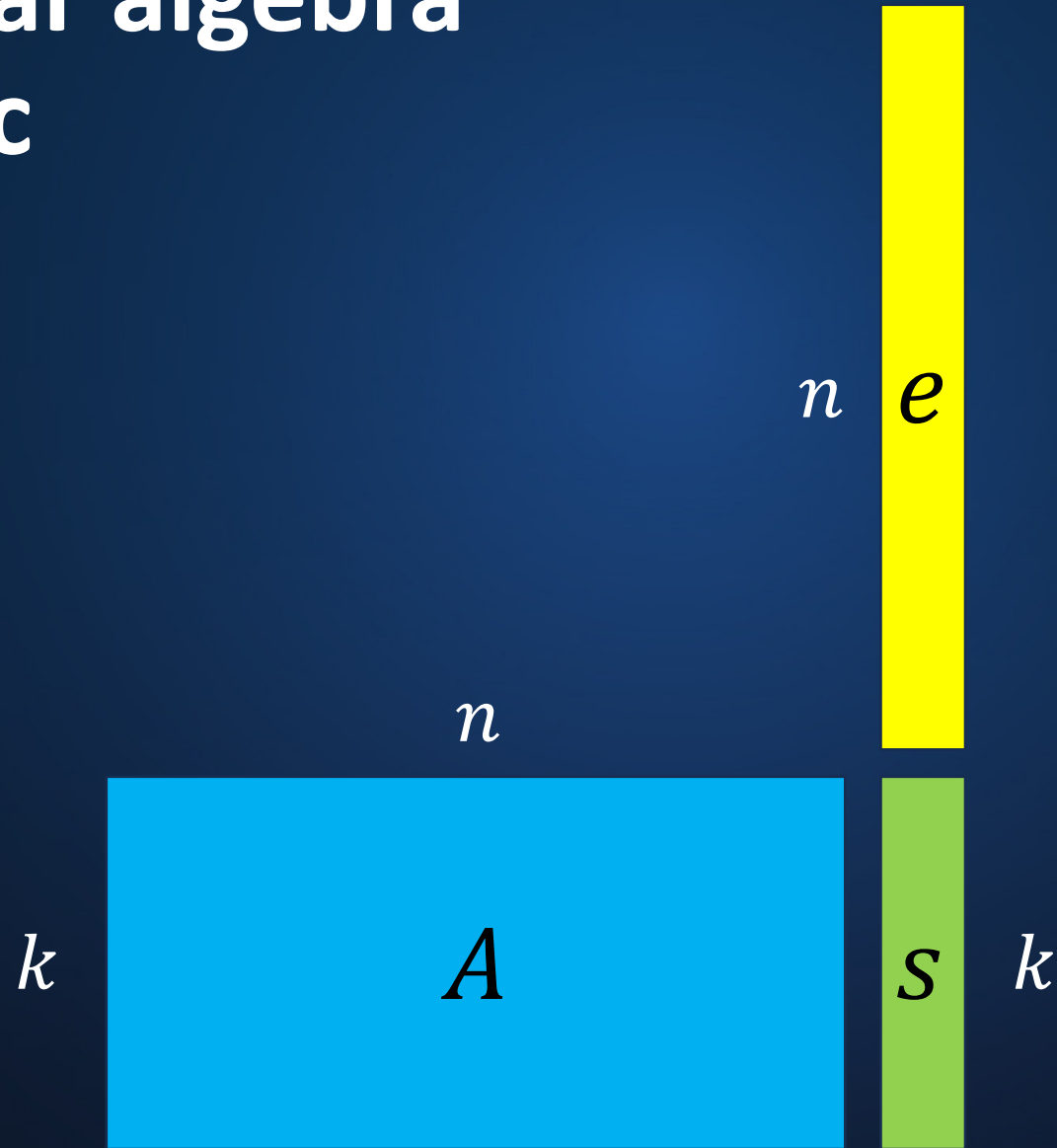


You know it!



# Linear algebra

## Basic



$$Ae^T = s^T$$

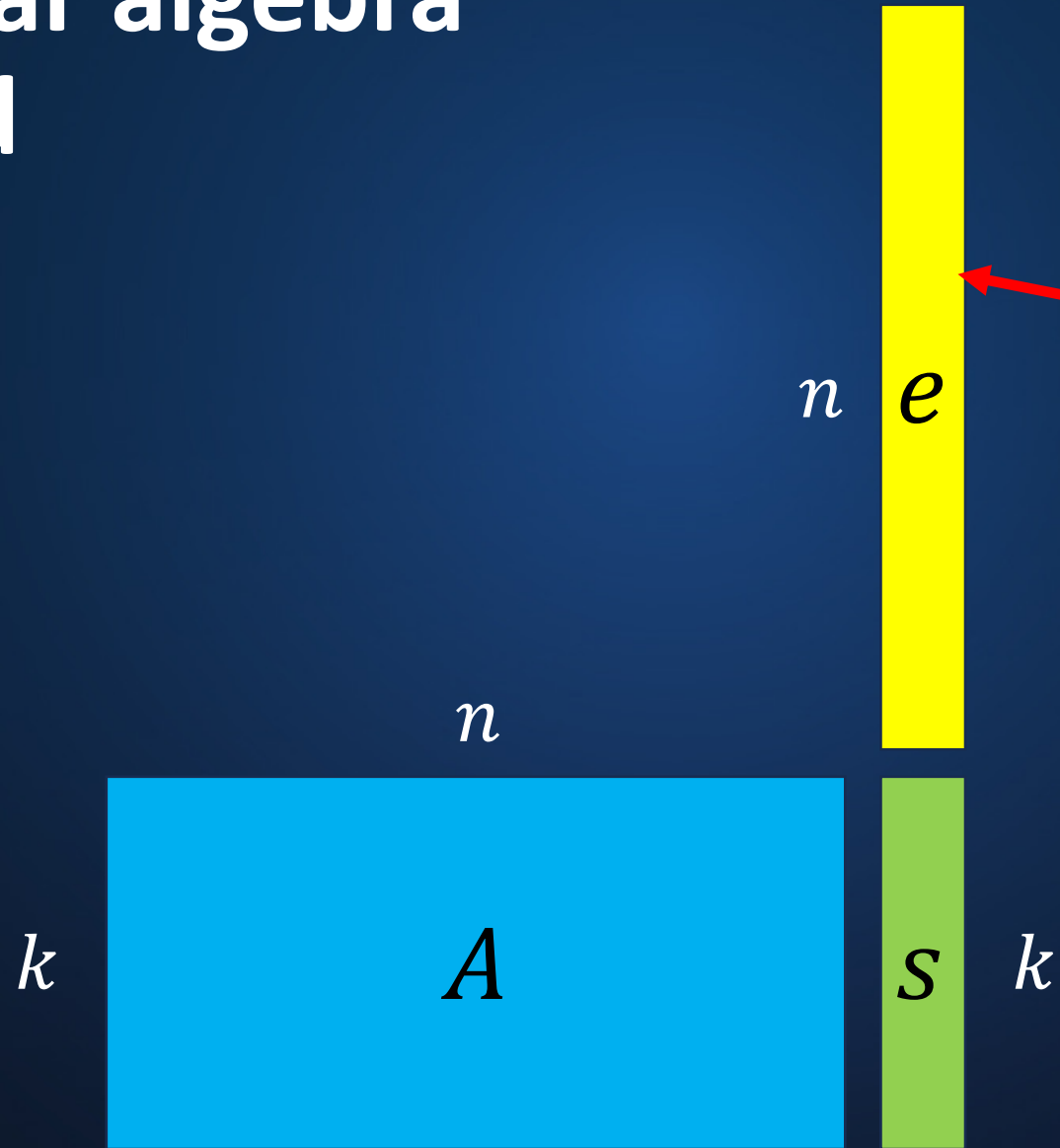
All entries in  $\mathbb{F}_q$

Given  $(A, s) \rightarrow$  Find  $e$

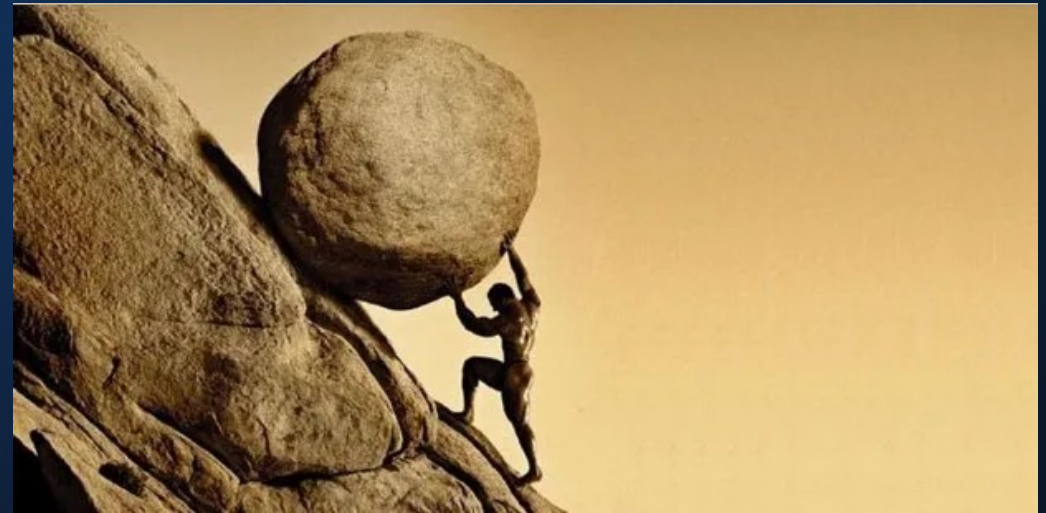


# Linear algebra

## Hard

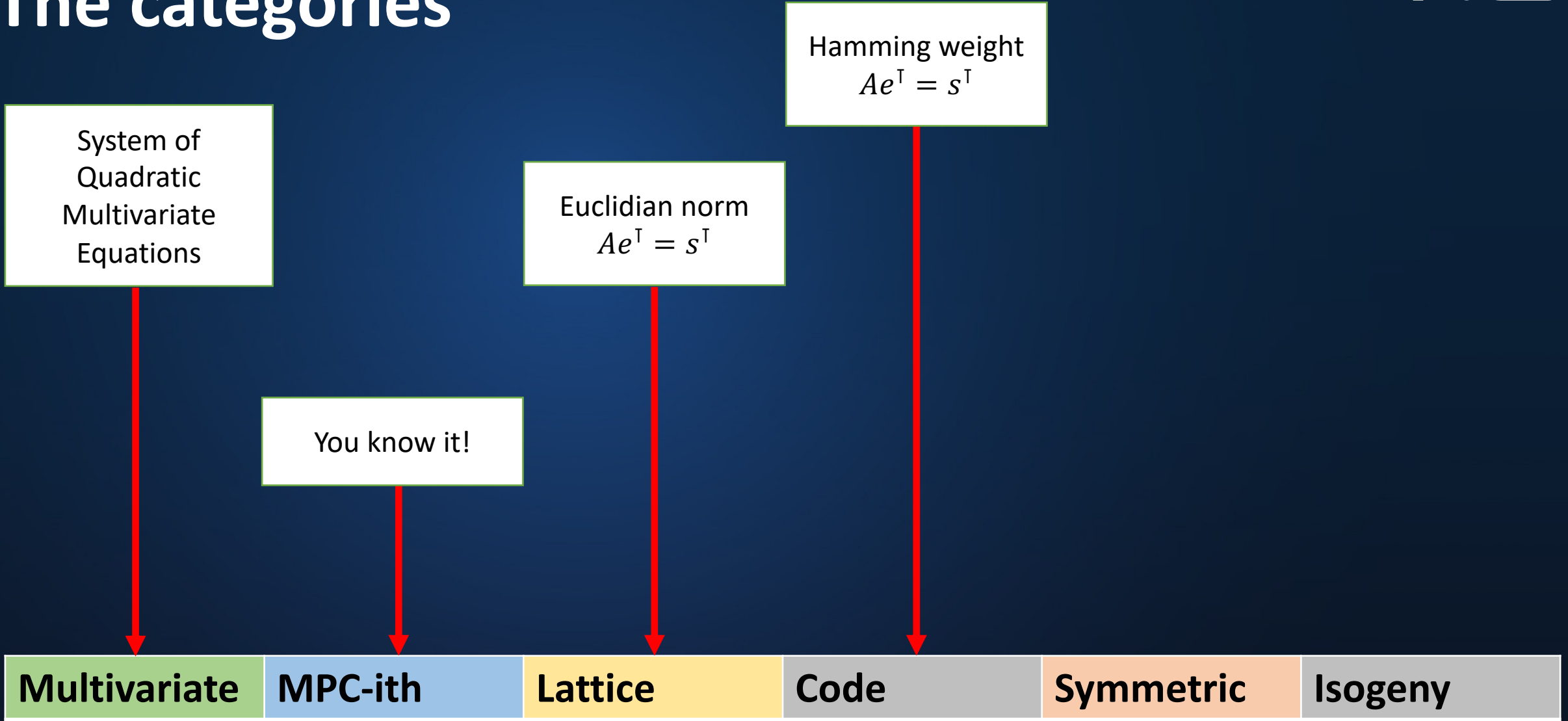


Add a constraint on the ``weight``





# The categories



System of  
Quadratic  
Multivariate  
Equations

You know it!

Euclidian norm  
 $Ae^T = s^T$

Hamming weight  
 $Ae^T = s^T$

**Multivariate**

**MPC-ith**

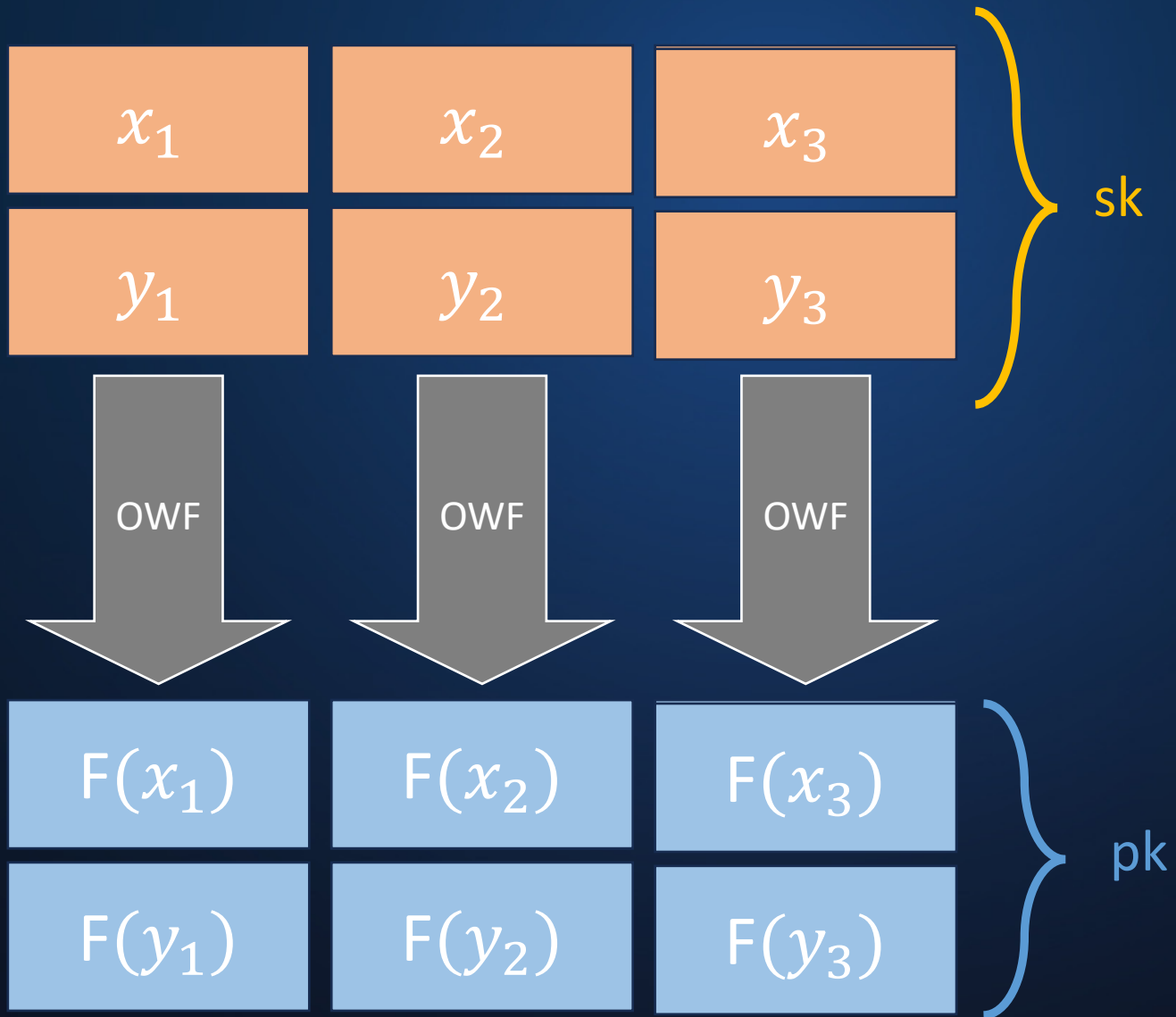
**Lattice**

**Code**

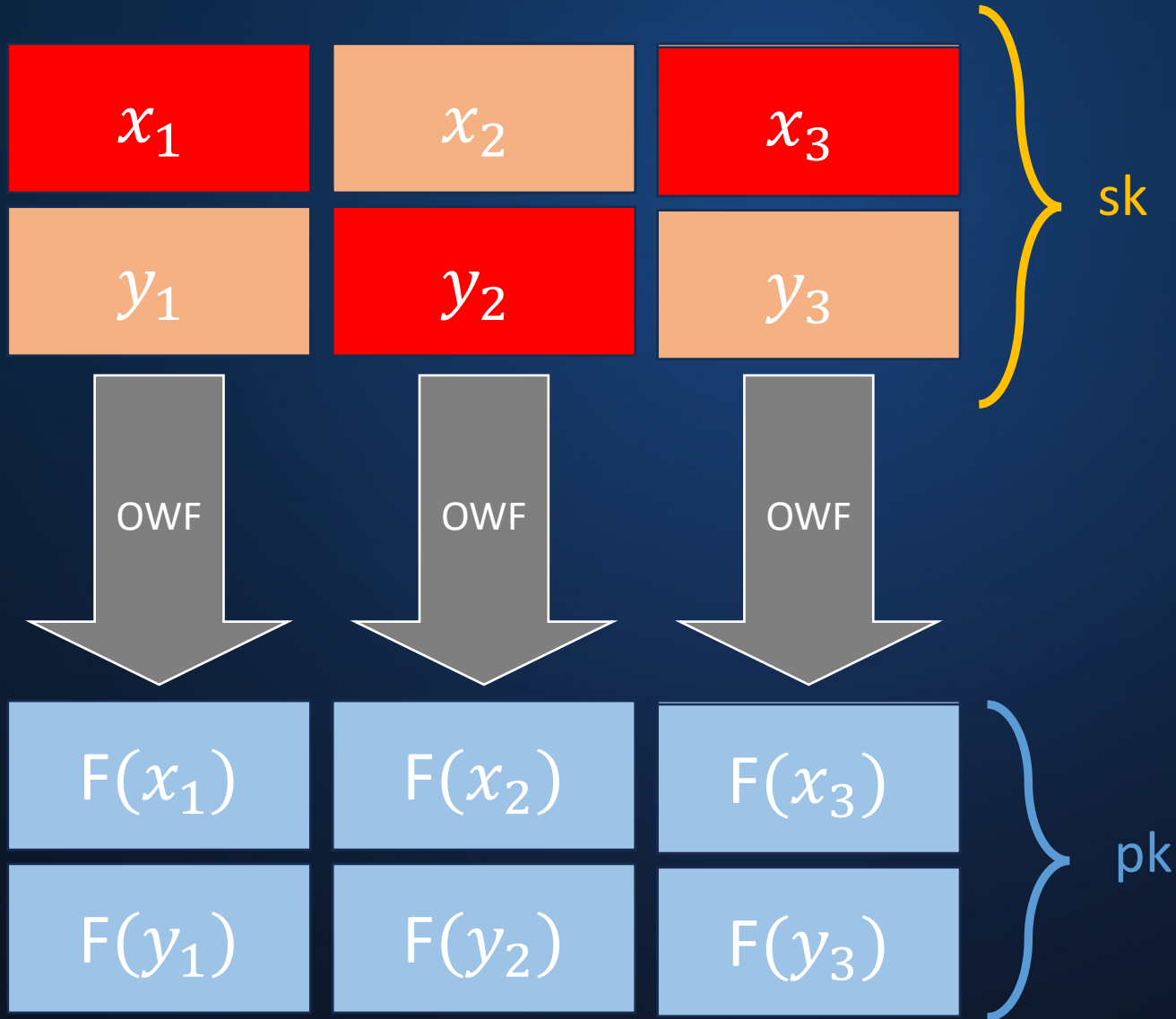
**Symmetric**

**Isogeny**

# Symmetric



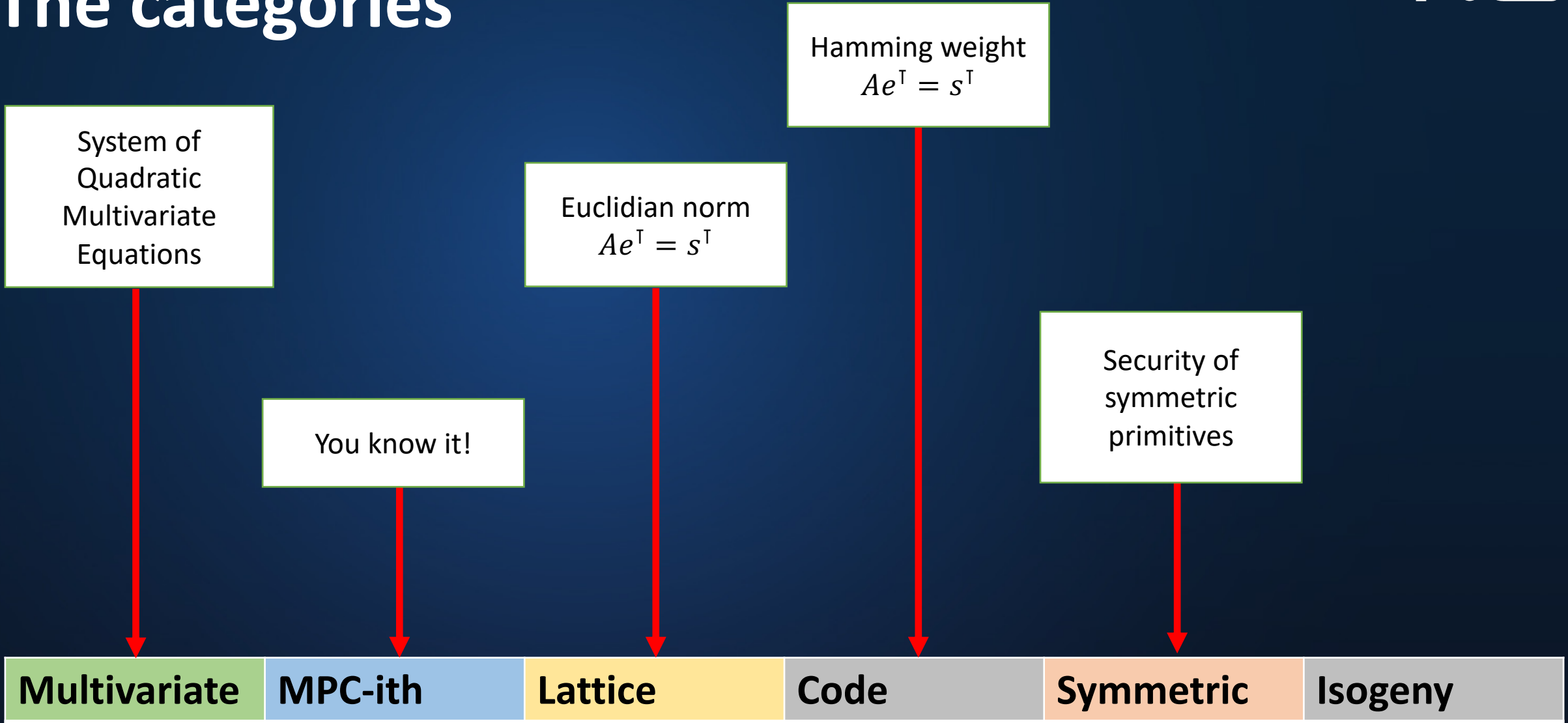
# Symmetric



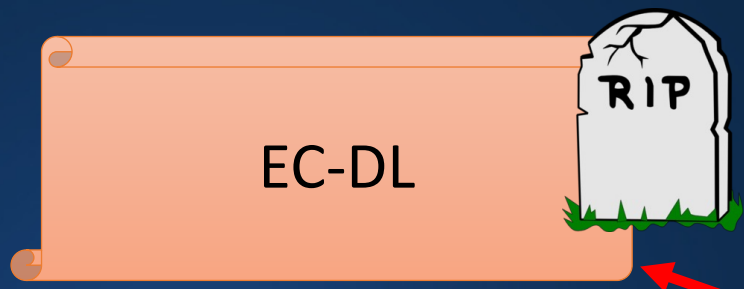
$$\text{Sign}(010) = F(x_1) \mid F(y_2) \mid F(x_3)$$

- A LOT of improvements:
- Merkle trees (FTS)
  - Winternitz (OTS)
  - etc.
  - SPHINCS+

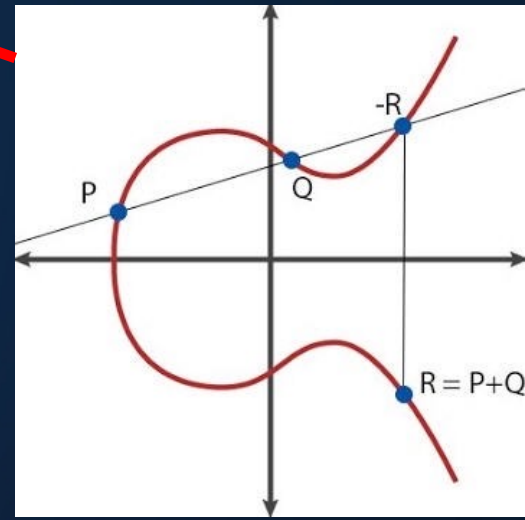
# The categories



# Isogeny

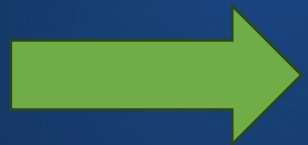


Abelian group

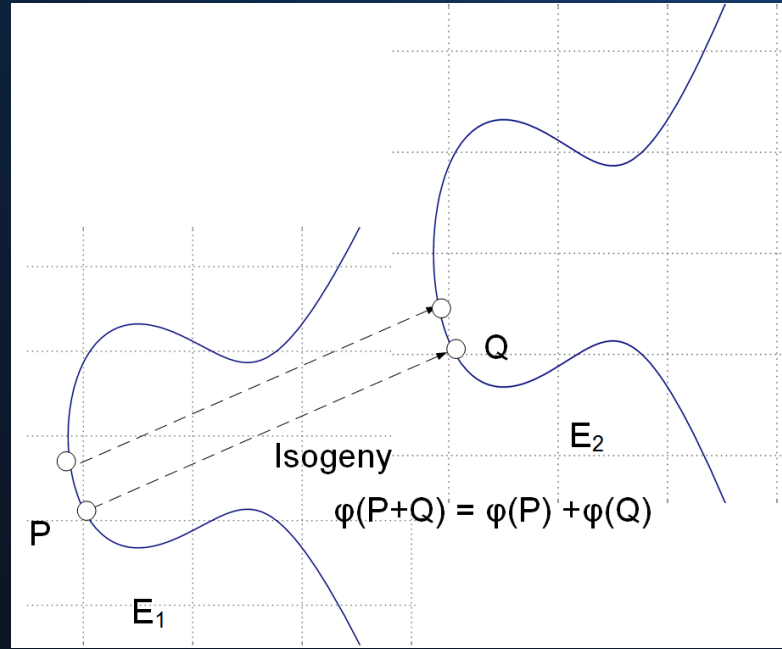
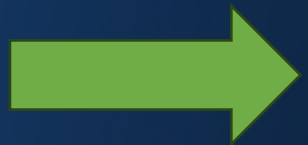


Elliptic curve

$$y = x^3 + ax + b$$

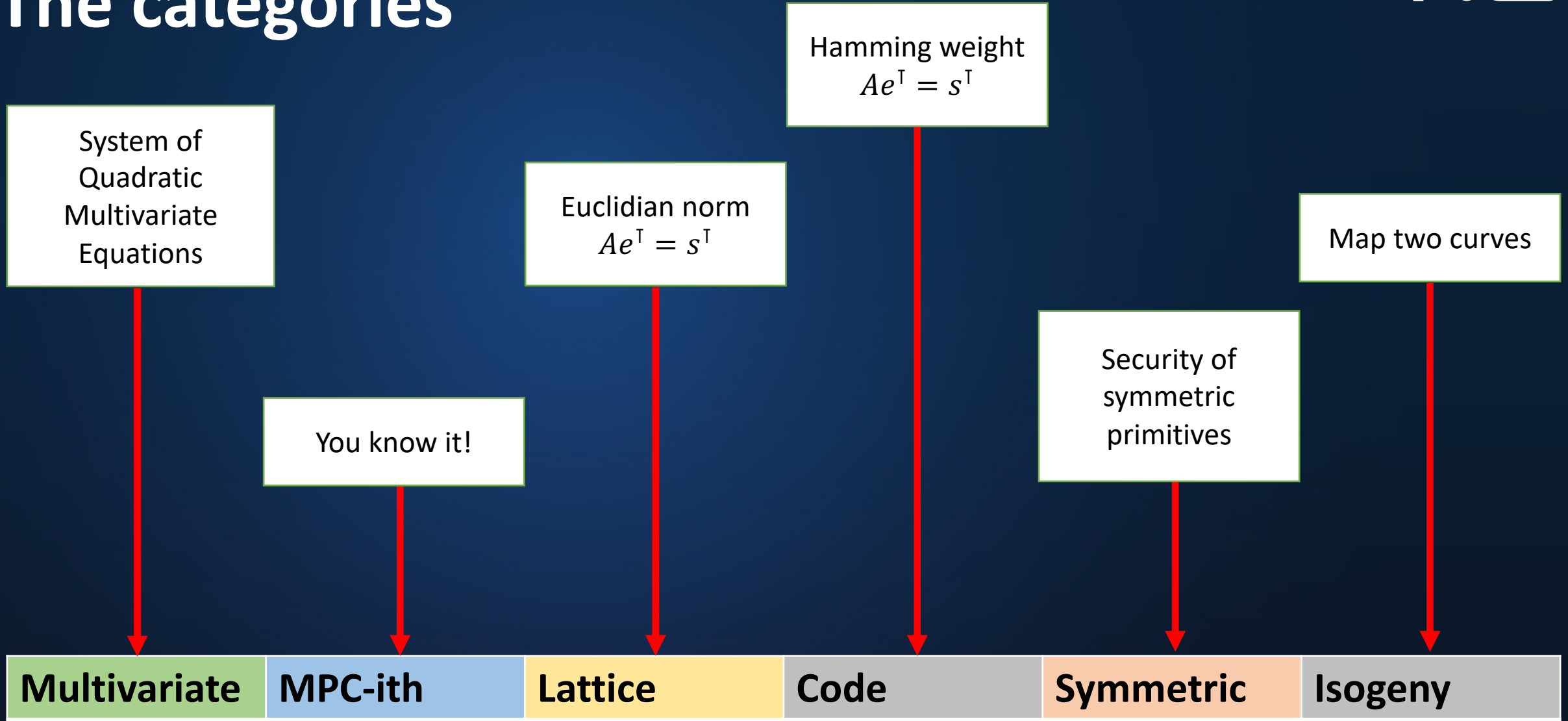


Points in  $\mathbb{F}_q$



An isogeny  $\phi$  between curves  $E_1$  and  $E_2$  is a group homomorphism  $E_1 \rightarrow E_2$ .  
*(usually defined by its kernel)*

# The categories



# Code-based keygens in a few words

McEliece

“Aleknovich – Kyber – HQC”

Classic McEliece  
(Binary Goppa codes)

BIKE  
(MDPC codes)

HQC

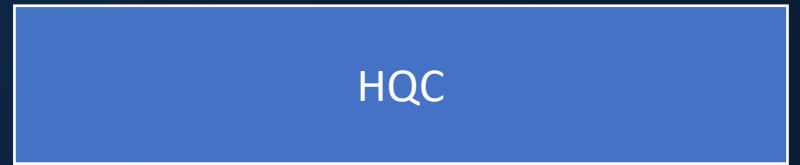
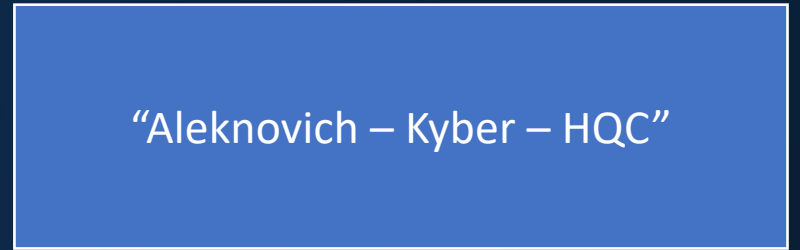
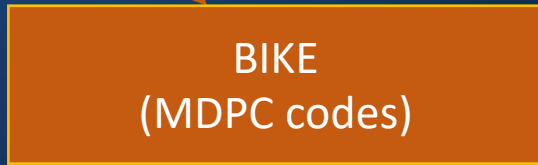
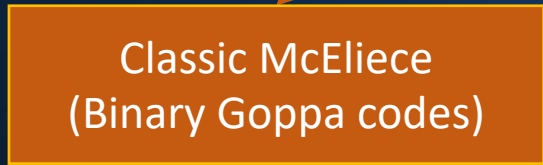
... and many variants!  
(RS, GRS, etc...)



NIST 4<sup>th</sup> Round



# Keygens in a few words



« Hide the structure of a structured code »

Binary Goppa code

Q-Cyclic - Sparse

Q-Cyclic instance of  $Ae^T = s^T$

Row echelon form / Gaussian elimination

Matrix-vector product

Row echelon form / Gaussian elimination

$$sk := \left[ \begin{array}{ccccc|ccccc} 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 1 & 0 \end{array} \right]$$

$$pk := \left[ \begin{array}{ccccc|ccccc} 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 \end{array} \right]$$

Polynomials modulo  $(X^n - 1)$

$$R := \frac{\mathbb{F}_2[X]}{(X^n - 1)} \cong \mathcal{C} \subset \mathbb{F}_2^{n \times n}$$

$$sk := (A, B) = (X^4 + X + 1, X^3 + X + 1) \in R^2$$

$$pk := (1, A^{-1}B) = (1, X^4 + X^3 + X^2) \in R^2$$

Feel free to contact me for more info on:

- multivariate-based cryptography 
- code-based cryptography 

**`maxime.bros@nist.gov`**