



On the Side-Channel Resistance of UOV

Survey of Physical Attacks and Recent Developments

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Outline

1. UOV from Two Perspectives

2. Fault Attacks

Skip Random Sampling of Vinegar Variables [SK20]

Bit-Flip in Central Map [FKN+22]

3. Side Channel Attacks

Horizontal SCA on Linear Transformation [PSK+18]

Template Attack on Evaluation of Vinegar Variables [ACK+23]

4. Takeaways

UOV from Two Perspectives

UOV - a Remarkable Candidate

UOV stands out, since

- it is a comparably old scheme with 25 years of cryptanalysis
- many current (and past) multivariate signature schemes are modifications of it

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- 'e.g., **UOV**' ✓

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Comparison with Dilithium

Oil and Vinegar: Modern Parameters and Implementations²

Key sizes and performance data

Signature Scheme	public key	secret key Bytes	signature	KeyGen	Sign Cycles	Verify
ov-lp	278 432	237 912	128	2 903 434	105 324	90 336
ov-lp-pkc	43 576	237 912	128	2 858 724	105 324	224 006
ov-lp-pkc-sk	43 576	64	128	2 848 774	1 876 442	224 006
Dilithium2	1 312	2 544	2 420	124 031	333 013	118 412

²Beullens, W., Chen, M. S., Hung, S. H., Kannwischer, M. J., Peng, B. Y., Shih, C. J., and Yang, B. Y. (2023). Oil and Vinegar: Modern Parameters and Implementations. IACR TCHES, 321-365.

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 - Include a trapdoor that can only be used with the secret key
- **Verify** if $\mathcal{P}(\mathbf{s}) = \mathbf{t}$ really holds

Two Descriptions of UOV in the Literature (1/2)

UOV with hidden central map \mathcal{F}

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- Fix and insert vinegar variables \tilde{v}_i to get m linear equations in m oil variables

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- T has block matrix structure $T = \begin{pmatrix} I_v & T_1 \\ 0 & I_m \end{pmatrix}$

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- The vector $\mathbf{s} = \mathbf{v} + \mathbf{o}$ forms a valid signature

Fault Attacks

Skip Random Sampling of Vinegar Variables

Main idea

- Skip the random sampling of vinegar values (already discussed in [HTS11]³ and [KL19]⁴)

$$\mathbf{t} \xrightarrow{\mathcal{F}^{-1}} \begin{pmatrix} \mathbf{v} \\ \mathbf{y} \end{pmatrix} \xrightarrow{T^{-1}} \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \begin{pmatrix} \mathbf{v} + T_1 \cdot \mathbf{y} \\ \mathbf{y} \end{pmatrix}$$

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- Solution to \mathcal{F}^{-1} are the randomly generated vinegar values $\mathbf{v} = (v_1, \dots, v_{n-m})^\top$ and the computed oil variables $\mathbf{y} = (y_1, \dots, y_m)^\top$

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- We have $\begin{pmatrix} \mathbf{s}_1^{(i)} \\ \mathbf{s}_2^{(i)} \end{pmatrix} - \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix}$

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- Repeat m times to solve for T_1 (requires m faulted signatures)

Reduce Number of Needed Faulted Signatures

In fact, one can do even better

- The vector $\begin{pmatrix} \mathbf{s}_1^{(i)} \\ \mathbf{s}_2^{(i)} \end{pmatrix} - \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix}$ represents an oil vector, i.e.

$$\mathcal{P} \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathcal{F} \begin{pmatrix} I_v & T_1 \\ 0 & I_m \end{pmatrix} \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathcal{F} \begin{pmatrix} 0 \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathbf{0}$$

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- This is easy to recognize in the oil space description, since

$$\mathbf{s}^{(i)} - \mathbf{s} = (\mathbf{v} + \mathbf{o}^{(i)}) - (\mathbf{v} + \mathbf{o}) = \mathbf{o}^{(i)} - \mathbf{o} \in \mathcal{O}$$

Reduce Number of Needed Faulted Signatures

In fact, one can do even better

- The vector $\begin{pmatrix} \mathbf{s}_1^{(i)} \\ \mathbf{s}_2^{(i)} \end{pmatrix} - \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix}$ represents an oil vector, i.e.

$$\mathcal{P} \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathcal{F} \begin{pmatrix} l_v & T_1 \\ 0 & l_m \end{pmatrix} \begin{pmatrix} T_1 \cdot (\mathbf{y}^{(i)} - \mathbf{y}) \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathcal{F} \begin{pmatrix} 0 \\ (\mathbf{y}^{(i)} - \mathbf{y}) \end{pmatrix} = \mathbf{0}$$

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- One oil vector enables key recovery in polynomial time \rightarrow next slide

Algebraic Attack

Knowledge of an oil vector dramatically simplifies algebraic key recovery attacks

- For two oil vectors $\mathbf{o}_1, \mathbf{o}_2$ it holds

$$\mathcal{P}'(\mathbf{o}_1, \mathbf{o}_2) = \mathcal{P}(\mathbf{o}_1 + \mathbf{o}_2) - \mathcal{P}(\mathbf{o}_1) - \mathcal{P}(\mathbf{o}_2) = \mathbf{0} \in \mathbb{F}_q^m$$

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Details can be found in [ACK+23] ⁶

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⁶Aulbach, T., Campos, F., Krämer, J., Samardjiska, S., and Stöttinger, M.: Separating Oil and Vinegar with a Single Trace: Side-Channel Assisted Kipnis-Shamir Attack on UOV. IACR TCHES 2023

Summary of the Fault Attack [SK20]

Summary

- **Instruction skip** to reuse the vinegar variables
- **Number of needed faulted signatures** is reduced from m to now only **1**
- Distinguish between reuse and zero setting (analyzed in [SK20]⁷ and [KKT22]⁸)

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- Store old vinegar variables and only output signature if there are no large overlaps

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Future work

- Execute instruction skip on a target device
- Apply to various modifications of UOV

Bit-Flip in Central Map

Fault model

- Introduce a fault that changes one coefficient $\alpha'_{i,j}^{(k)}$ in the central map \mathcal{F} (already discussed in [HTS11] and [KL19])
- Faulted coefficient is randomly chosen and attacker does not know its location

$$F^{(k)} = \begin{pmatrix} \alpha_{1,1}^{(k)} & \cdots & \alpha_{1,v}^{(k)} & \alpha_{1,v+1}^{(k)} & \cdots & \alpha_{1,n}^{(k)} \\ 0 & \ddots & \vdots & \vdots & \alpha'_{i,j}^{(k)} & \vdots \\ 0 & 0 & \alpha_{v,v}^{(k)} & \alpha_{v,v+1}^{(k)} & \cdots & \alpha_{v,n}^{(k)} \\ 0 & \cdots & 0 & 0 & \cdots & 0 \\ \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 0 & \cdots & 0 \end{pmatrix}$$

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- One coefficient in the k -th linear equation is altered

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Fault propagation

$$\mathbf{t} \xrightarrow{\mathcal{F}'^{-1}} \begin{pmatrix} \mathbf{v} \\ \mathbf{y} \end{pmatrix} \xrightarrow{T^{-1}} \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \mathbf{s}'$$

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- This yields quadratic equations in the i -th and j -th row of T

Iterate the following steps to achieve key recovery (Details in [FKN+22]¹⁰)

1. Employ signing oracle to get $N = n(n + 1)/2$ message and faulted signature pairs
2. Obtain rows of the secret transformation T
3. Transform \mathcal{P} to a smaller system by reducing the number of variables

¹⁰Furue, H., Kiyomura, Y., Nagasawa, T., and Takagi, T.: A New Fault Attack on UOV Multivariate Signature Scheme. PQCrypto 2022

Summary of the Fault Attack [FKN+22]

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- Randomization fault
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Future work

- Find a way to physically cause the randomization in exactly one entry
- Transfer the attack to implementation with compressed keys, where the central map is not stored

QuantumHammer: A Practical Hybrid Attack on the LUOV Signature Scheme¹¹

¹¹Mus, K., Islam, S., and Sunar, B. QuantumHammer: A Practical Hybrid Attack on the LUOV Signature Scheme. ACM SIGSAC Conference on Computer and Communications Security 2020

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- Uses Rowhammer attack to introduce faults to the linear transformation T
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Side Channel Attacks

Horizontal SCA on Linear Transformation T

Main idea¹²

$$\mathbf{t} \xrightarrow{\mathcal{F}^{-1}} \begin{pmatrix} \mathbf{v} \\ \mathbf{y} \end{pmatrix} \xrightarrow{T^{-1}} \begin{pmatrix} \mathbf{s}_1 \\ \mathbf{s}_2 \end{pmatrix} = \begin{pmatrix} \mathbf{v} + T_1 \cdot \mathbf{y} \\ \mathbf{y} \end{pmatrix}$$

- Perform power analysis of matrix-vector multiplication

$$\begin{pmatrix} I_v & T_1 \\ 0 & I_m \end{pmatrix} \cdot \begin{pmatrix} \mathbf{v} \\ \mathbf{y} \end{pmatrix} = \begin{pmatrix} \mathbf{v} + T_1 \cdot \mathbf{y} \\ \mathbf{y} \end{pmatrix}$$

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- Here, the vector \mathbf{y} is known, and the matrix T_1 is the secret we want to obtain

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- Either obtain all entries of T by SCA or identify certain rows and reduce the system \mathcal{P} as shown in previous fault attack

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Matrix-Vector Multiplication

The vulnerable function in more detail

$$\begin{pmatrix} I & T_1 \\ 0 & I \end{pmatrix} \cdot \begin{pmatrix} \mathbf{v} \\ \mathbf{y} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & t_{1,4} & t_{1,5} \\ 0 & 1 & 0 & t_{2,4} & t_{2,5} \\ 0 & 0 & 1 & t_{3,4} & t_{3,5} \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ v_3 \\ y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \\ y_1 \\ y_2 \end{pmatrix} + \begin{pmatrix} t_{1,4} \cdot y_1 + t_{1,5} \cdot y_2 \\ t_{2,4} \cdot y_1 + t_{2,5} \cdot y_2 \\ t_{3,4} \cdot y_1 + t_{3,5} \cdot y_2 \\ 0 \\ 0 \end{pmatrix}$$

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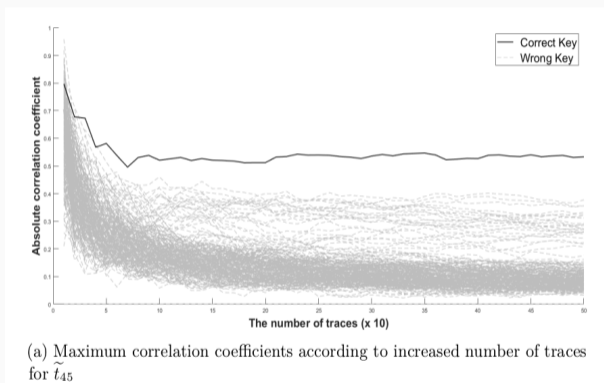
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Compute Correlation with Hypothetical Values

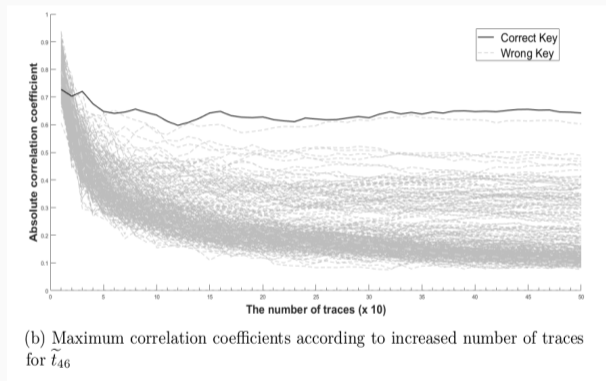
Example with clear separation between correct key elements and wrong key element



Correlation coefficients for all possible field elements and the entry t_{45} [PSK+18]

Compute Correlation with Hypothetical Values

Example with two possible candidate for the correct key element



Correlation coefficients for all possible field elements and the entry t_{46} [PSK+18]

Summary of the Horizontal SCA

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- Attack the matrix-vector product code on the ChipWhisperer-Lite evaluation platform
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Countermeasures

- Masking or shuffling are classical countermeasures for this
- Randomization of the input value (since T is linear)

Summary of the Horizontal SCA

Summary

- Correlation power analysis on field multiplication
- Around 30 – 100 power traces are needed to recover field elements

Practicality

- Attack the matrix-vector product code on the ChipWhisperer-Lite evaluation platform
- Target board is an 8-bit Atmel XMEGA128 (might be more difficult on 32-bit devices)
- Parameters were strongly reduced ($n = 8$ and $m = 6$)

Countermeasures

- Masking or shuffling are classical countermeasures for this
- Randomization of the input value (since T is linear)

Future work

- Analyze efficiency impact of countermeasures
- Transfer the attack to modern and optimized implementations

Attack Insertion of Vinegar Values in Public Key Map

Main idea¹³

- Measure power consumption of $\mathcal{P}(\mathbf{v})$

¹³Aulbach, T., Campos, F., Krämer, J., Samardjiska, S., and Stöttinger, M.: Separating Oil and Vinegar with a Single Trace: Side-Channel Assisted Kipnis-Shamir Attack on UOV. IACR TCHES 2023

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- Consider the matrix-vector multiplication

$$P^{(k)} \cdot \mathbf{v} = \begin{pmatrix} p_{1,1}^{(k)} & p_{1,2}^{(k)} & \cdots & p_{1,n}^{(k)} \\ & p_{2,2}^{(k)} & \cdots & p_{2,n}^{(k)} \\ & & \ddots & \vdots \\ & & & p_{n,n}^{(k)} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{pmatrix} \text{ for } k \in \{1, \dots, m\}$$

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- Secret \mathbf{v} is multiplied with a considerable amount of known values

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Template Attack

- Create a template by tracing the power consumption of

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for $\mathbf{v} = 0, 1, 2, \dots, q - 1 \in \mathbb{F}_q^m$

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- For each field element, we need to run and trace the matrix-vector multiplication only once \rightarrow in total $q = 256$ profiling traces
- Can be collected on another device (subtract some mean to erase the 'footprint' of the device)

Record Power Traces

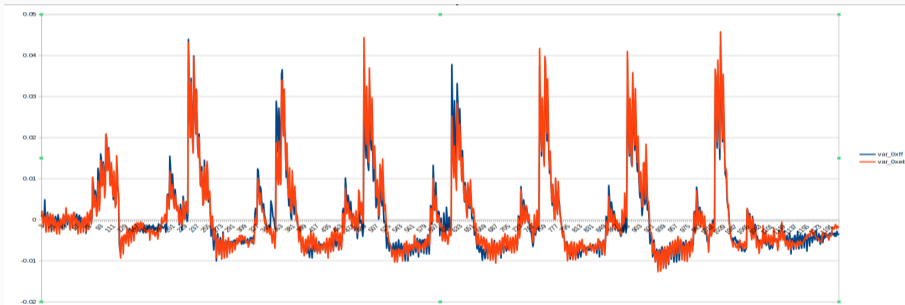
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- The vinegar variables are processed bitwise from LSB to MSB
- Consider the following example



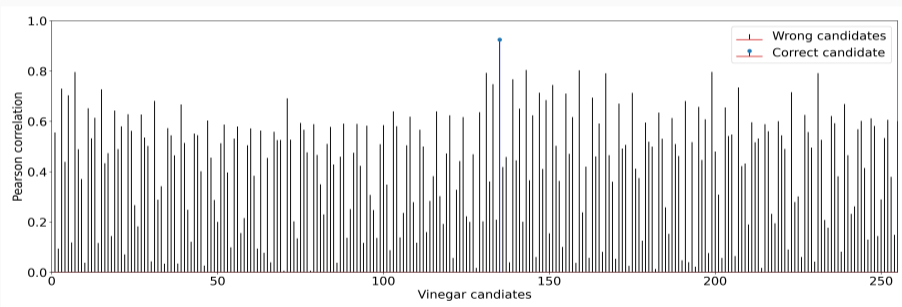
Compare power traces with $v_i = 0xFF$ vs $v_i = 0xEB$

Compute Correlation

- Trace the matrix-vector multiplications with secret vinegar variables on the target device

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- Trace the matrix-vector multiplications with secret vinegar variables on the target device
- Compute correlation to templates for each entry of \mathbf{v}



Correlation of the target trace with each of the 256 reference traces

Summary of the Template Attack

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- Very high success probability ($\approx 97\%$) for all vinegar variables
- Template attack with small number of profiling traces
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Future work

- Analyze efficiency impact of countermeasures
- Apply the attack to M4 implementations or using a different setup

Takeaways

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- Vinegar vectors and oil vectors should be equally secured
- With one of those, the secret key can be recovered in polynomial time
- Some physical attacks are still in a theoretical or simulated state
- Efficiency impact of countermeasures should be analyzed

Questions?

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Aulbach, Campos, Krämer, Samardjiska, Stöttinger:
Separating Oil and Vinegar with a Single Trace
<https://ia.cr/2023/335>



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