



CISPA

HELMHOLTZ CENTER FOR
INFORMATION SECURITY



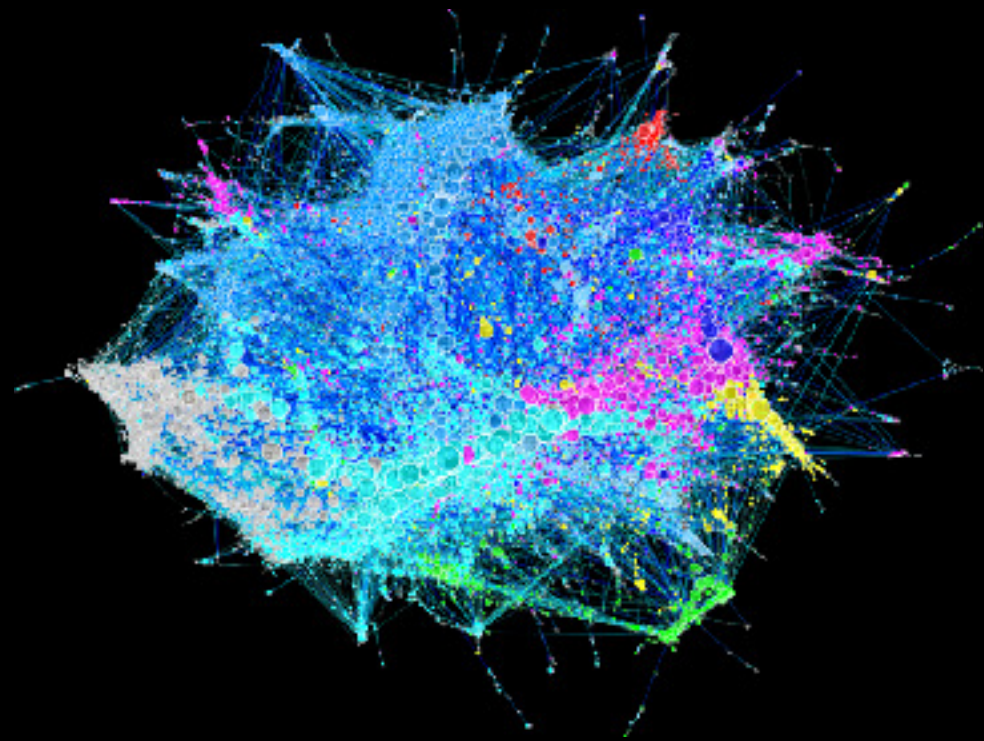
European Research Council
Established by the European Commission

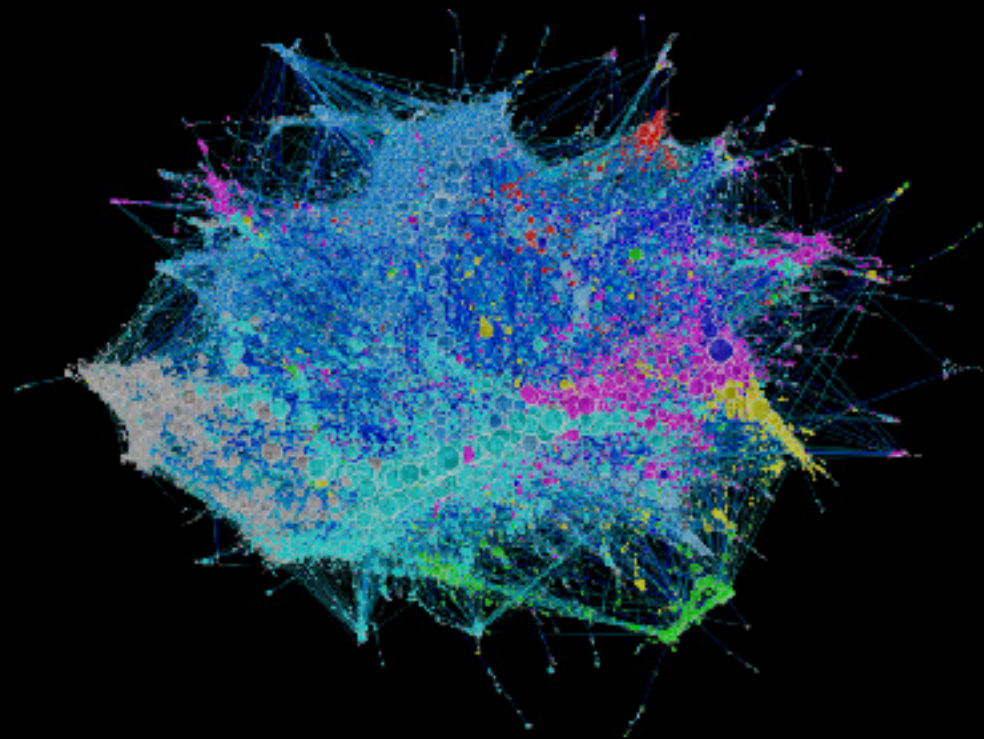
Laconic Cryptography: New Paradigms, Constructions and Directions

Nico Döttling | 06.03.2024

la·con·ic: using or involving the use of a minimum of words [Merriam Webster]



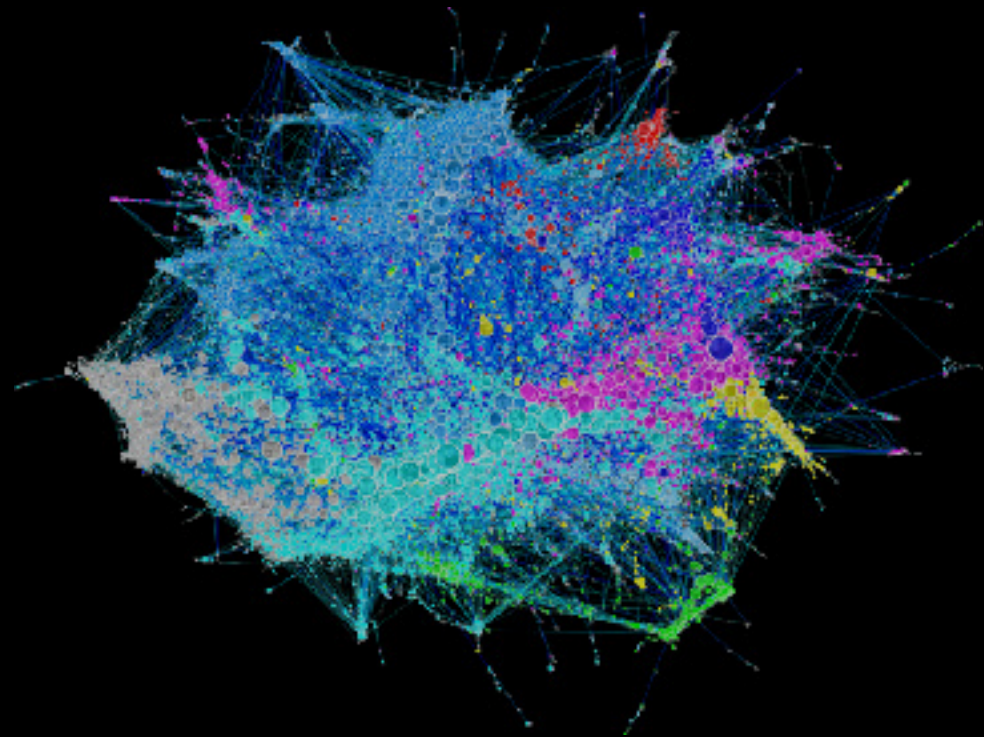




Data-Driven Methods



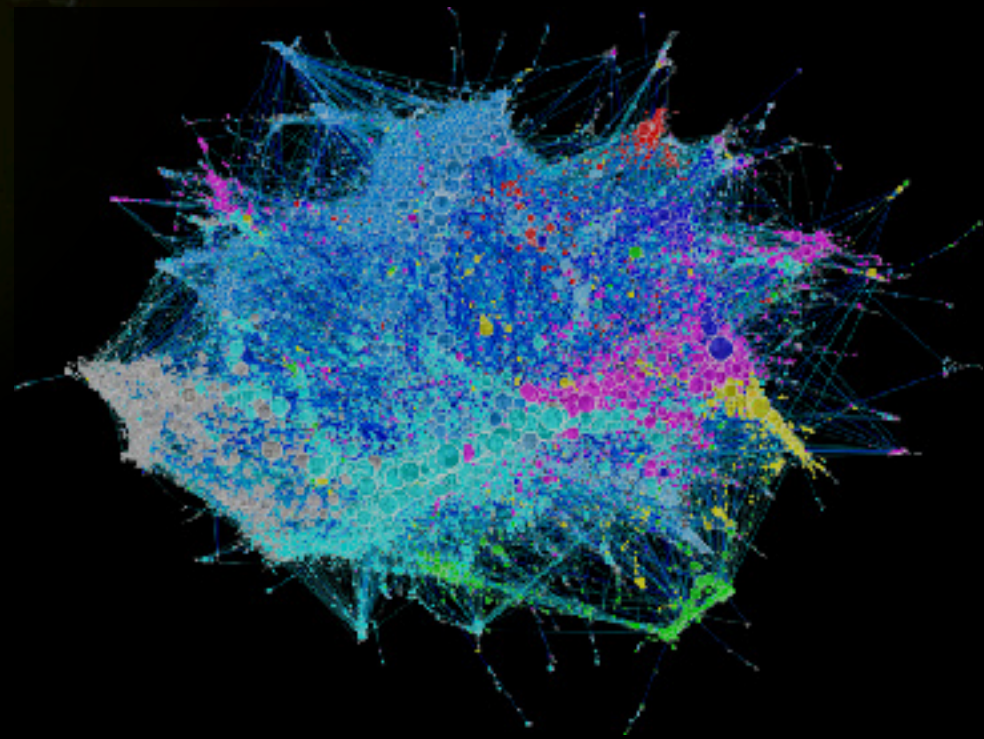
Advanced
Cryptography



Data-Driven
Methods



Advanced
Cryptography

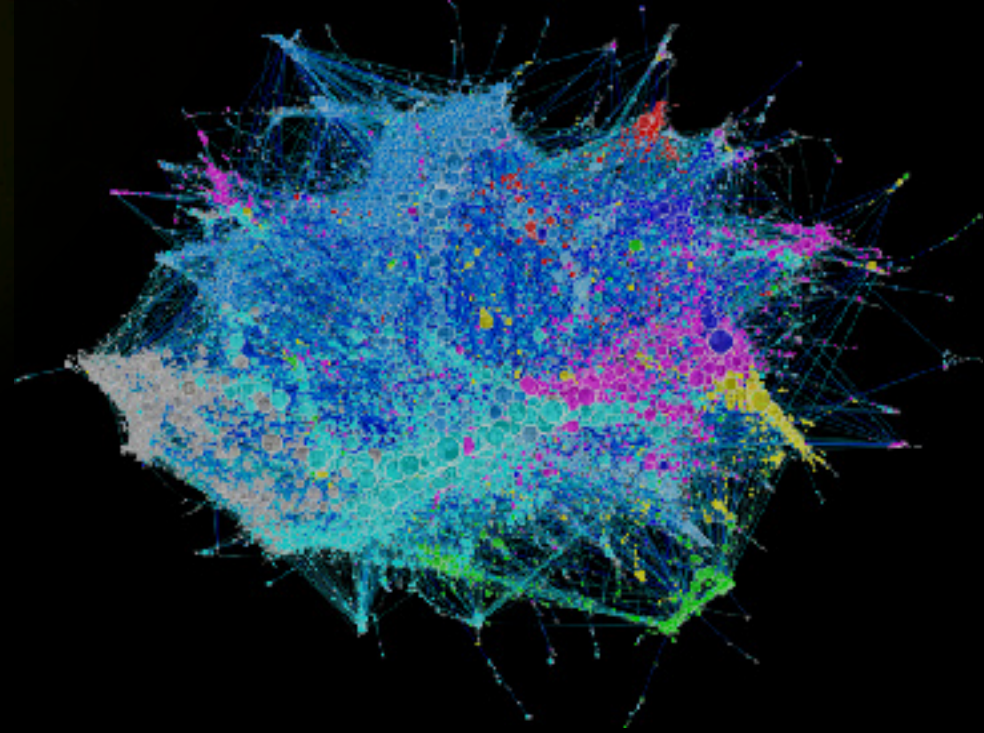


Data-Driven
Methods



Advanced
Cryptography

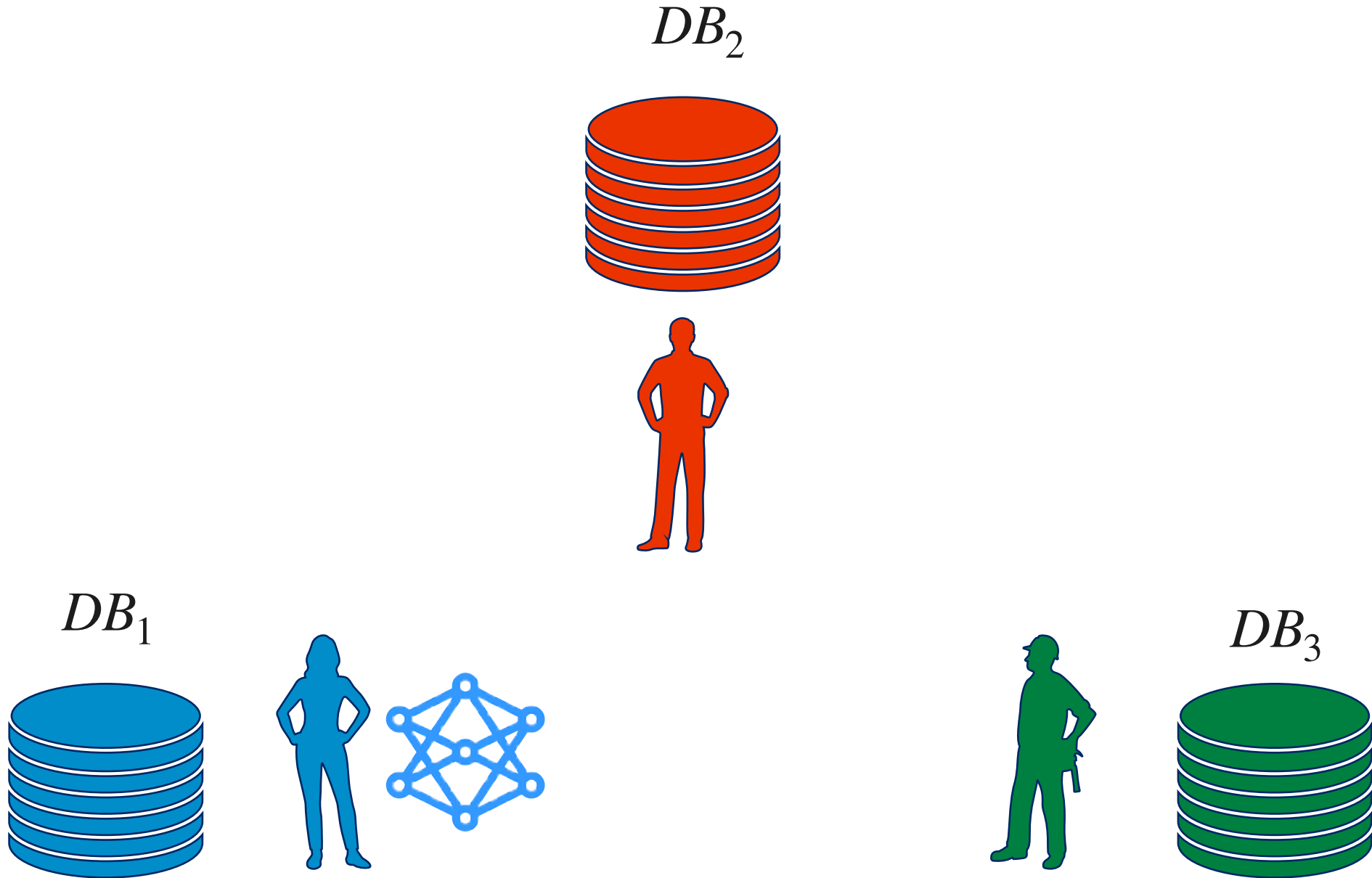
Communication &
Computational Overhead



Data-Driven
Methods



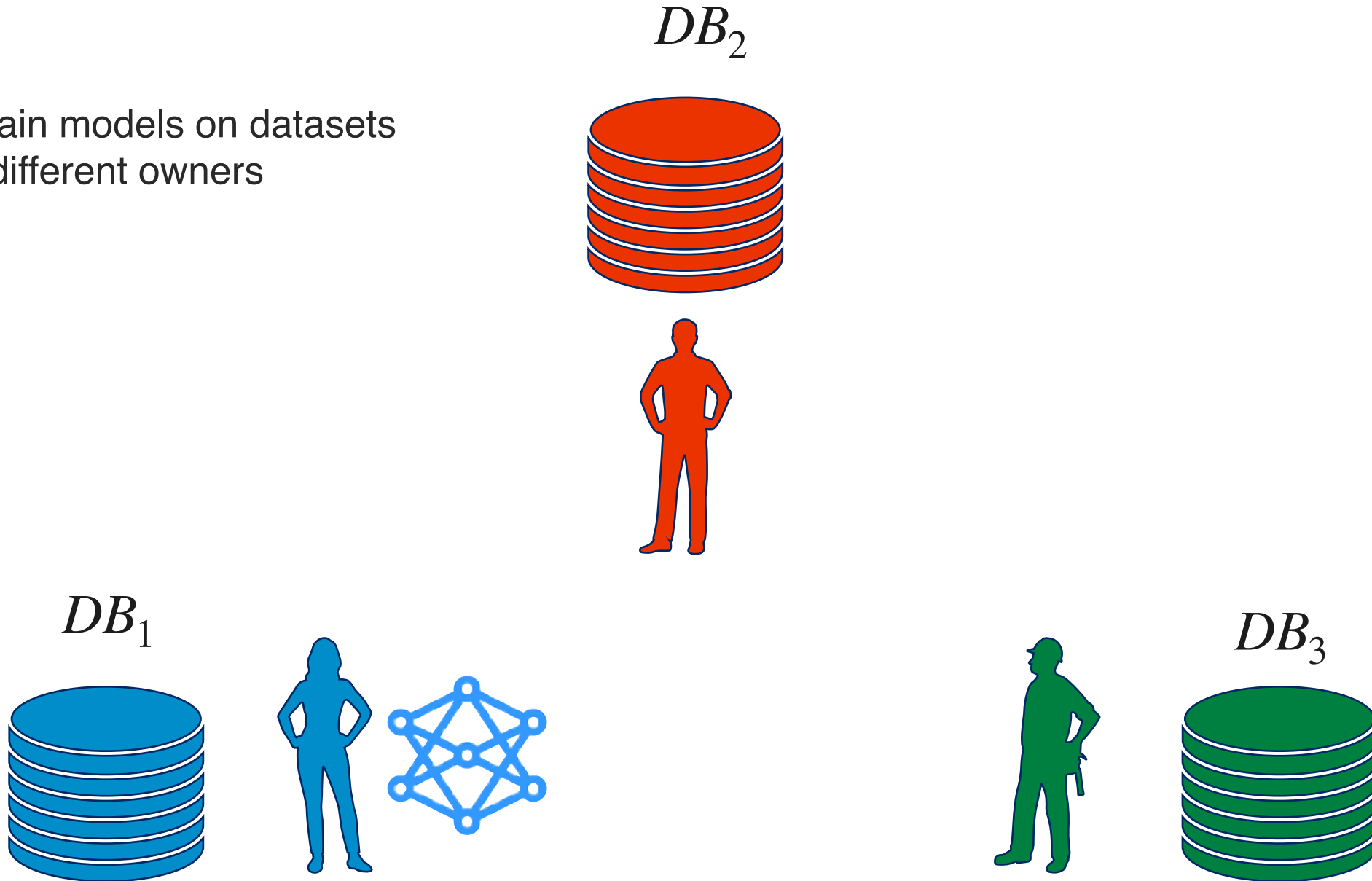
Motivation: Federated Learning





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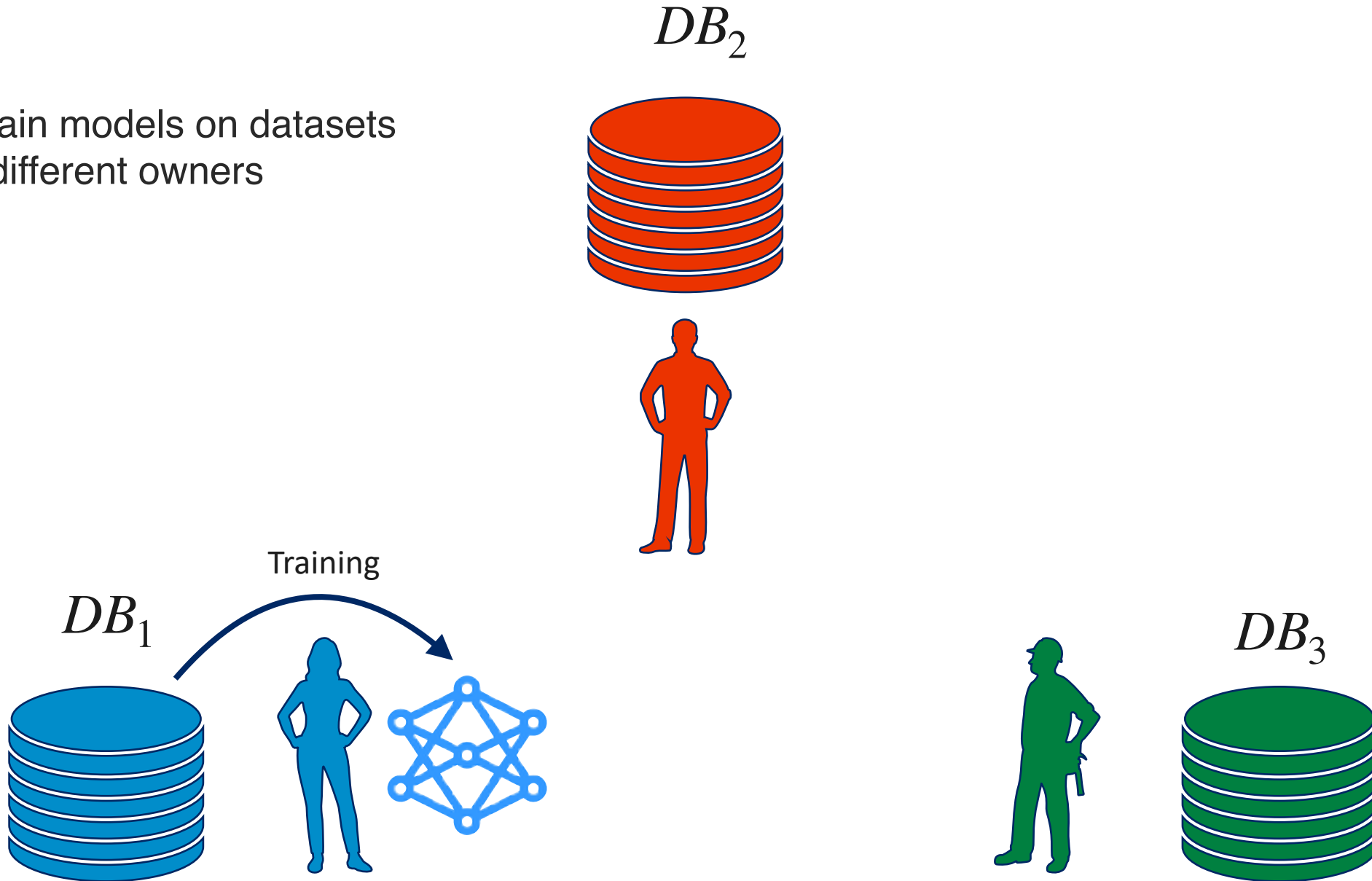
- Jointly train models on datasets held by different owners





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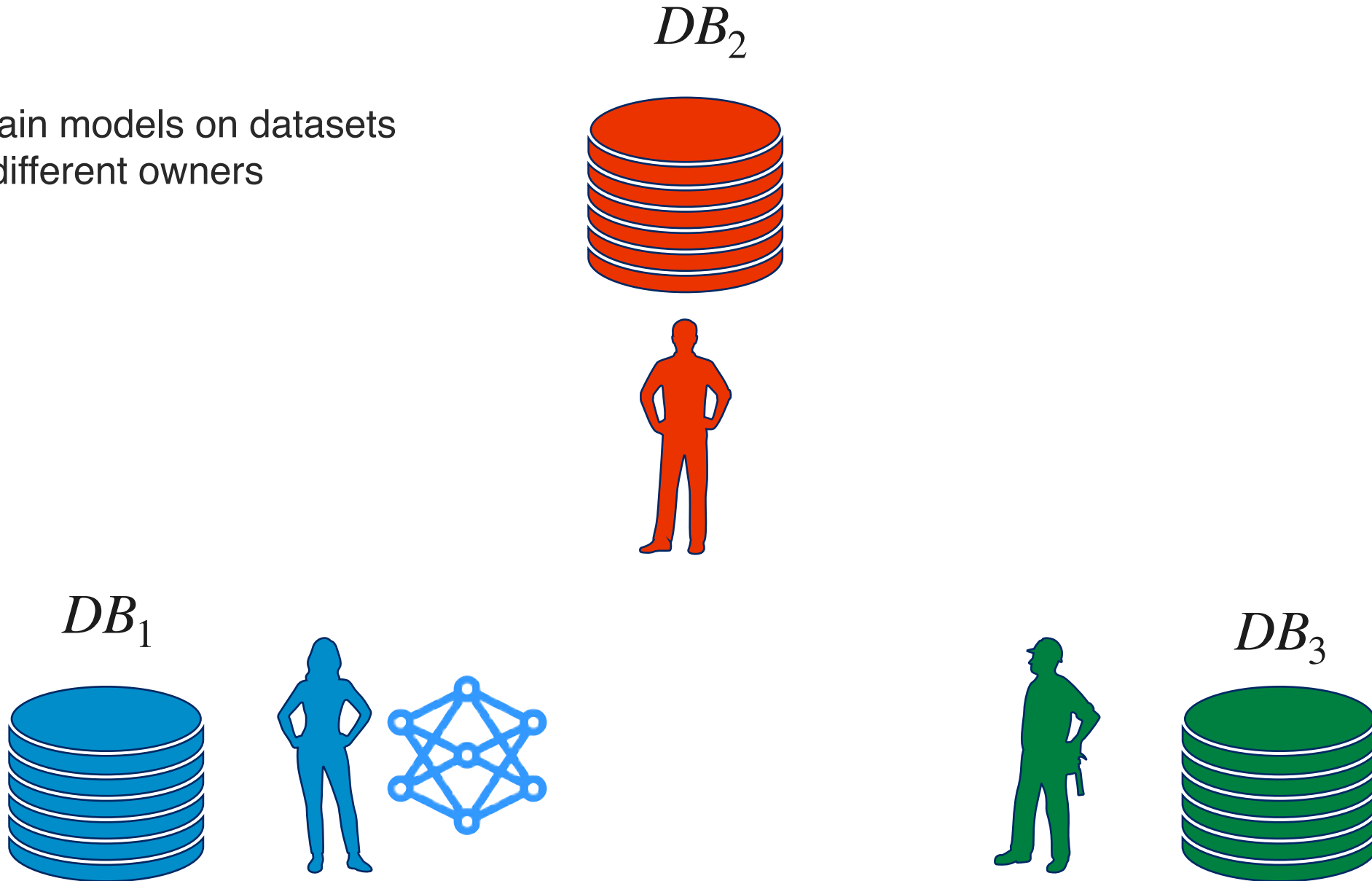
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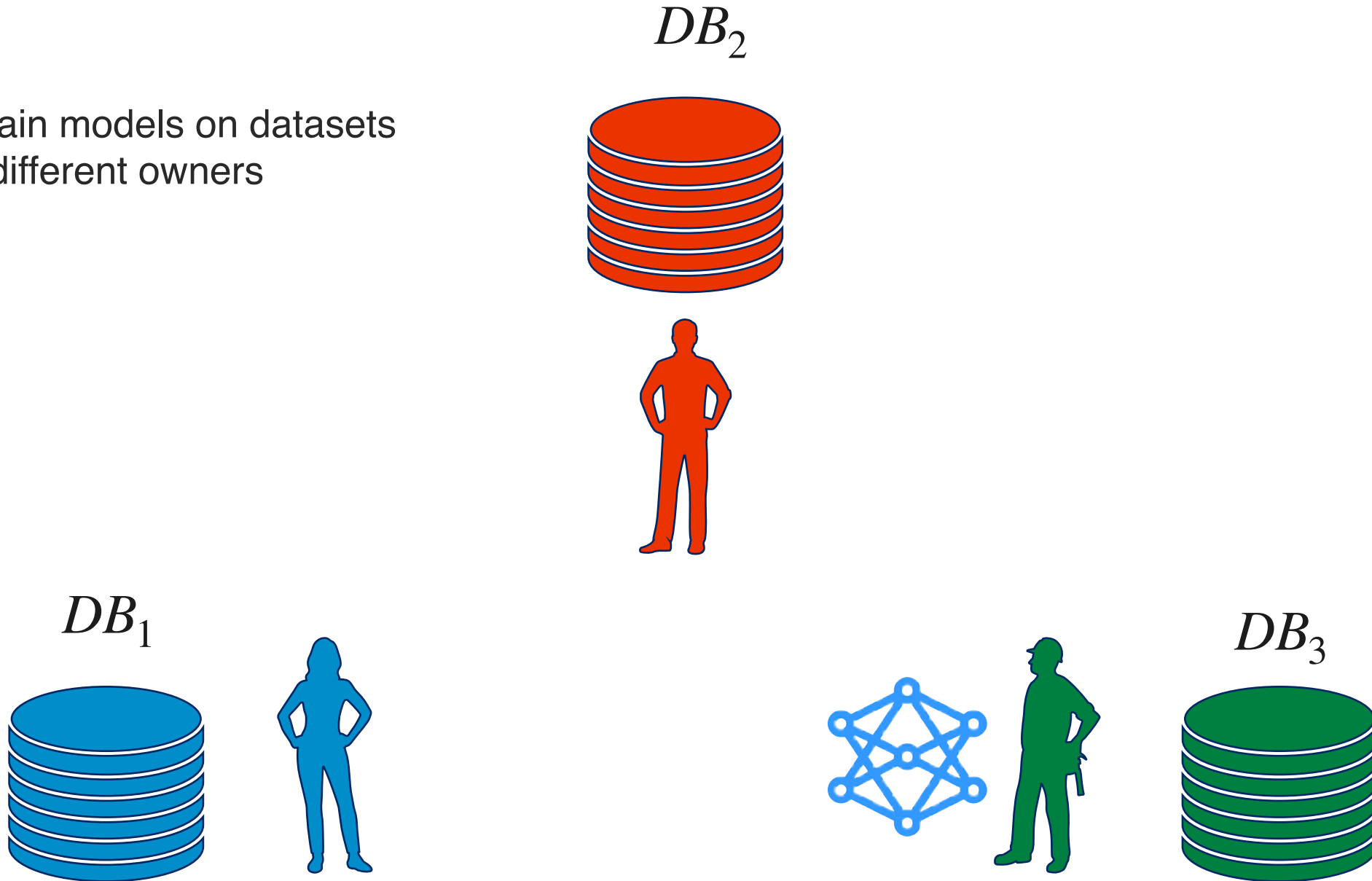
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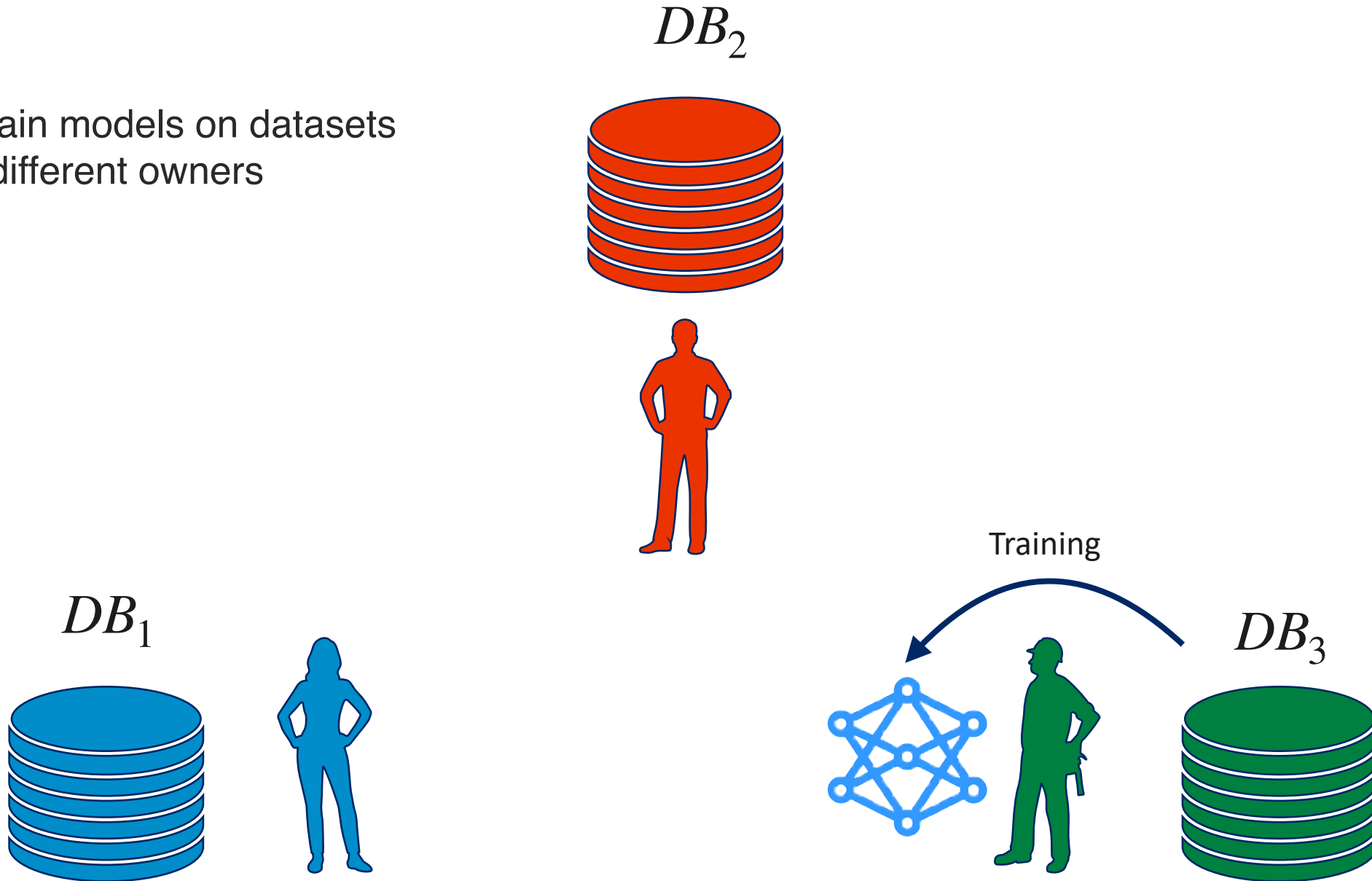
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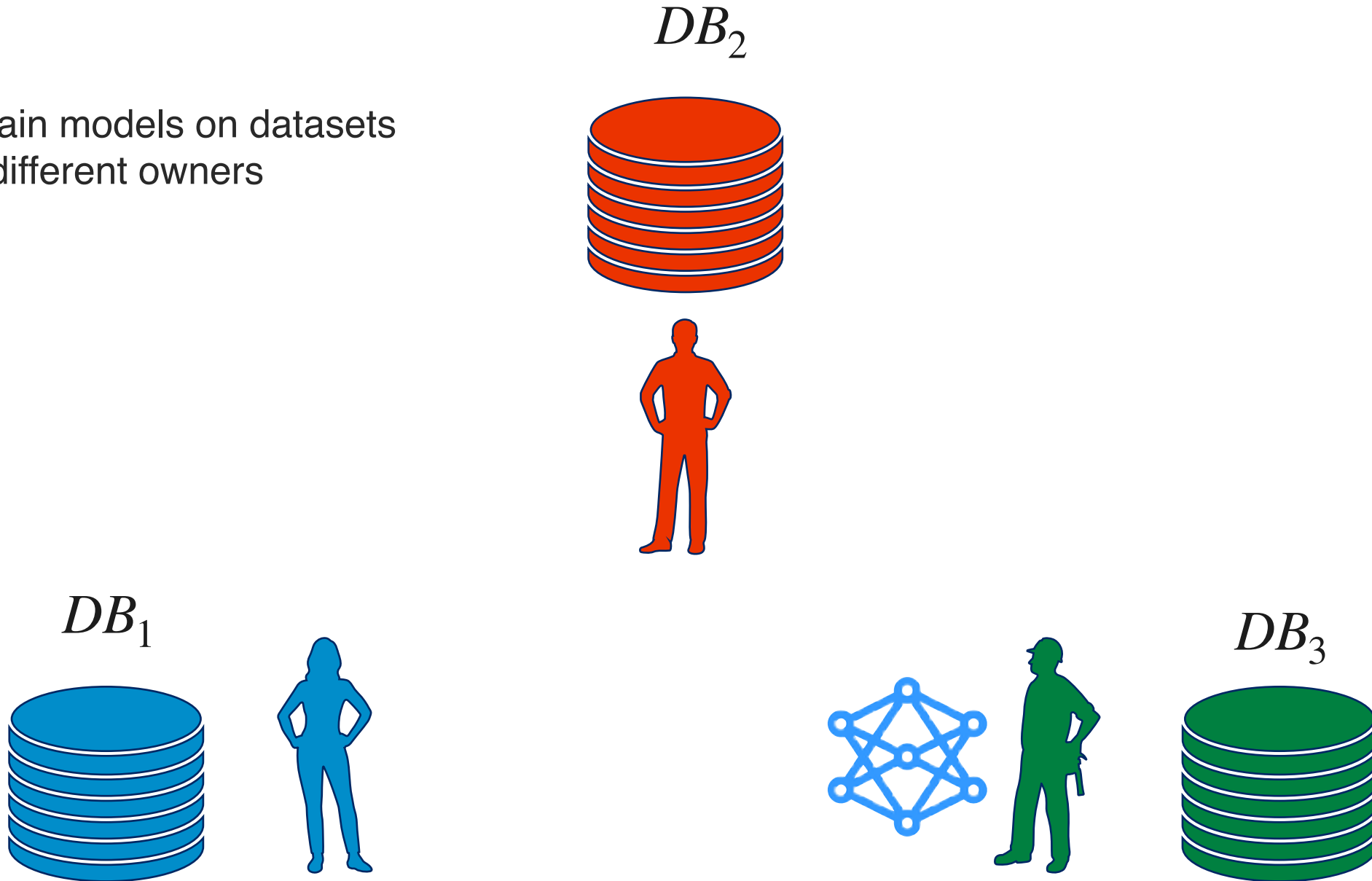
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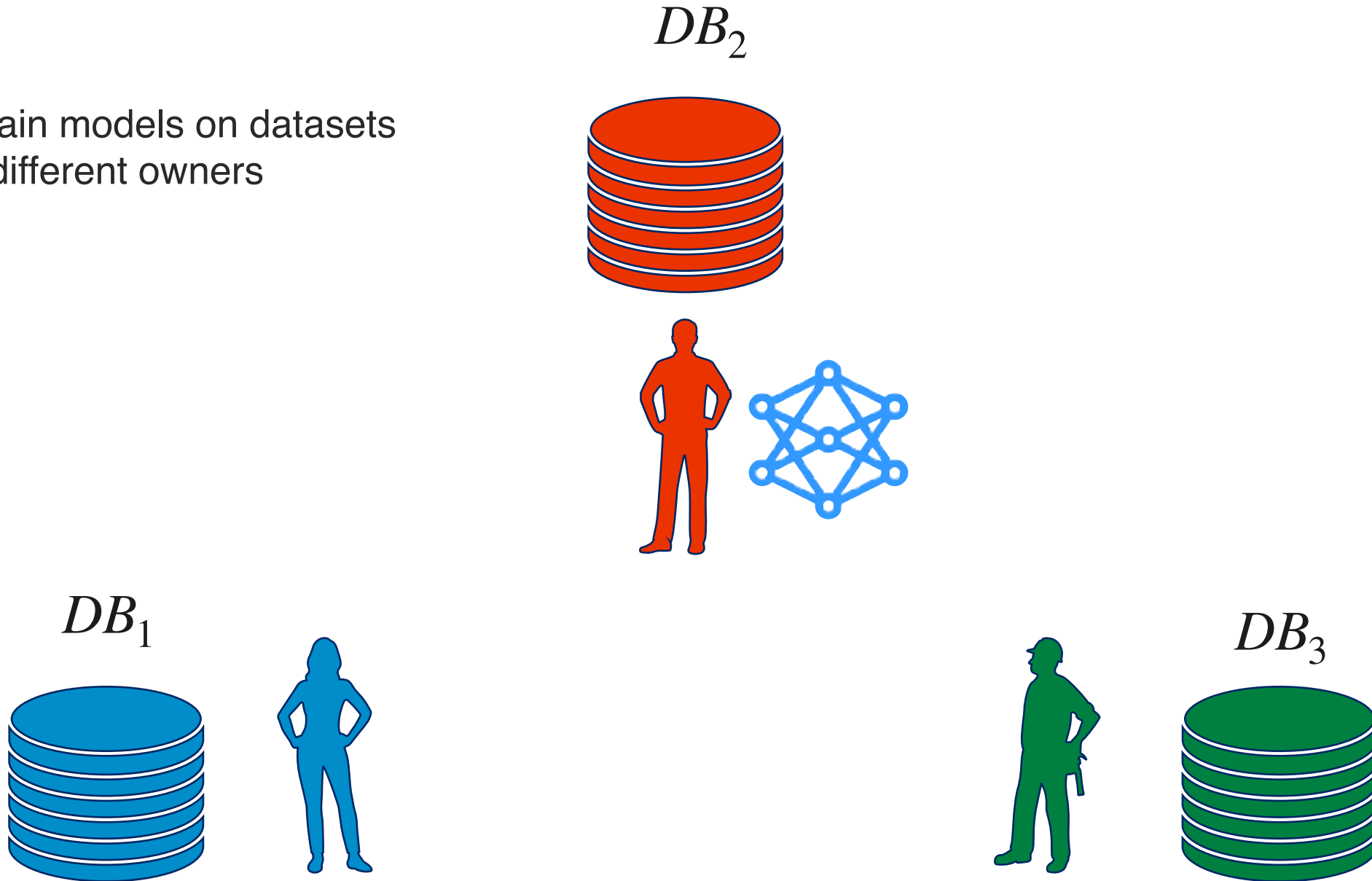
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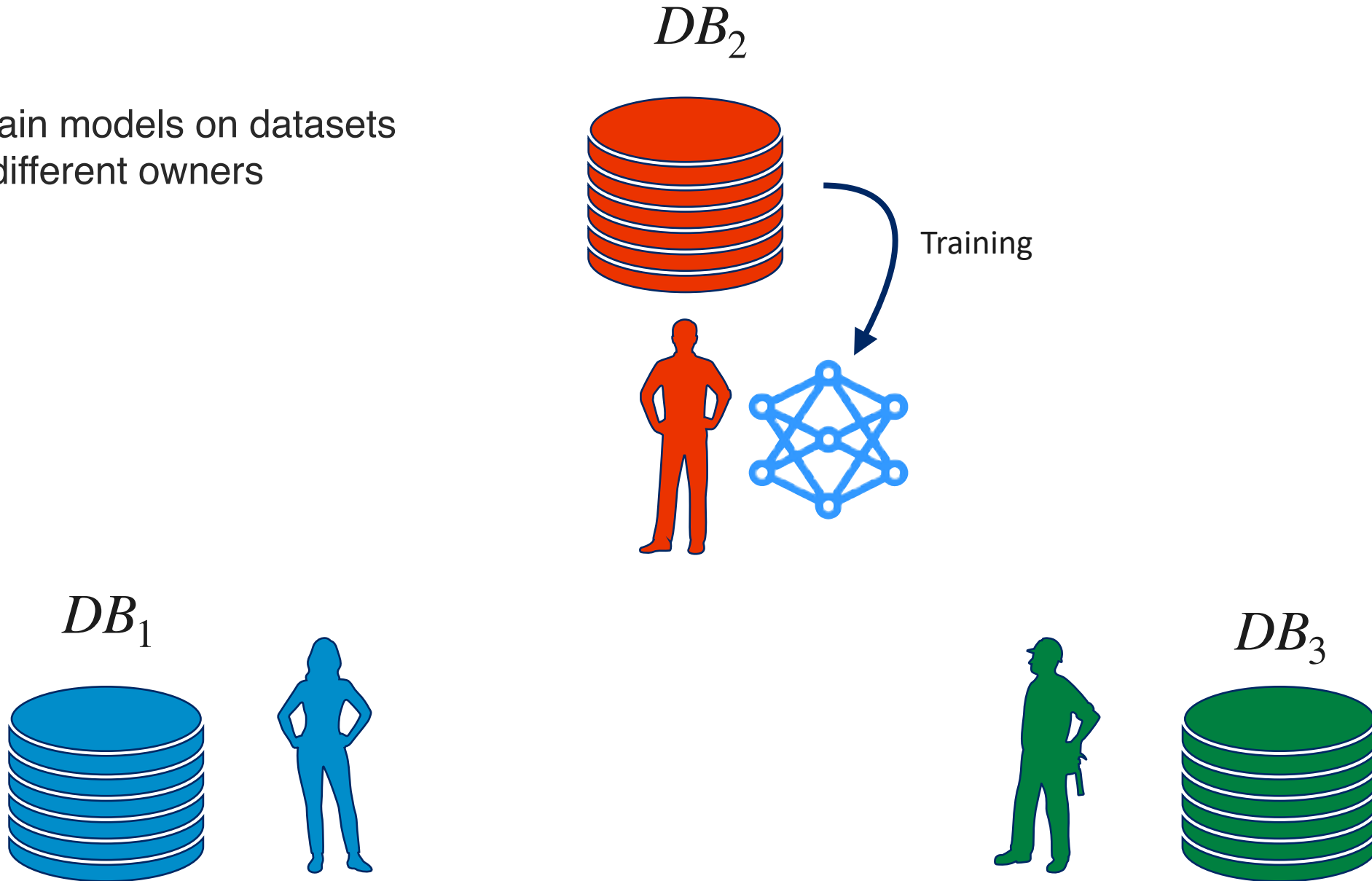
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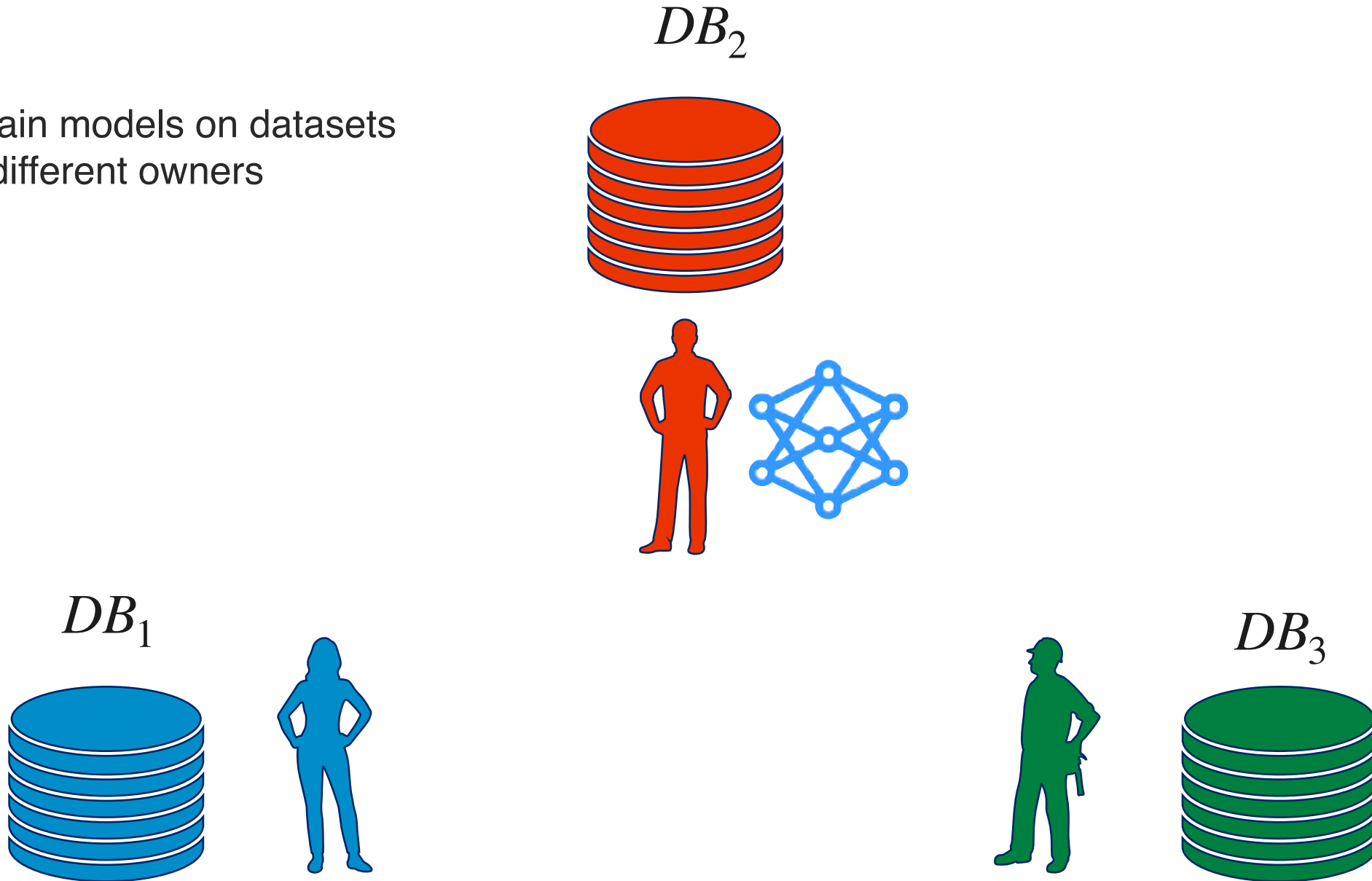
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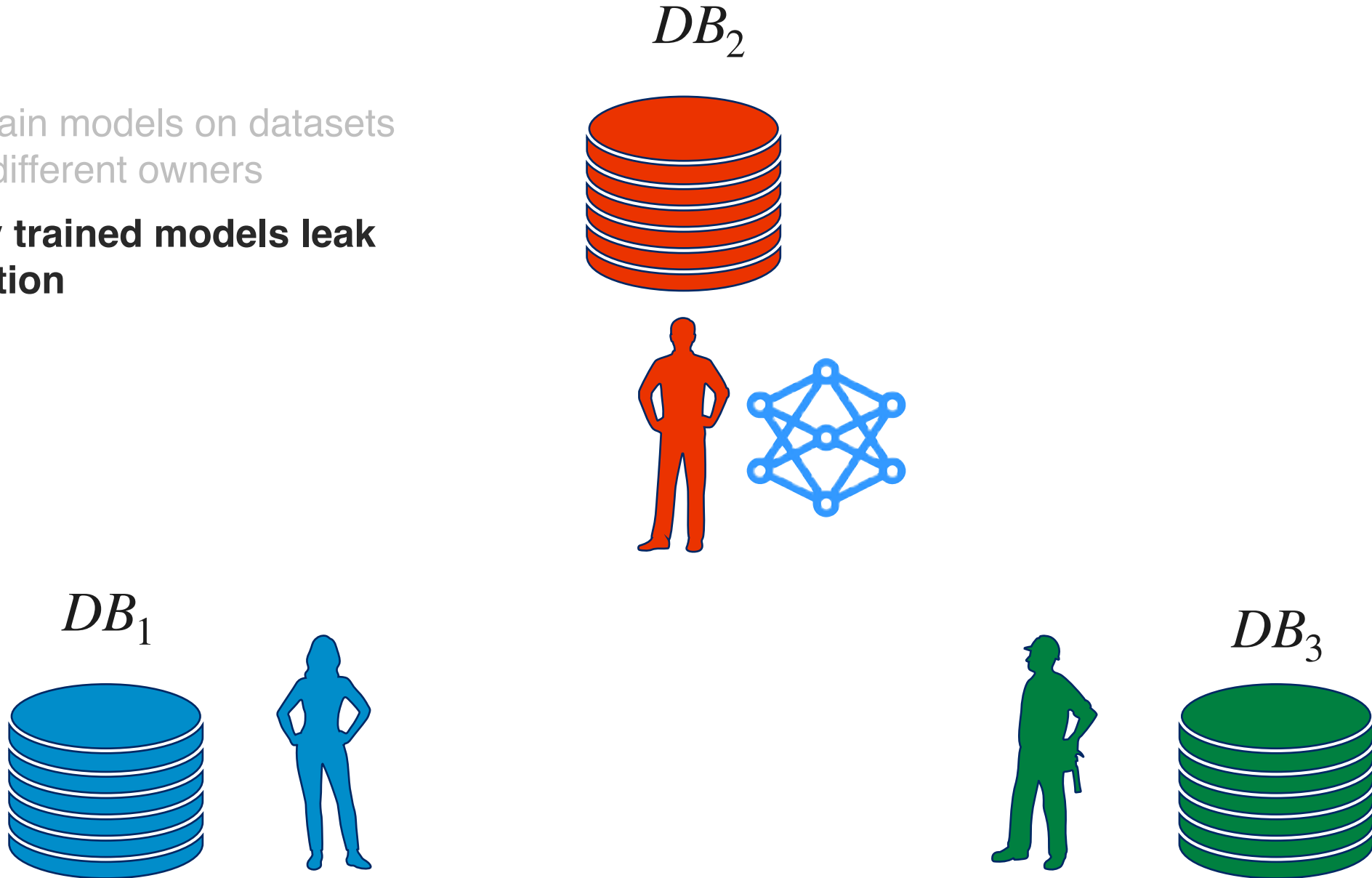
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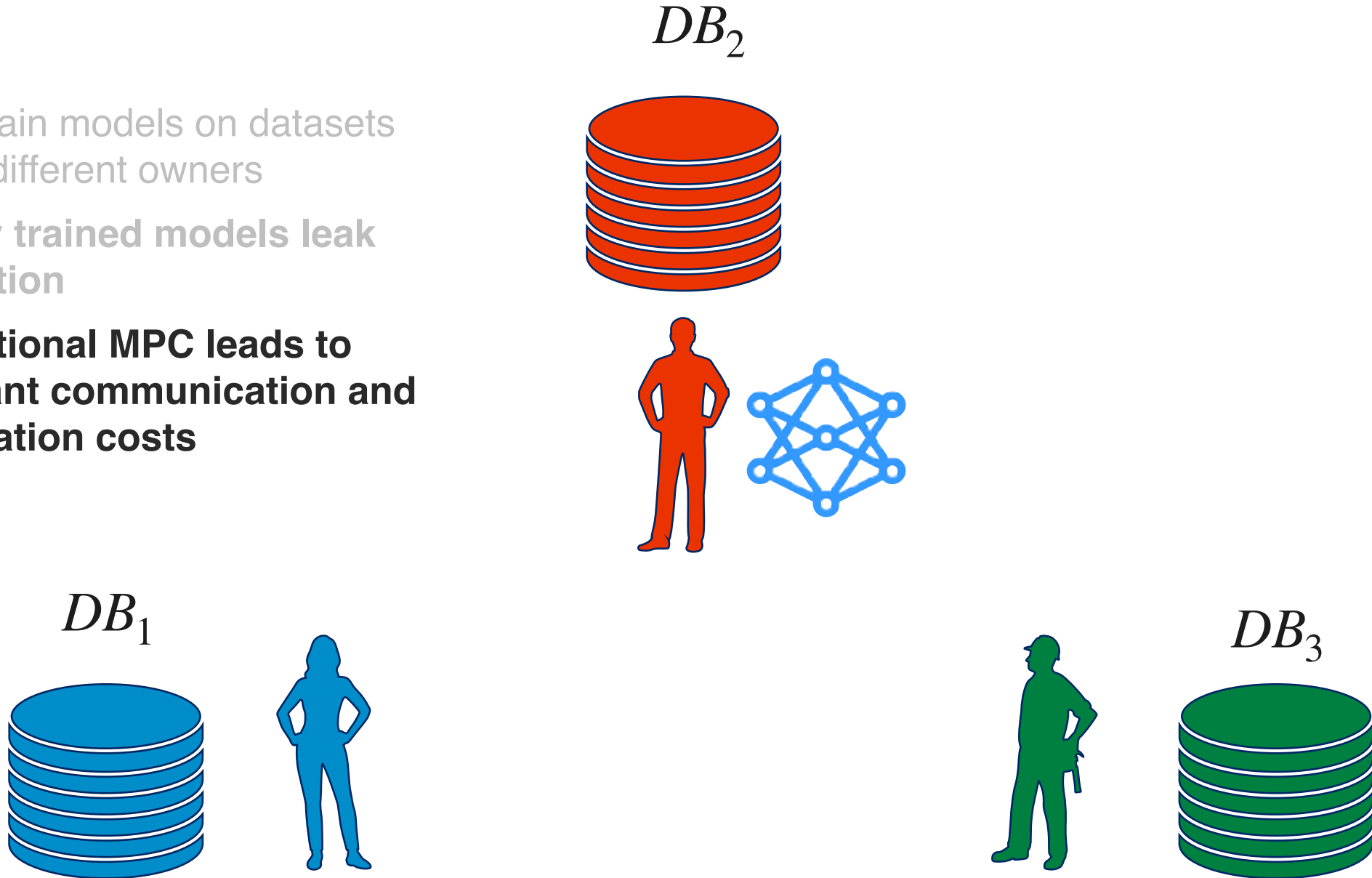
- Jointly train models on datasets held by different owners
- **Partially trained models leak information**





Motivation: Federated Learning

- Jointly train models on datasets held by different owners
- **Partially trained models leak information**
- **Conventional MPC leads to exorbitant communication and computation costs**







Homomorphic Encryption



Homomorphic Encryption

[Gentry STOC'09]

Fully homomorphic encryption using ideal lattices



Homomorphic Encryption

[Gentry STOC'09]

Fully homomorphic encryption using ideal lattices



Bob



Alice



Homomorphic Encryption

[Gentry STOC'09]

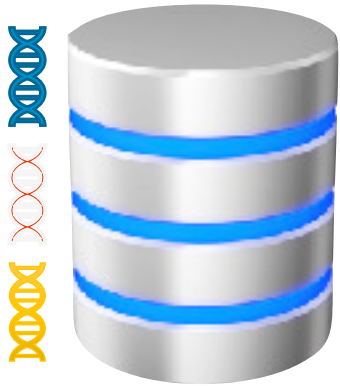
Fully homomorphic encryption using ideal lattices



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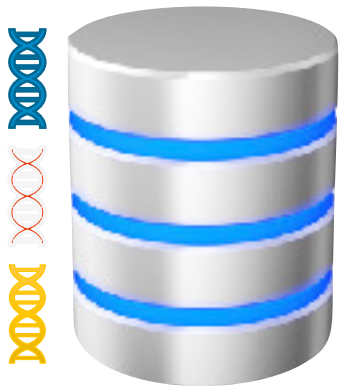
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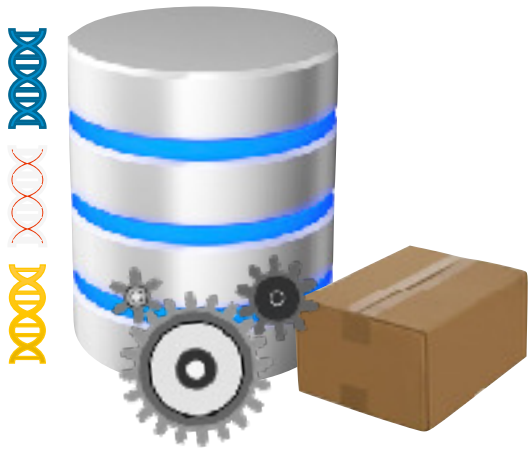
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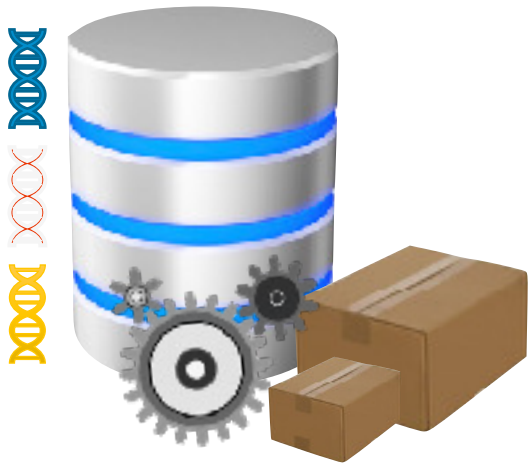
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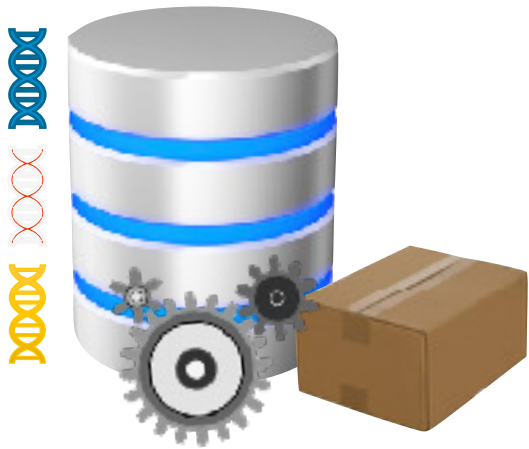
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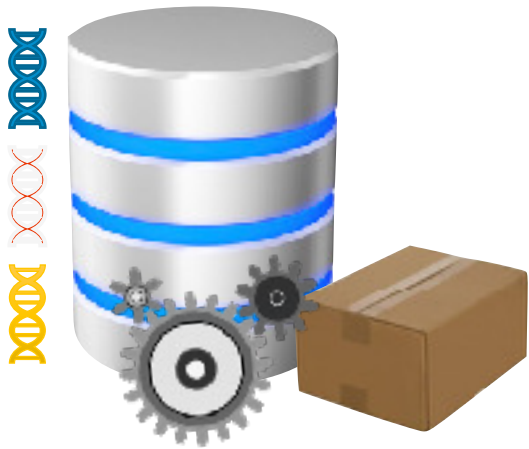
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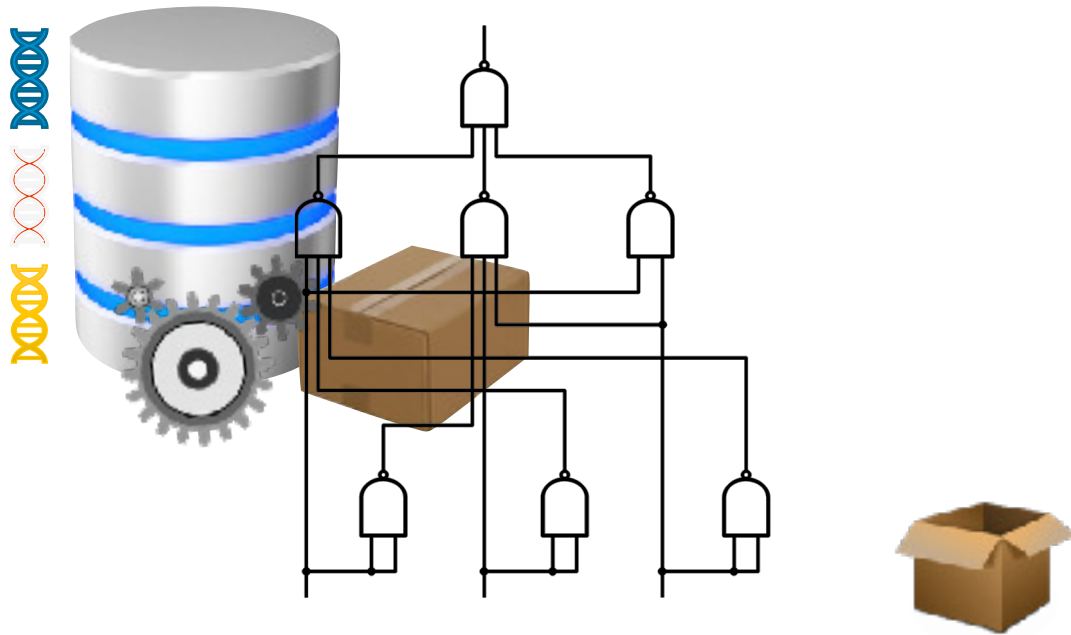
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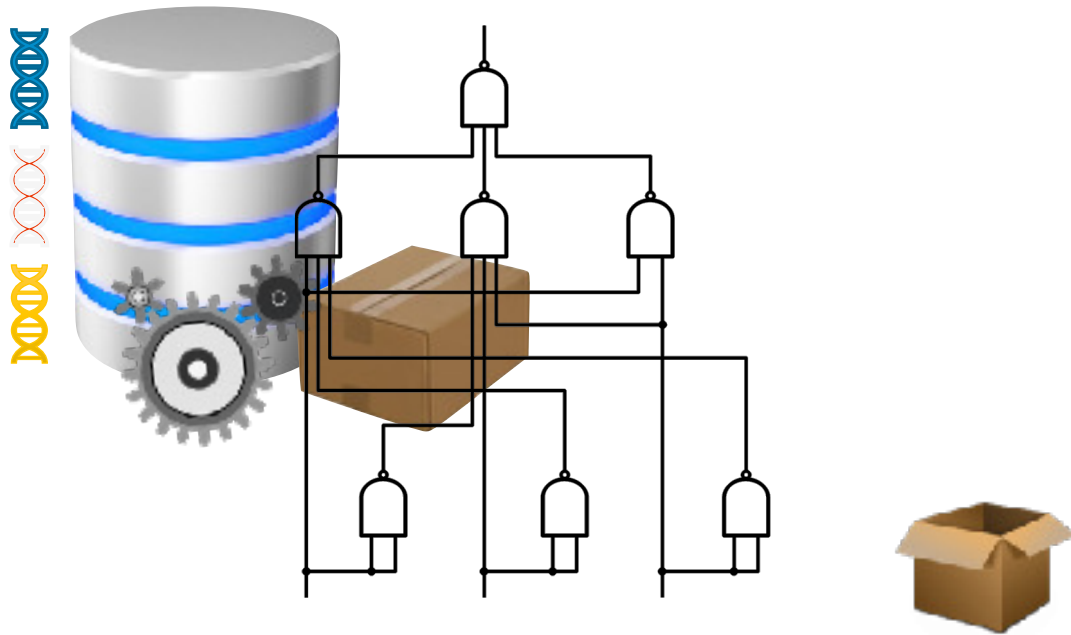
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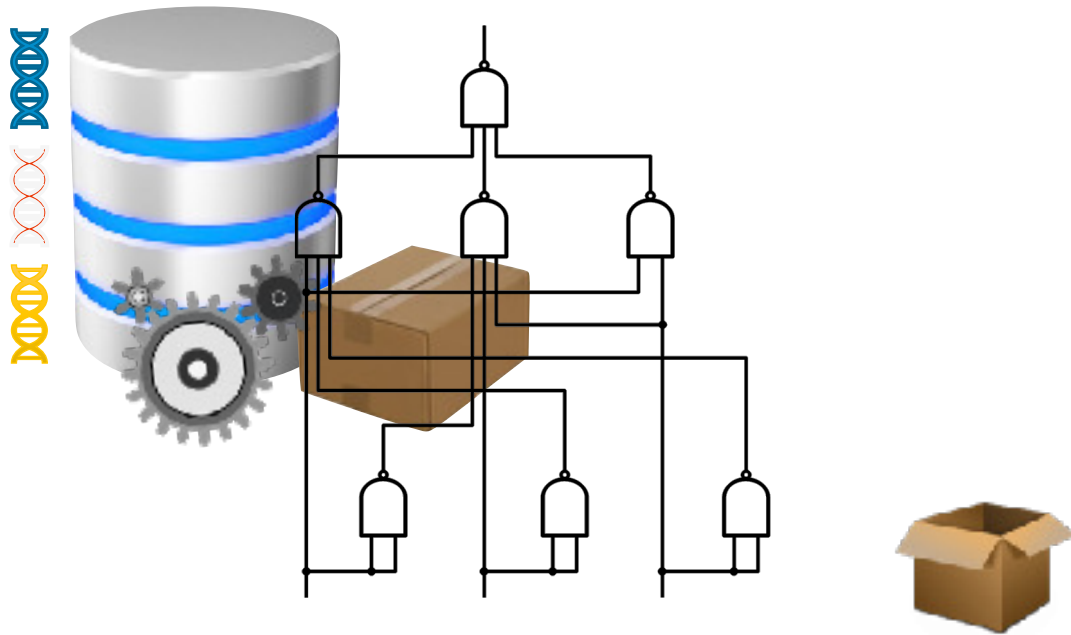
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Laconic Cryptography

[CDGGMP CRYPTO'17]

Laconic Oblivious Transfer and Its Applications



Homomorphic Encryption

[Gentry STOC'09]

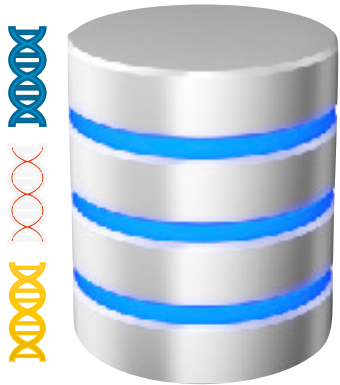
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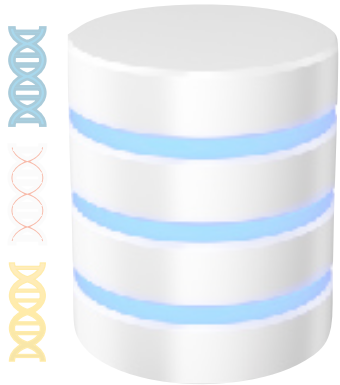
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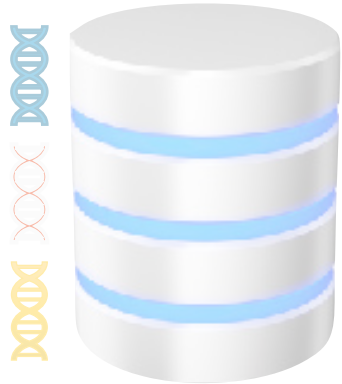
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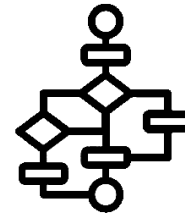
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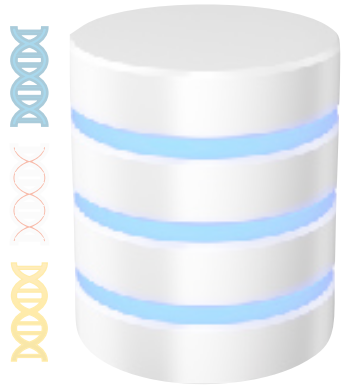
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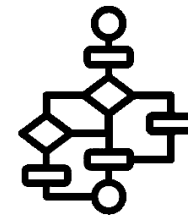
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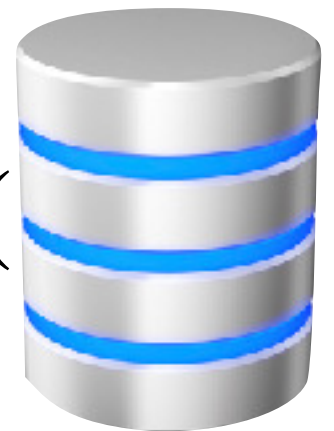
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$$= H(\text{Database})$$





Homomorphic Encryption

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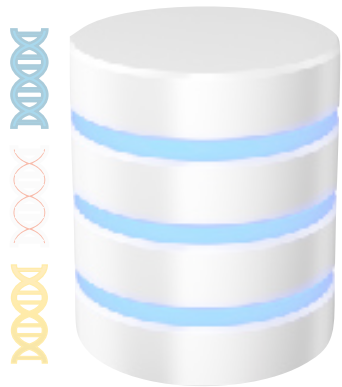
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Laconic Cryptography

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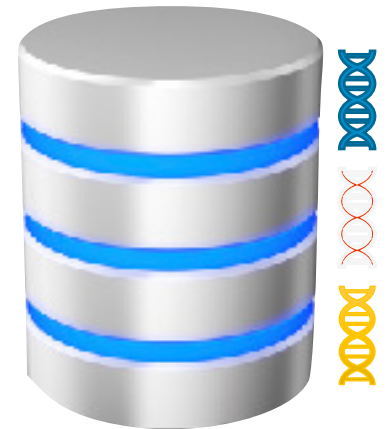
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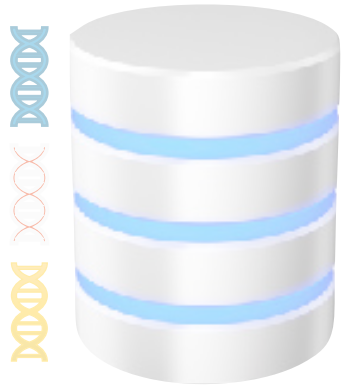
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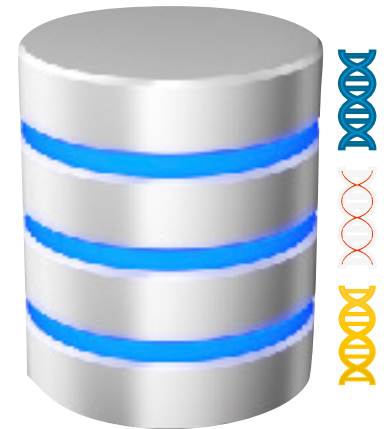
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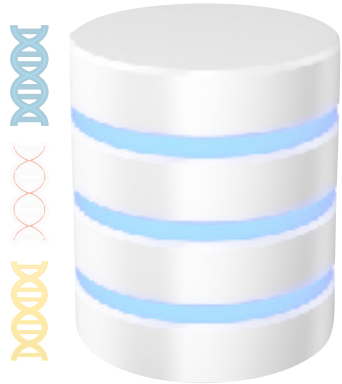
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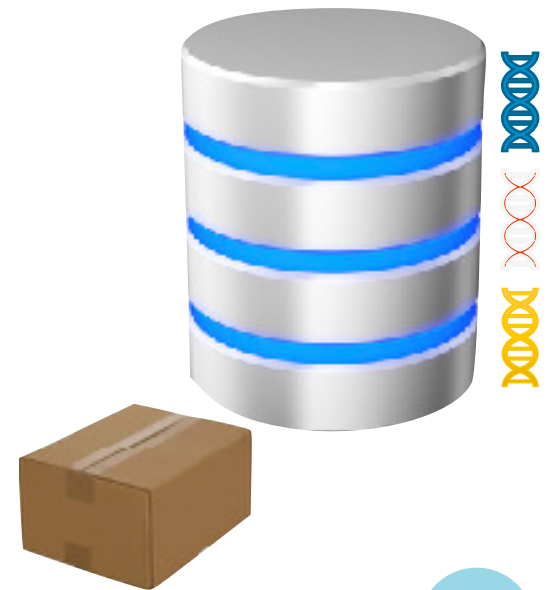
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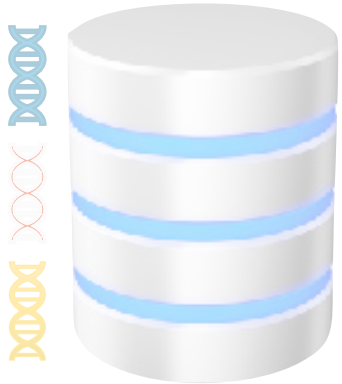
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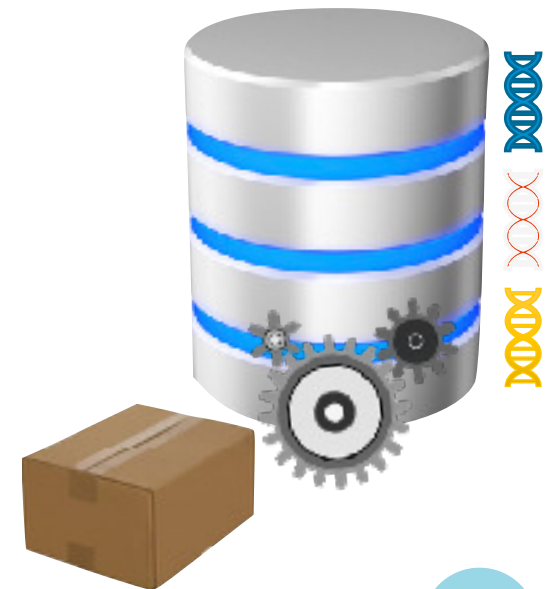
Laconic Oblivious Transfer and Its Applications



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Fully homomorphic encryption using ideal lattices



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Laconic Cryptography

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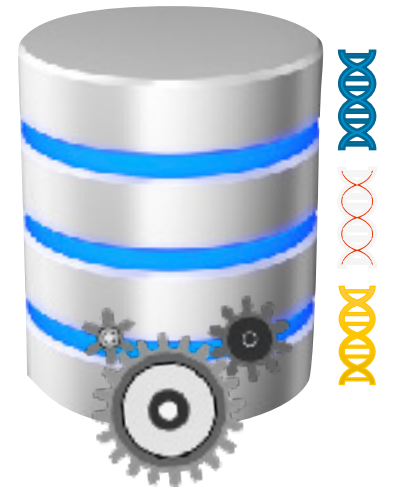
Laconic Oblivious Transfer and Its Applications



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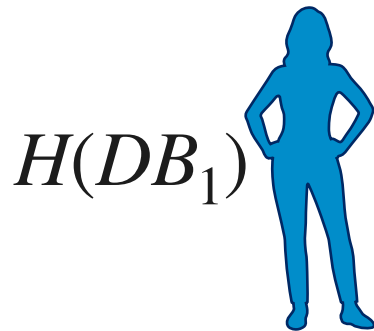
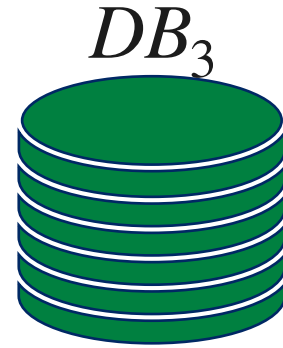
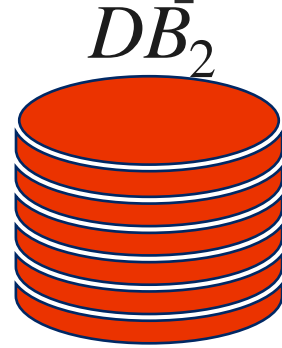
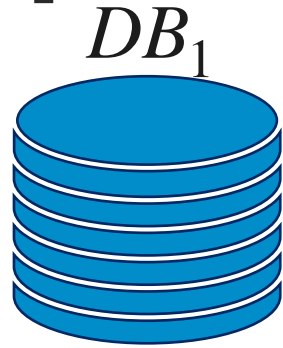




Paradigms

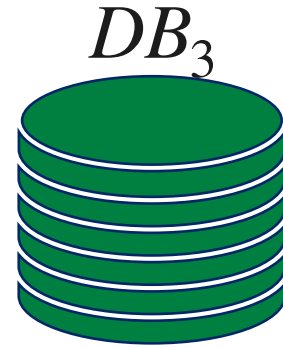
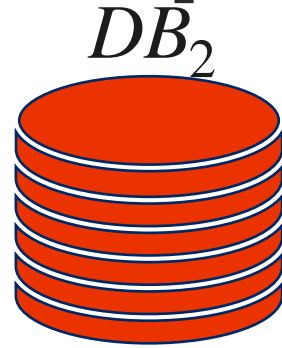
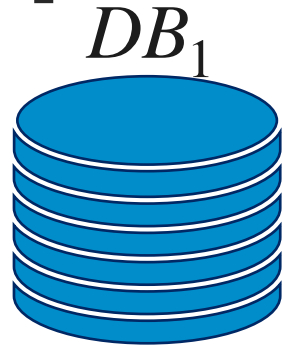


RAM Delegation [CDGGMP17]





RAM Delegation [CDGGMP17]



$H(DB_3)$
 P_3



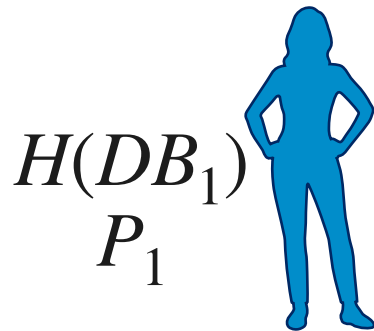
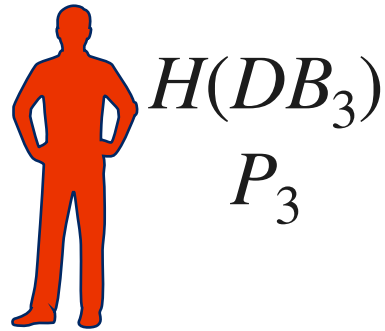
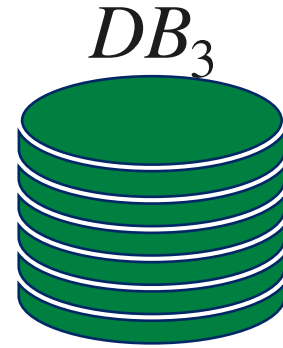
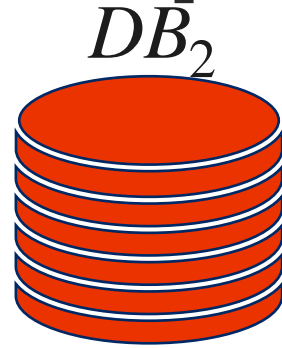
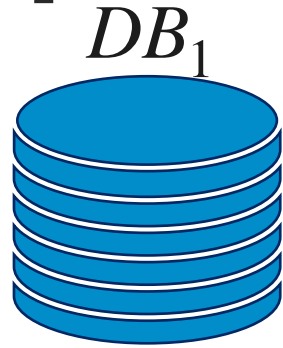
$H(DB_1)$
 P_1



$H(DB_2)$
 P_2



RAM Delegation [CDGGMP17]

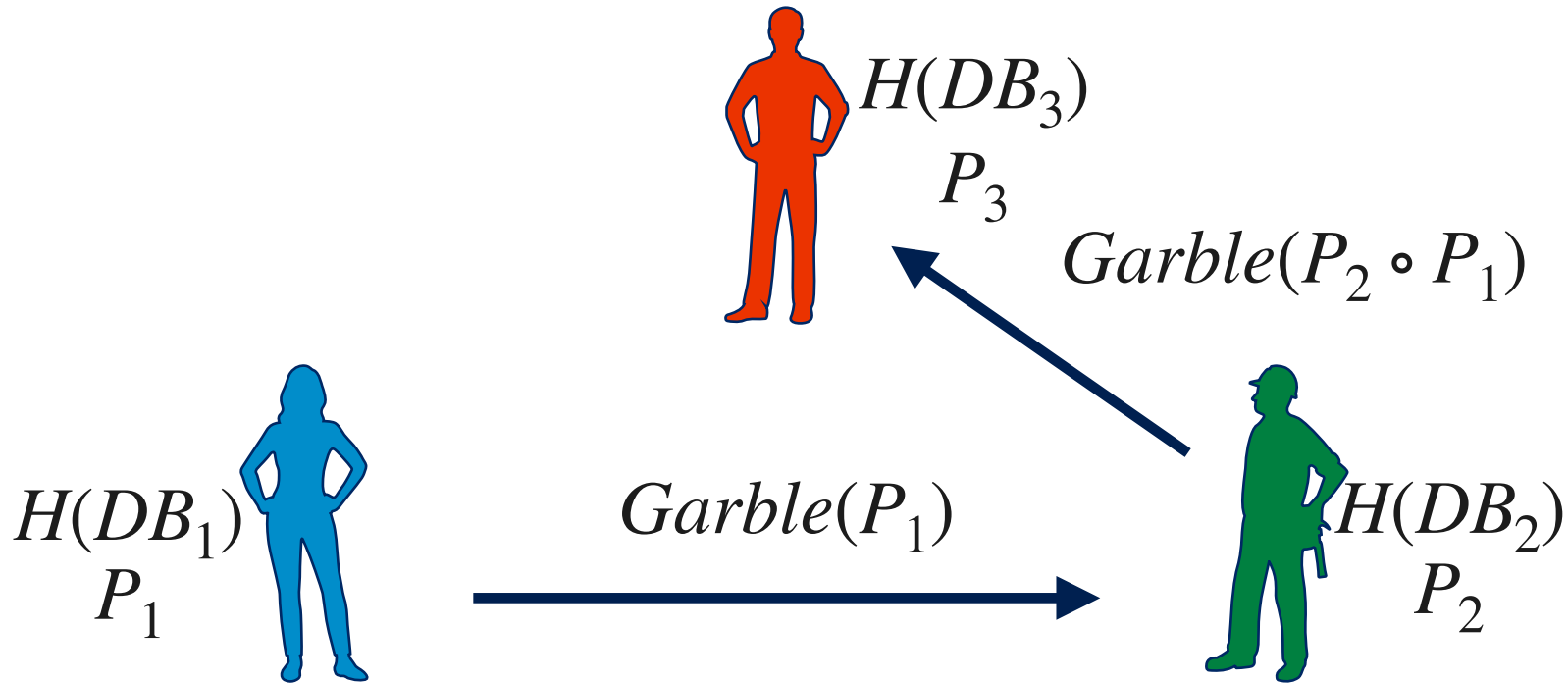
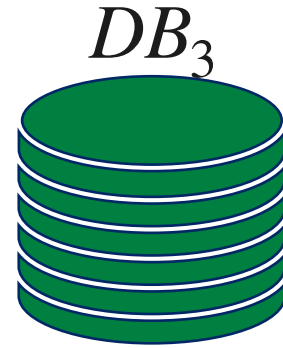
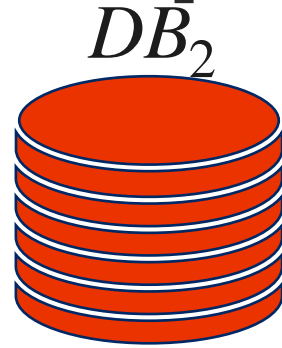
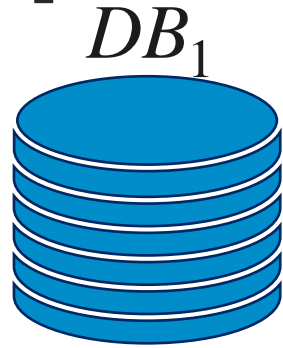


$Garble(P_1)$



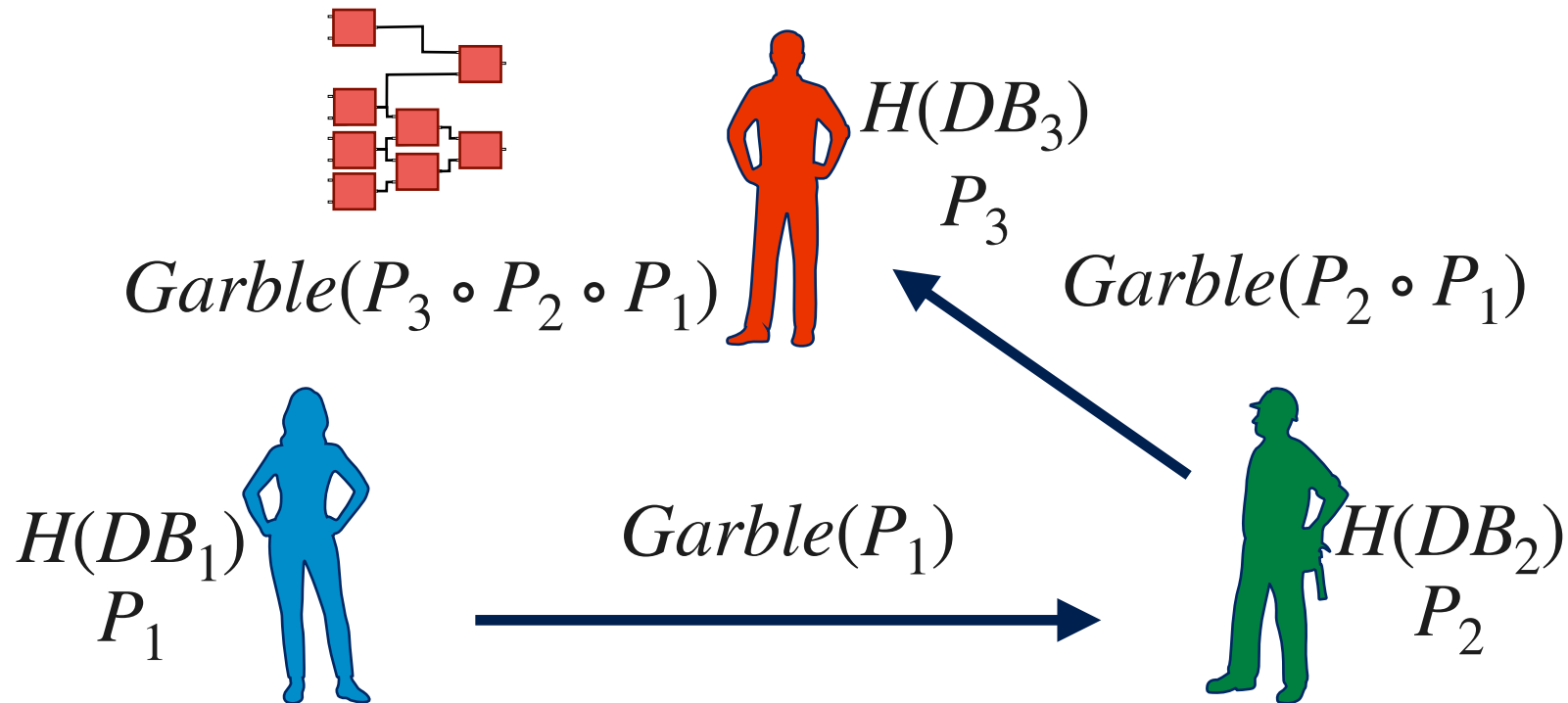
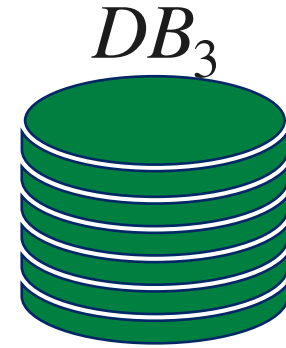
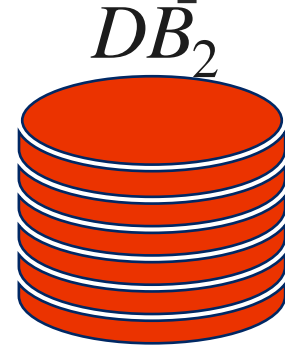
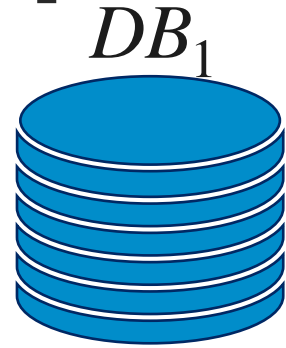


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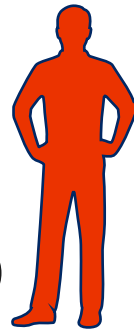
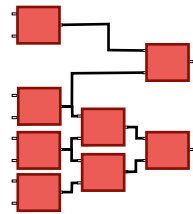
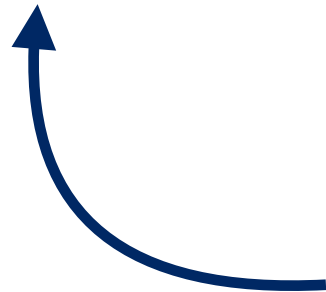
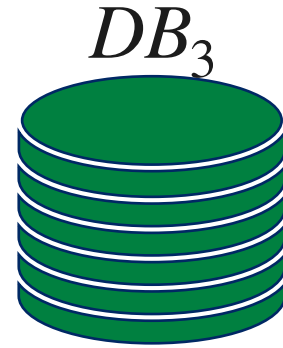
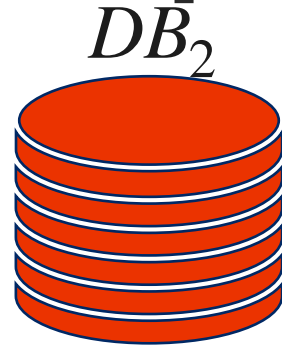
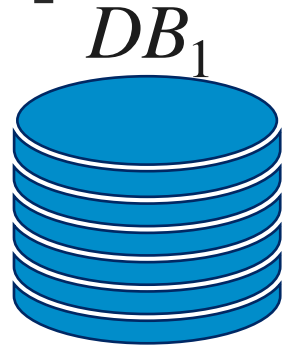


RAM Delegation [CDGGMP17]





RAM Delegation [CDGGMP17]



$H(DB_3)$

P_3

$Garble(P_3 \circ P_2 \circ P_1)$

$Garble(P_2 \circ P_1)$

$H(DB_1)$

P_1



$Garble(P_1)$



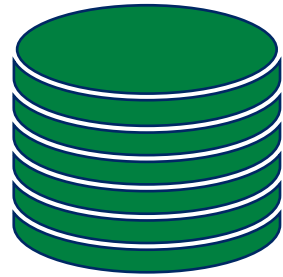
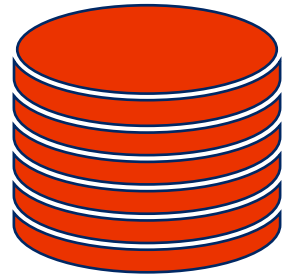
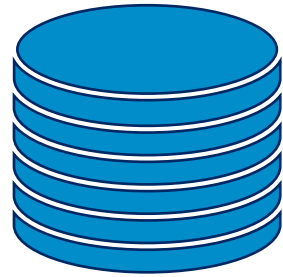
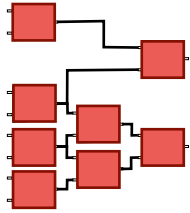
$H(DB_2)$

P_2



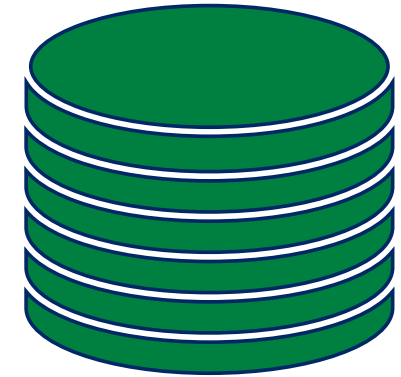
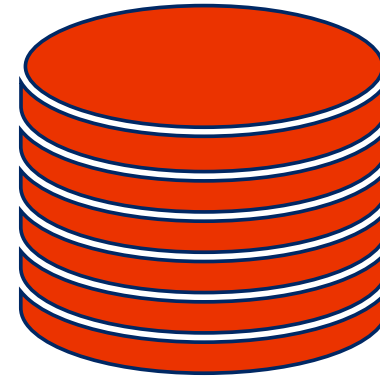
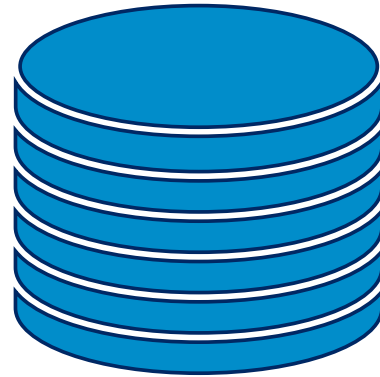
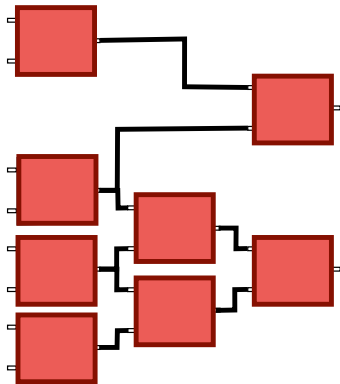


RAM Delegation [CDGGMP17]



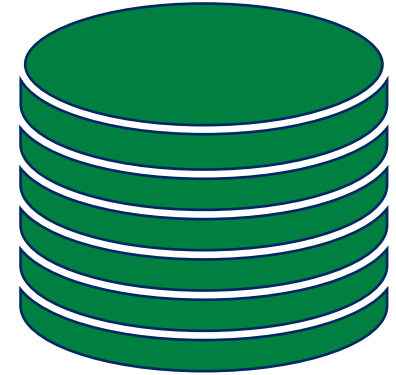
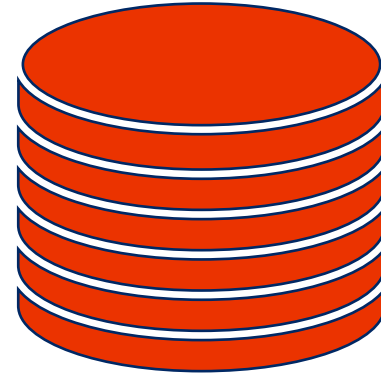
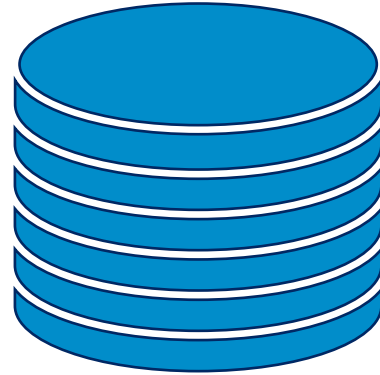
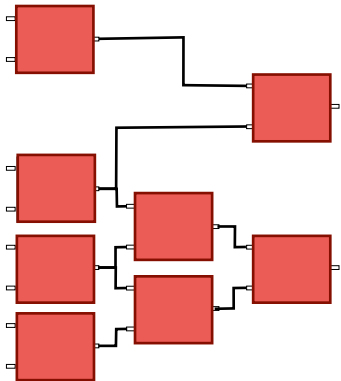


RAM Delegation [CDGGMP17]



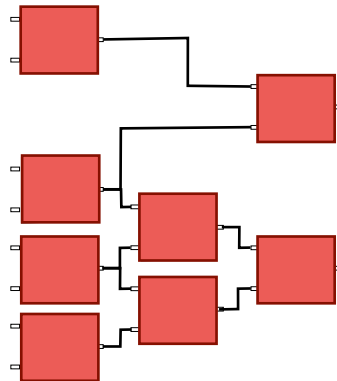
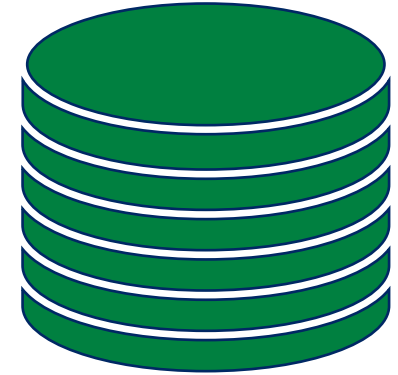
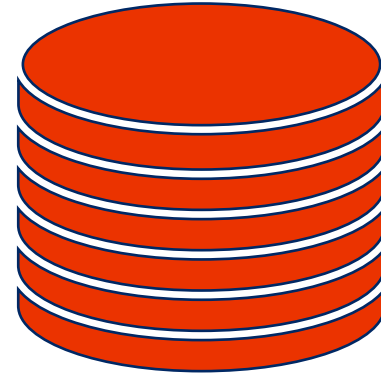
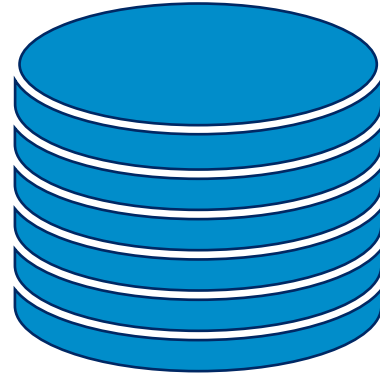


RAM Delegation [CDGGMP17]



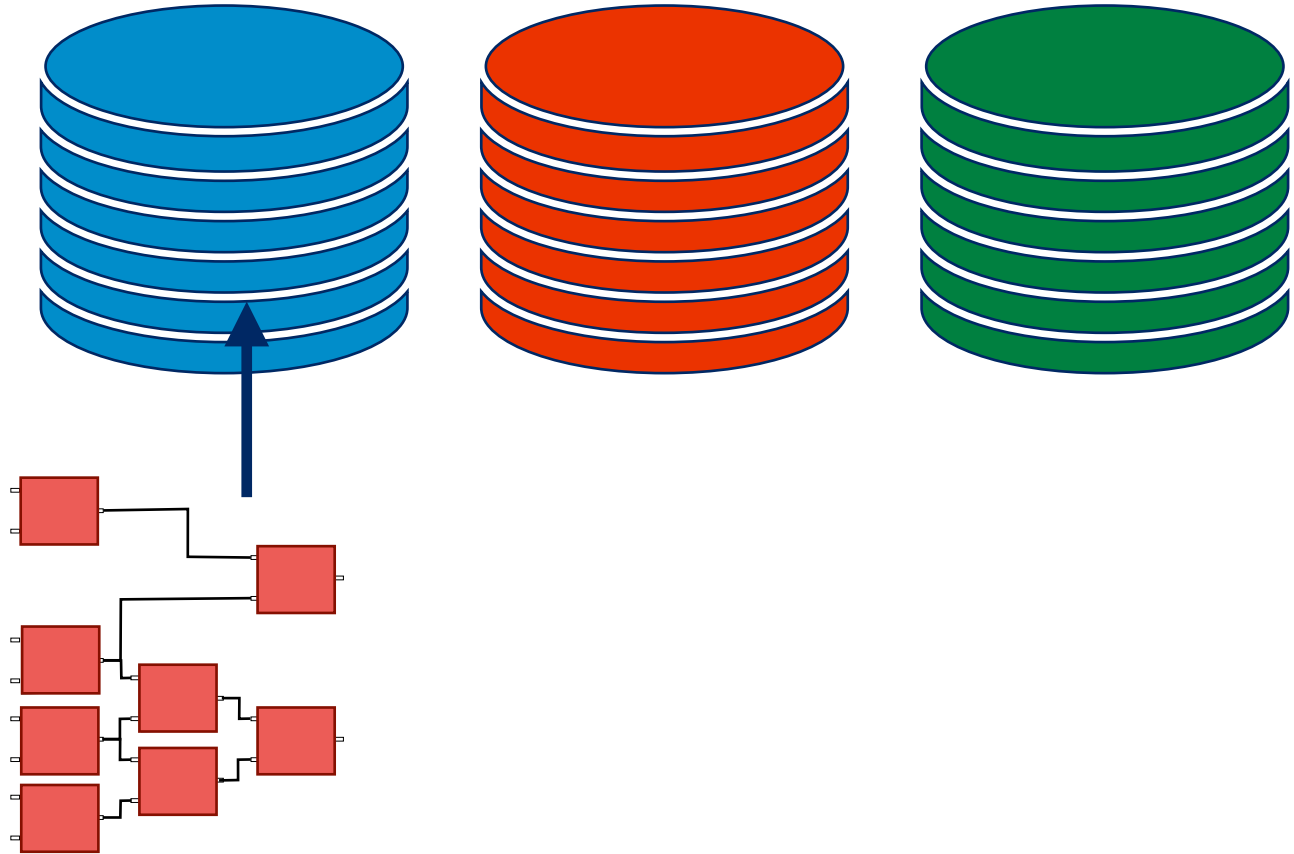


RAM Delegation [CDGGMP17]



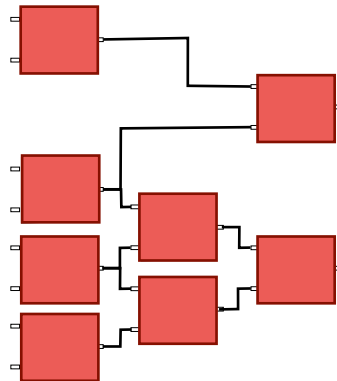
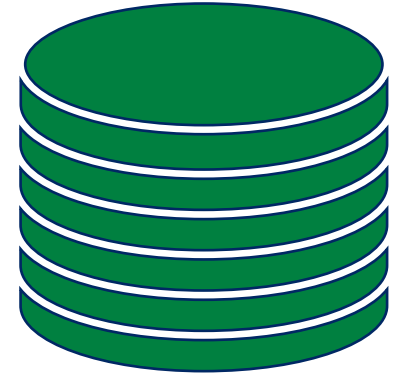
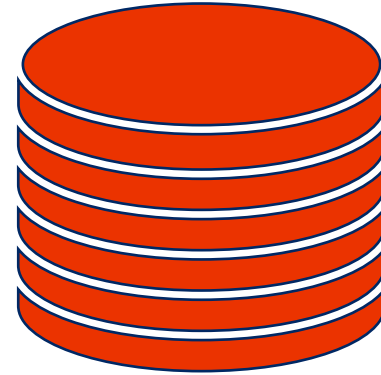
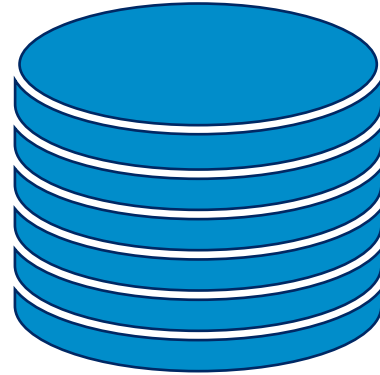


RAM Delegation [CDGGMP17]



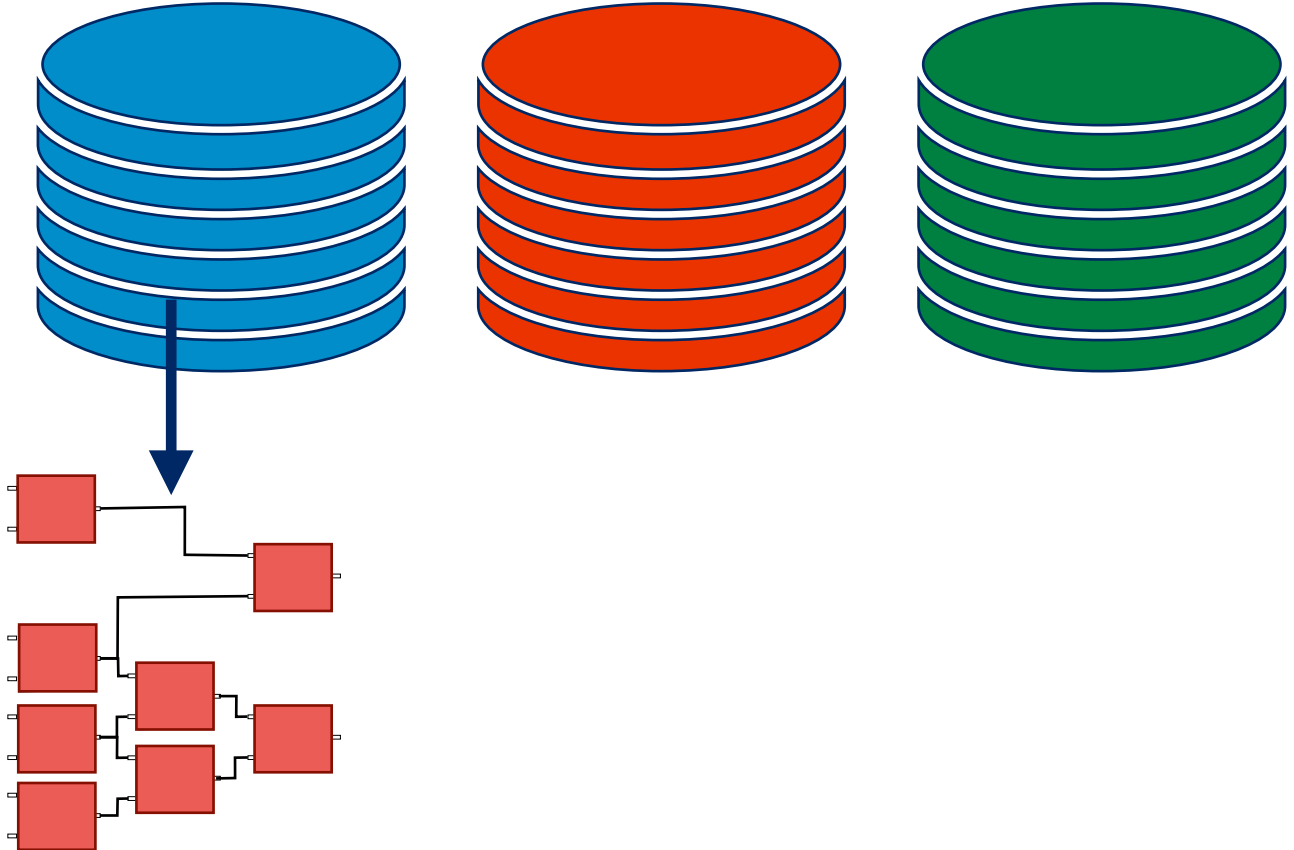


RAM Delegation [CDGGMP17]



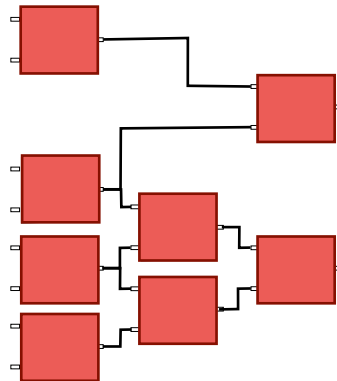
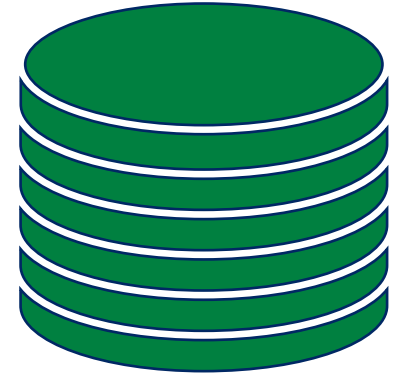
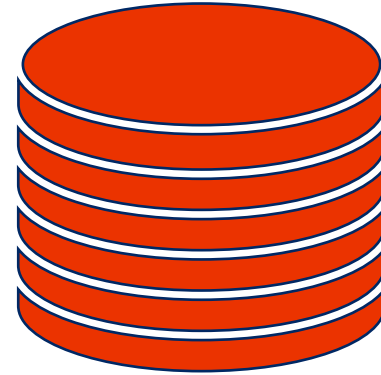
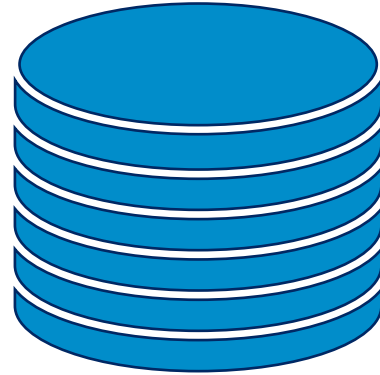


RAM Delegation [CDGGMP17]



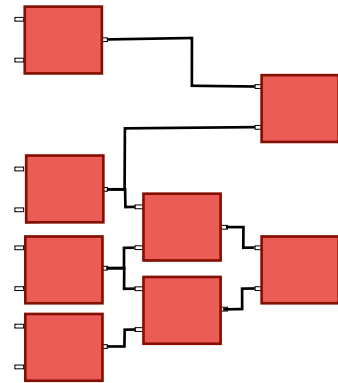
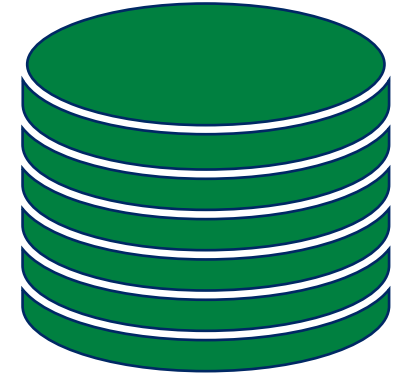
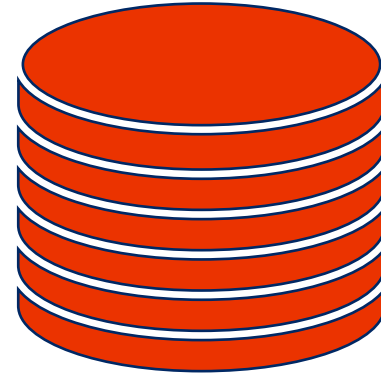
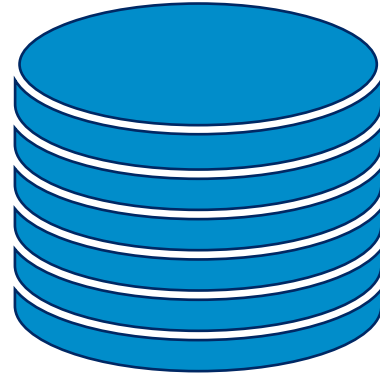


RAM Delegation [CDGGMP17]



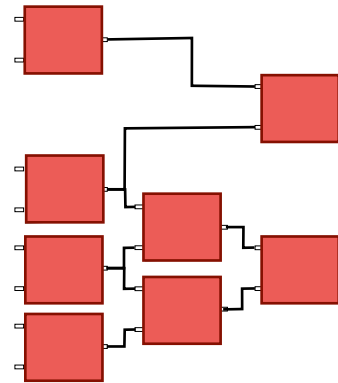
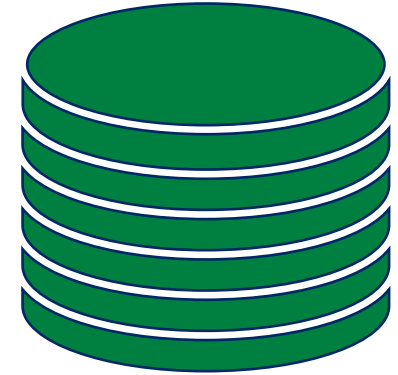
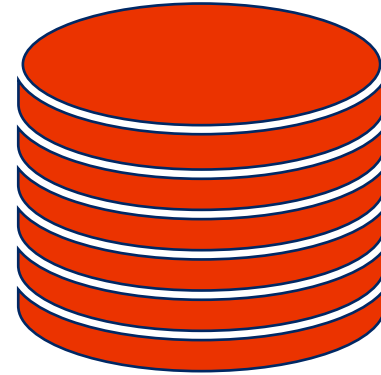
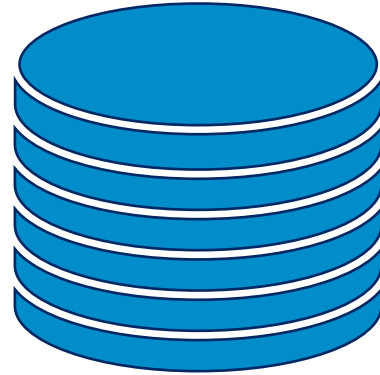


RAM Delegation [CDGGMP17]



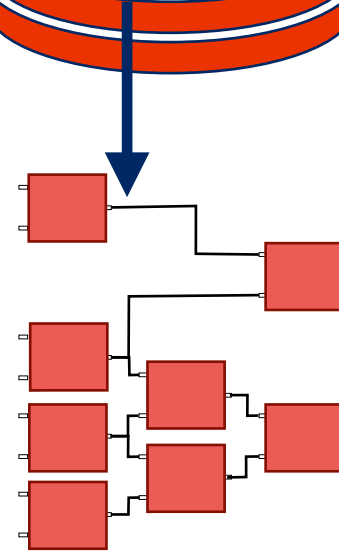
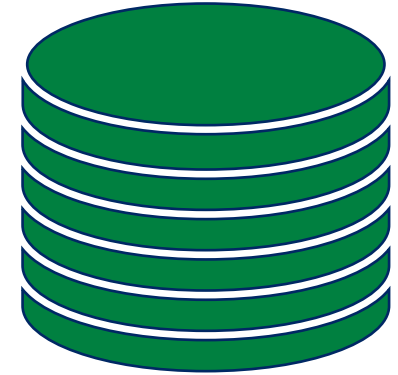
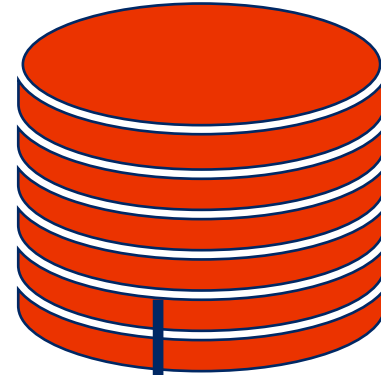
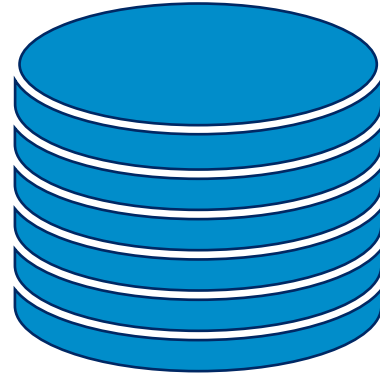


RAM Delegation [CDGGMP17]



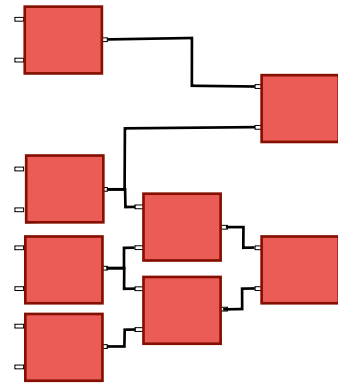
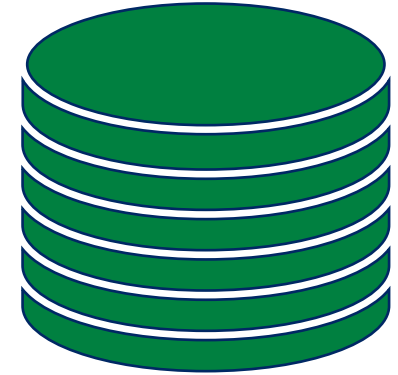
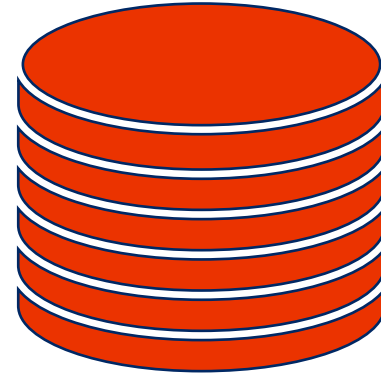
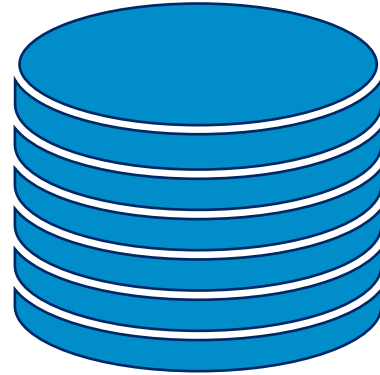


RAM Delegation [CDGGMP17]



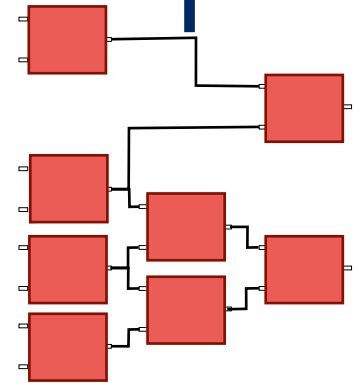
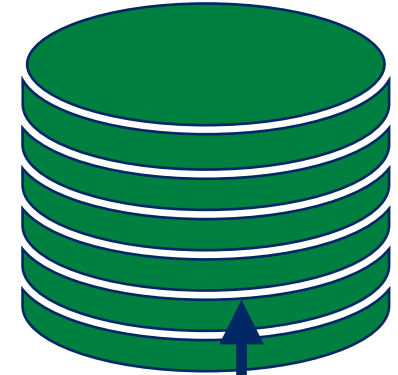
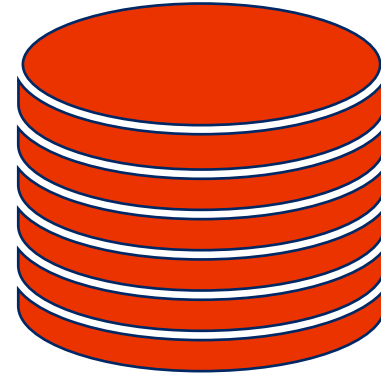
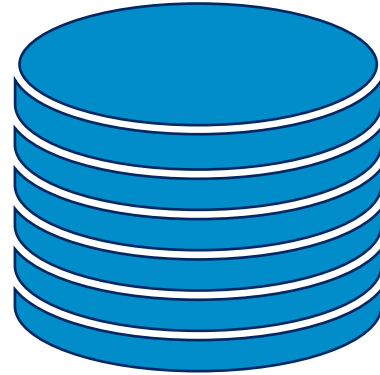


RAM Delegation [CDGGMP17]



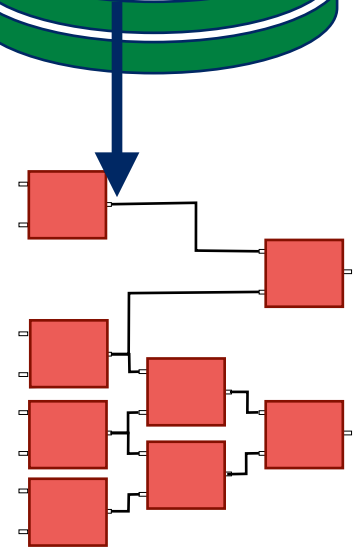
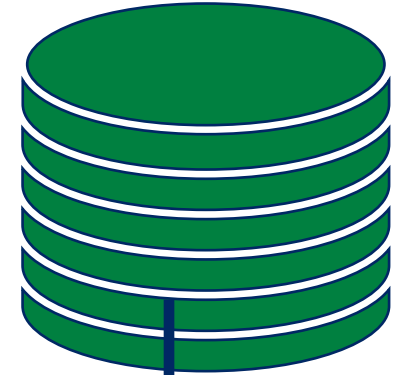
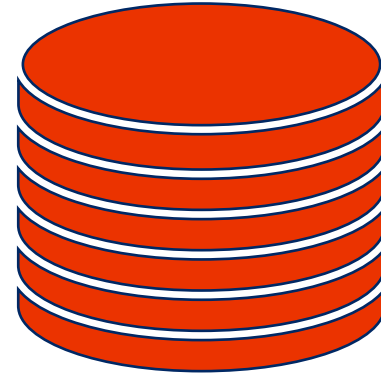
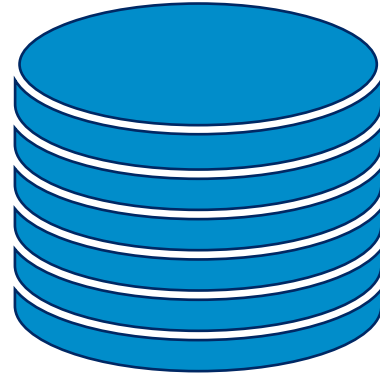


RAM Delegation [CDGGMP17]



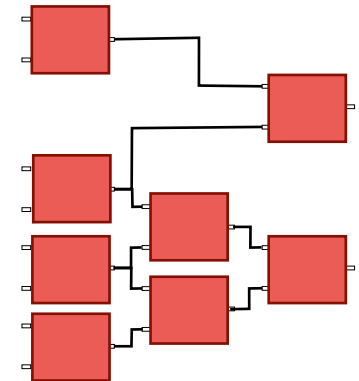
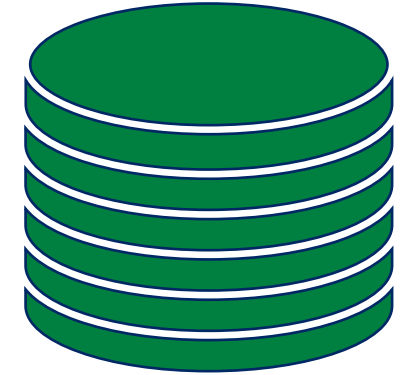
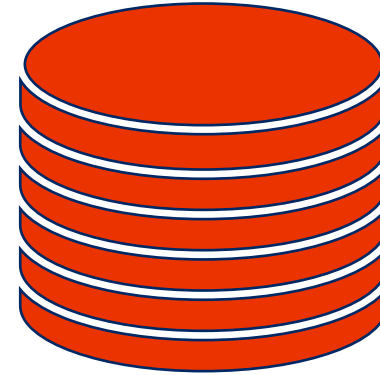
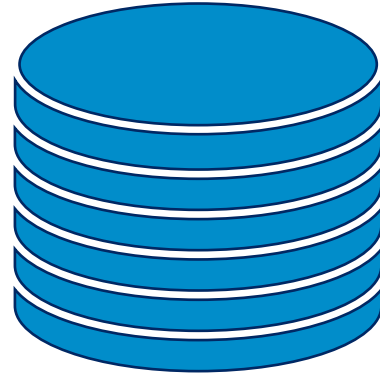


RAM Delegation [CDGGMP17]



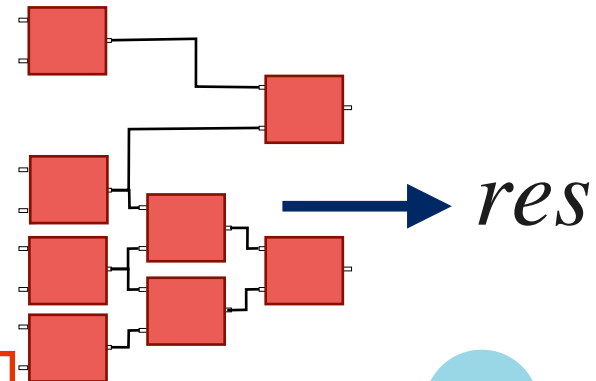
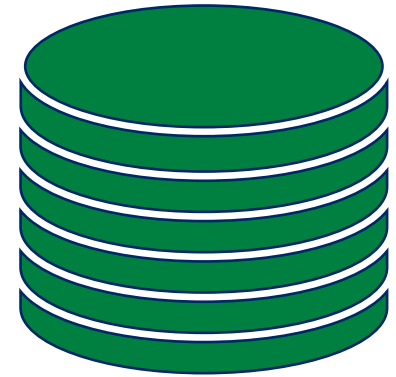
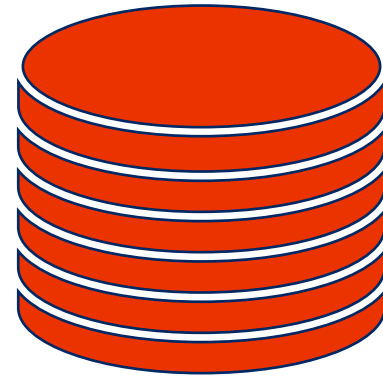
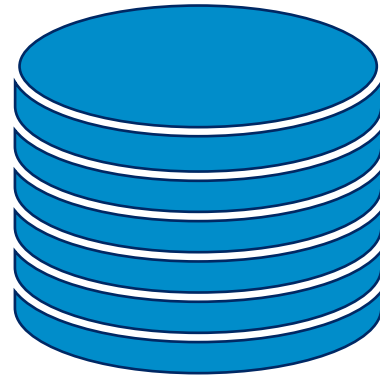


RAM Delegation [CDGGMP17]





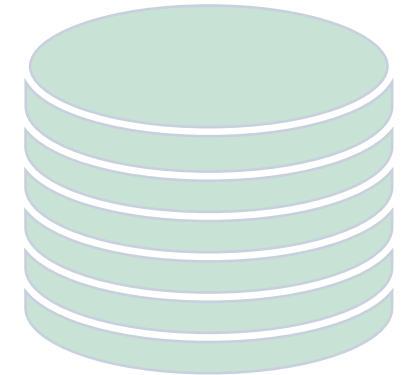
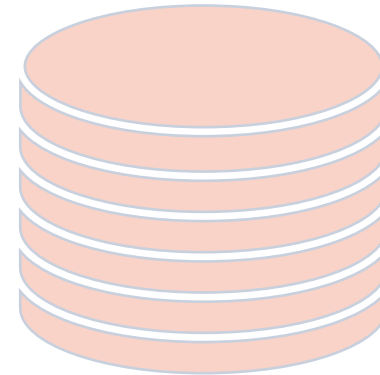
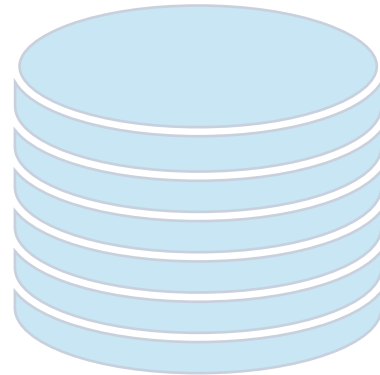
RAM Delegation [CDGGMP17]



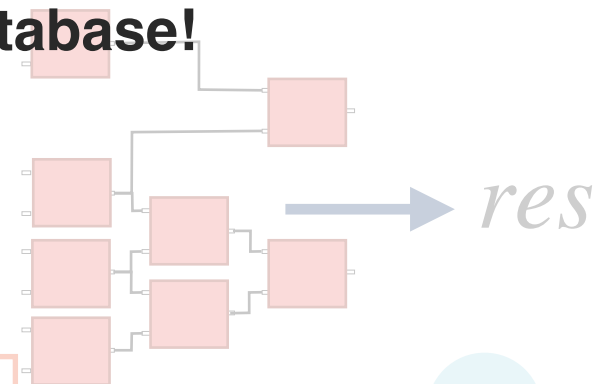
Nothing more than *res* is revealed, even if parties collude



RAM Delegation [CDGGMP17]



Need a primitive to let garbled program access large database!



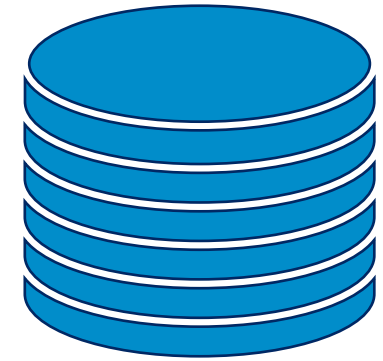
Nothing more than *res* is revealed, even if parties collude



Laconic OT



i, m_0, m_1



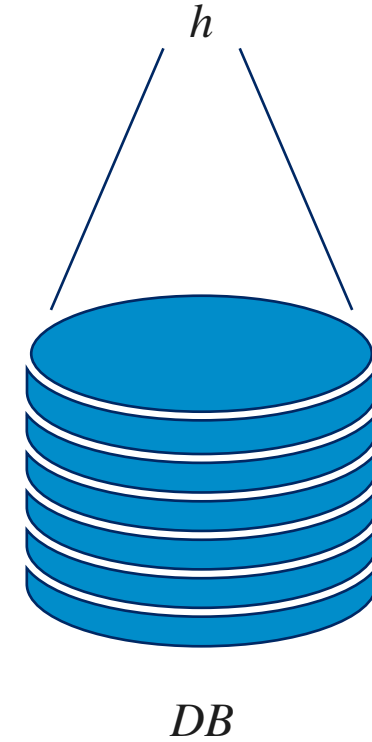
DB



Laconic OT



i, m_0, m_1





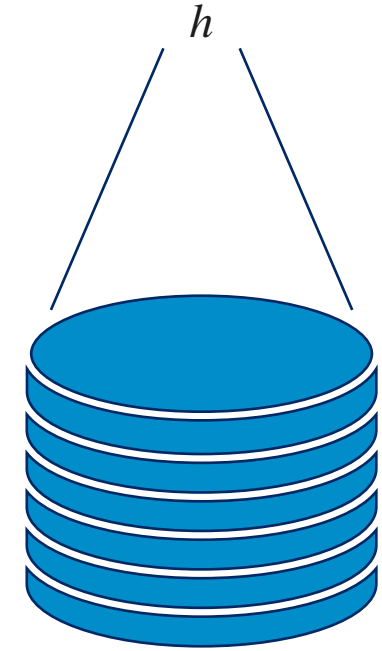
Laconic OT



i, m_0, m_1



h



DB





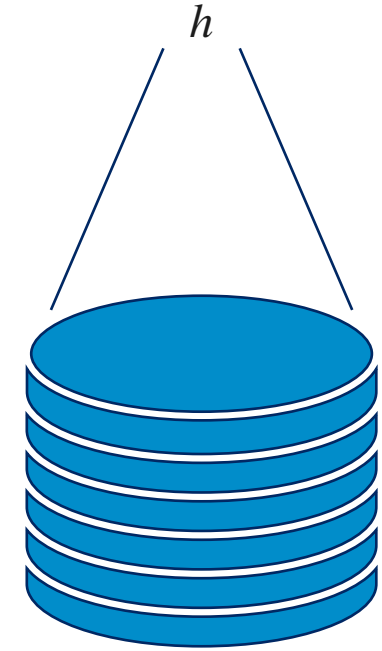
Laconic OT



i, m_0, m_1



$$c = \text{Enc}(h, i, m_0, m_1)$$



DB



Laconic OT



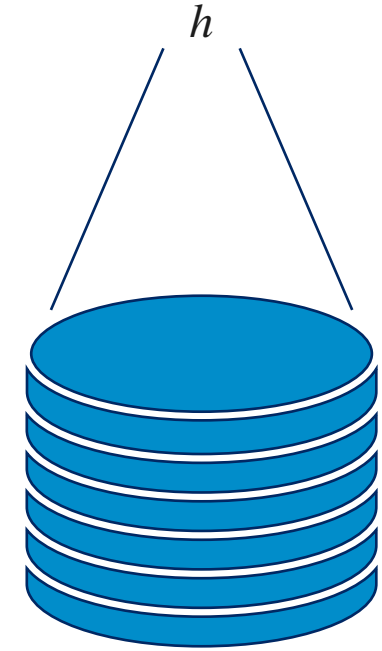
i, m_0, m_1

h



$c = Enc(h, i, m_0, m_1)$

c



DB





Laconic OT



i, m_0, m_1

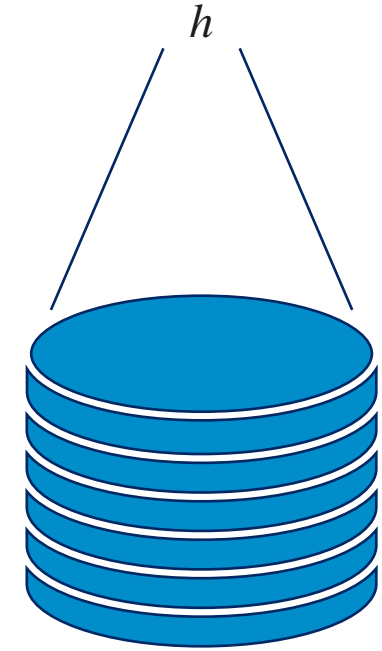


h

$$c = \text{Enc}(h, i, m_0, m_1)$$



c



DB



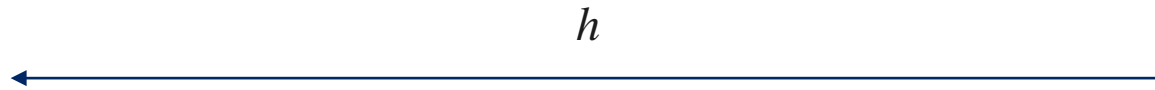
$$m_{DB_i} = \text{Dec}(DB, c)$$



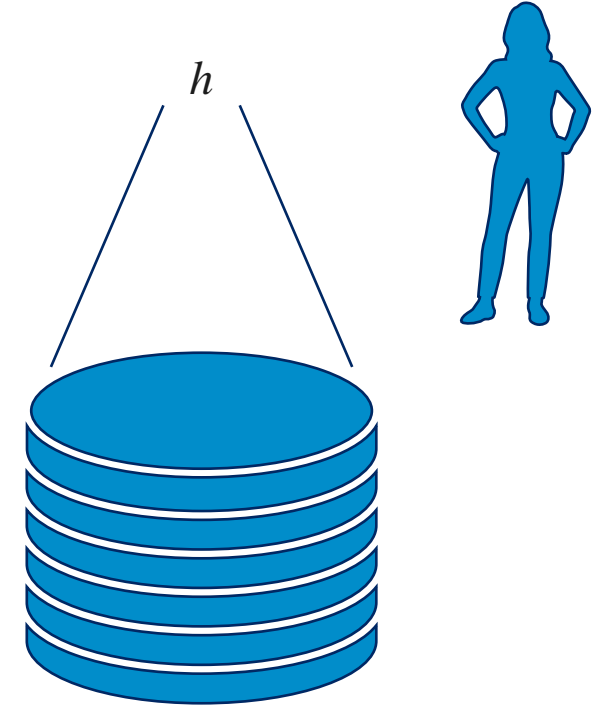
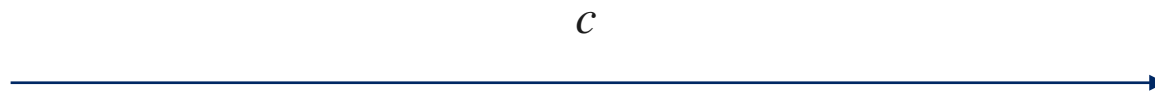
Laconic OT



i, m_0, m_1



$c = Enc(h, i, m_0, m_1)$



DB

$m_{DB_i} = Dec(DB, c)$

Learns nothing about m_{1-DB_i}

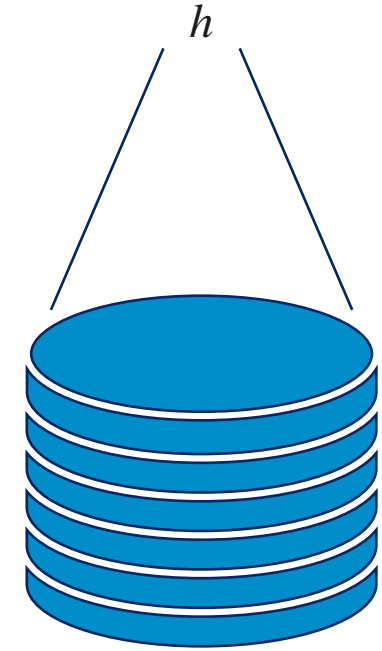
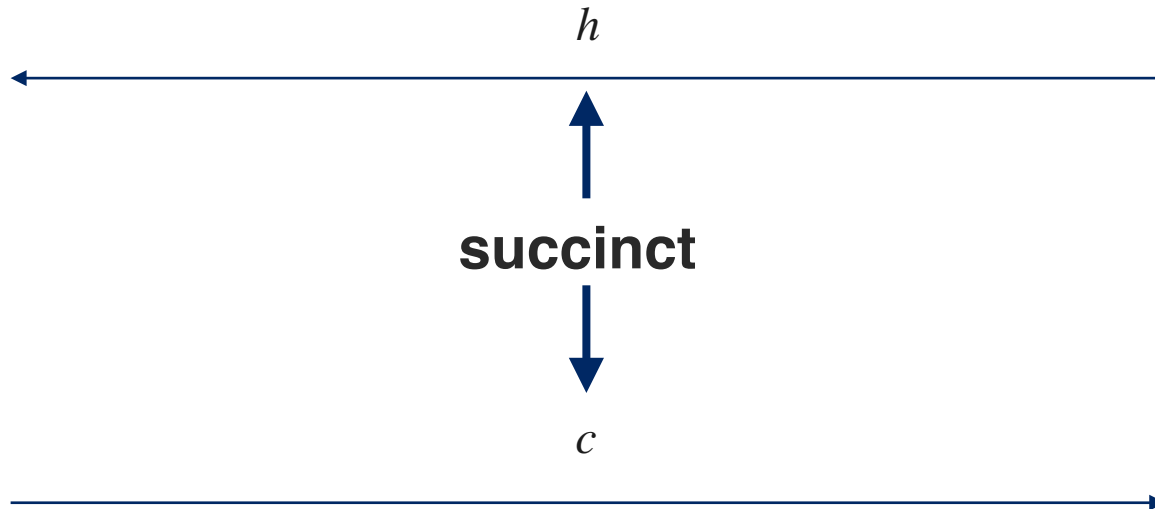


Laconic OT



i, m_0, m_1

$c = Enc(h, i, m_0, m_1)$



DB

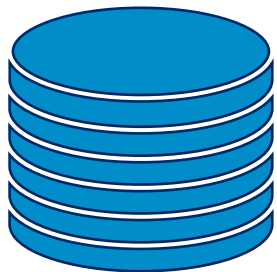
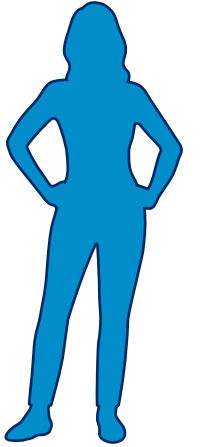
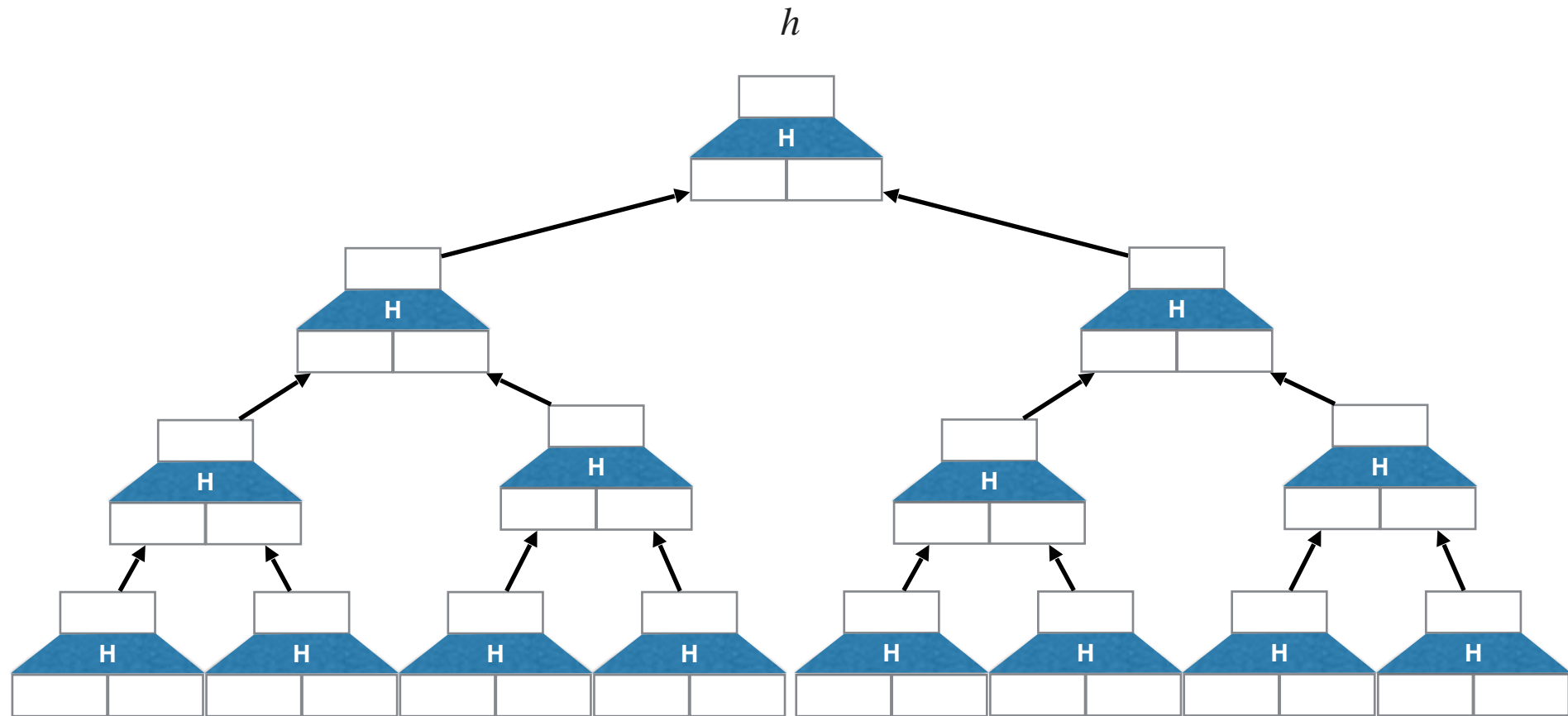
$m_{DB_i} = Dec(DB, c)$

Learns nothing about m_{1-DB_i}



Constructing Laconic OT [CDGGMP17]

Hashing: Merkle Trees

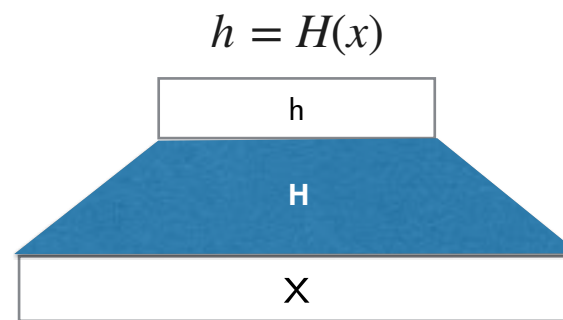


Building Block: Hash Encryption

$$h = H(x)$$

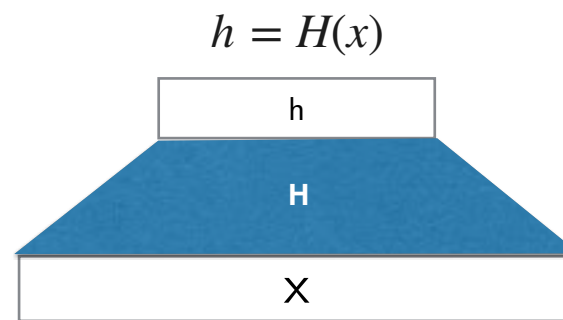


Building Block: Hash Encryption



Building Block: Hash Encryption

i, b, m



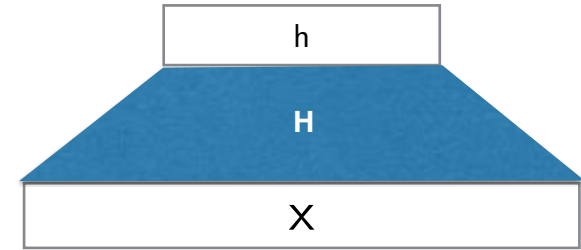
Building Block: Hash Encryption

i, b, m

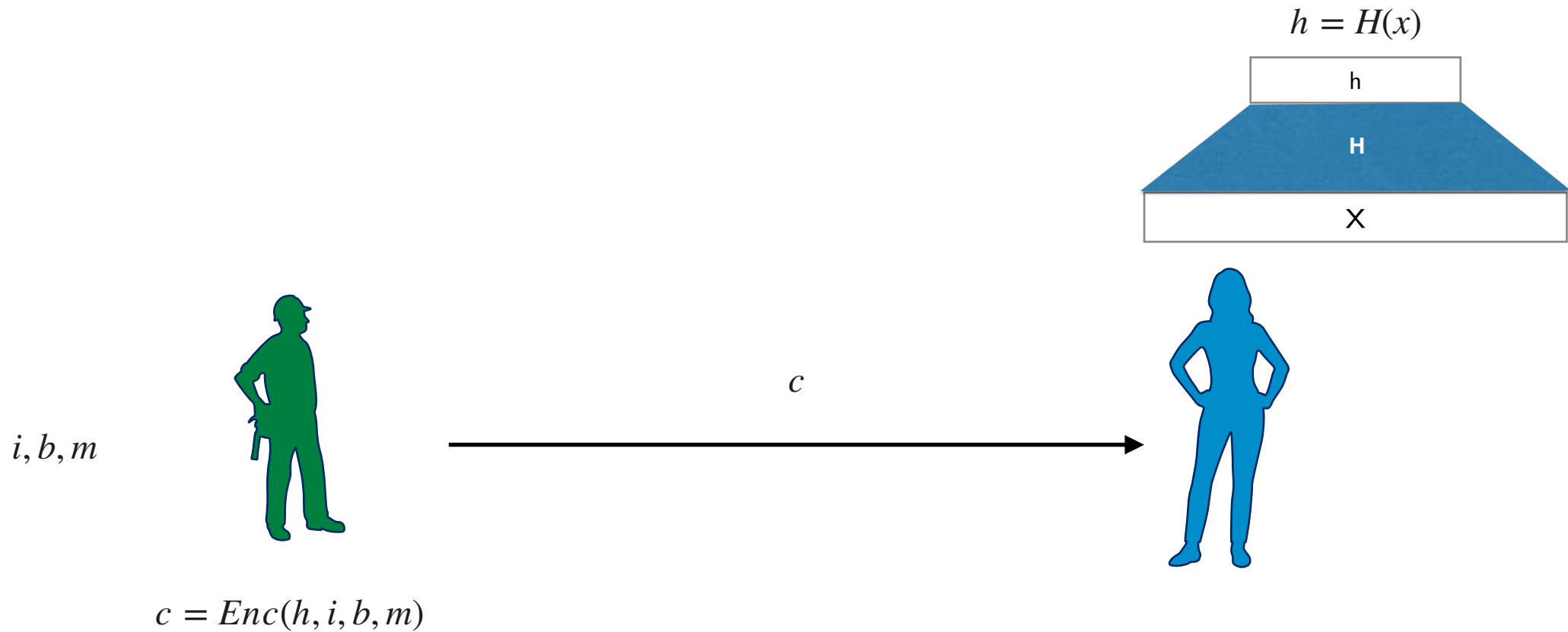


$$c = \text{Enc}(h, i, b, m)$$

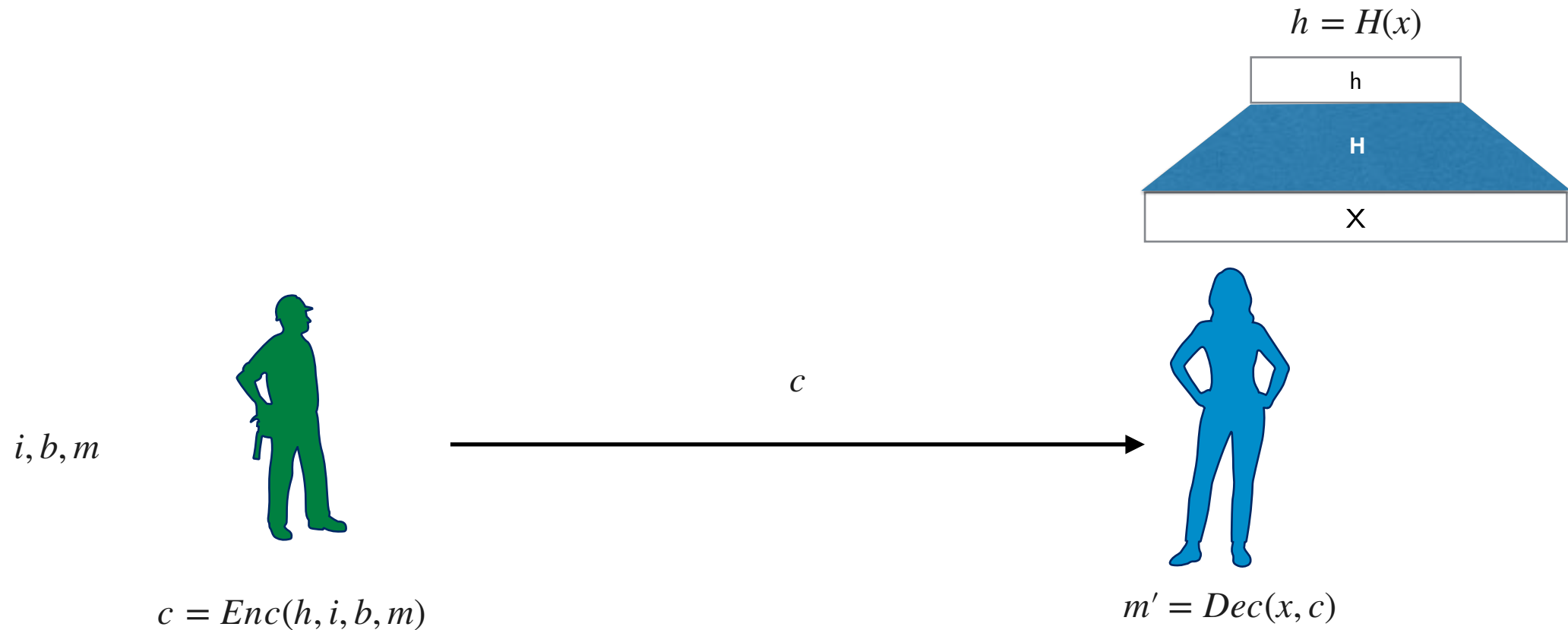
$$h = H(x)$$



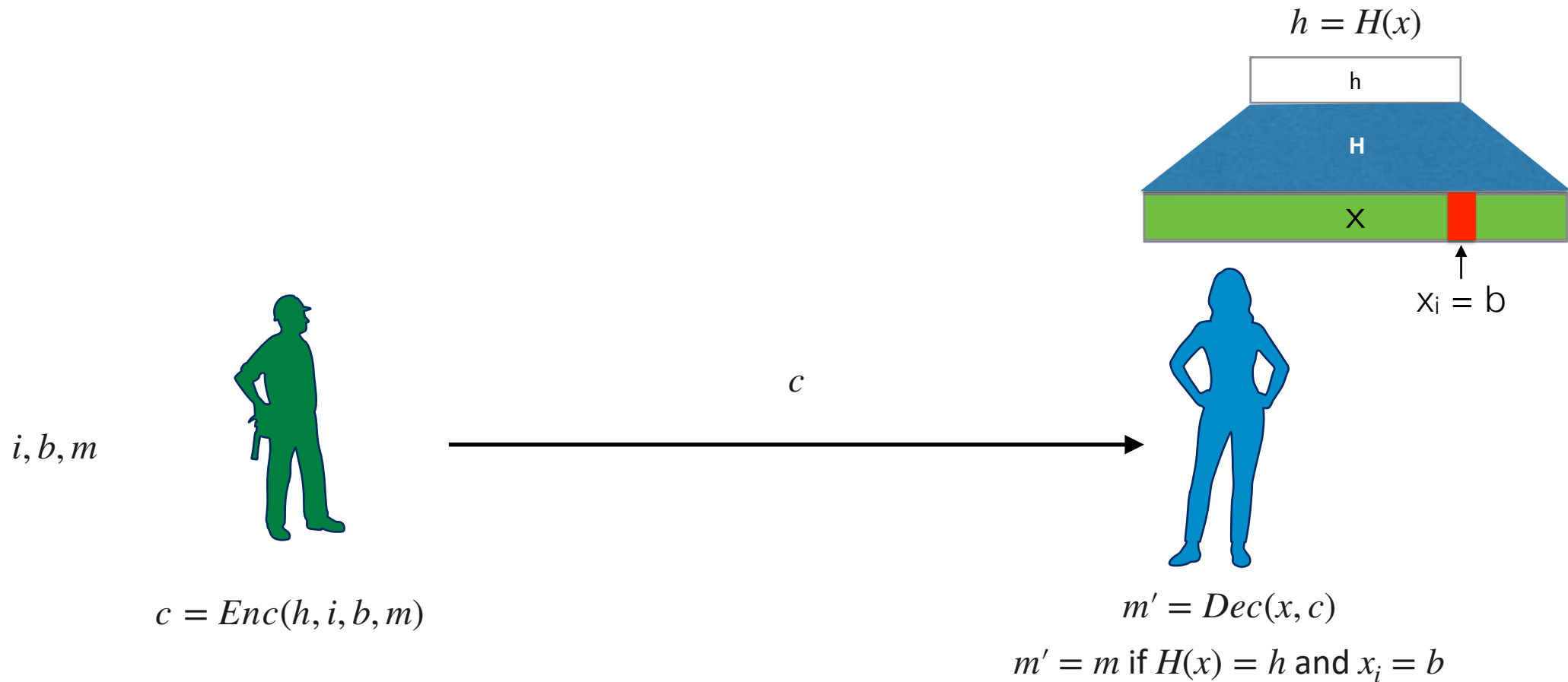
Building Block: Hash Encryption



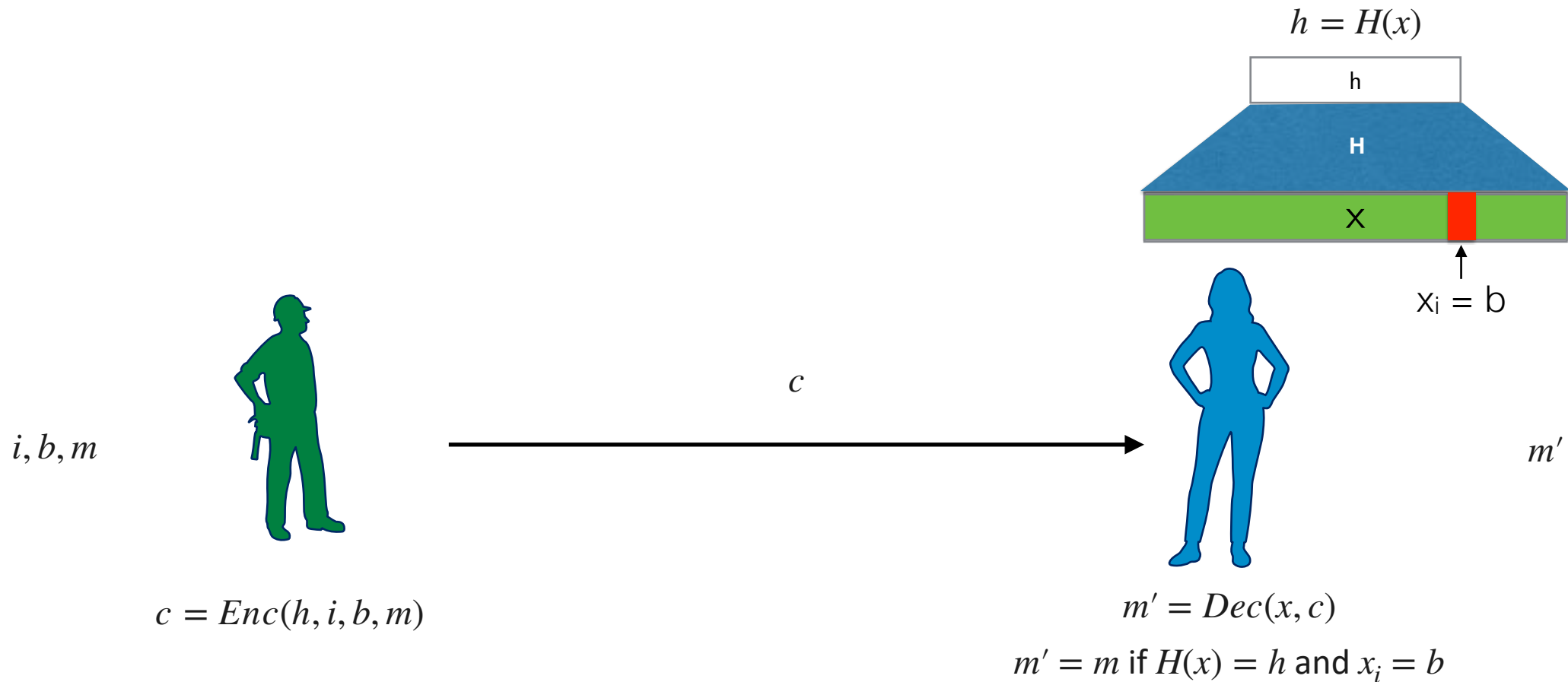
Building Block: Hash Encryption



Building Block: Hash Encryption



Building Block: Hash Encryption



Hash Encryption from DDH (CDH)

$$k = \left(g, g_{1,0} = g^{\alpha_{1,0}}, \dots, g_{i,0} = g^{\alpha_{i,0}}, \dots, g_{n,0} = g^{\alpha_{n,0}}, \right. \\ \left. g_{1,1} = g^{\alpha_{1,1}}, \dots, g_{i,1} = g^{\alpha_{i,1}}, \dots, g_{n,1} = g^{\alpha_{n,1}} \right)$$

$$H(k, x; r) \leftarrow g^r \cdot \prod_j g_{j,x_j} = h$$

$Enc(k, (h, i, b), m) :$

$$c_1 \leftarrow h^s$$

$$e \leftarrow g_{i,b}^s \cdot m$$

$$c_0 \leftarrow g^s$$

$$\forall j \neq i : c_{j,0} \leftarrow g_{j,0}^s$$

$$c_{j,1} \leftarrow g_{j,1}^s$$

$Dec(k, (x, r), c) :$

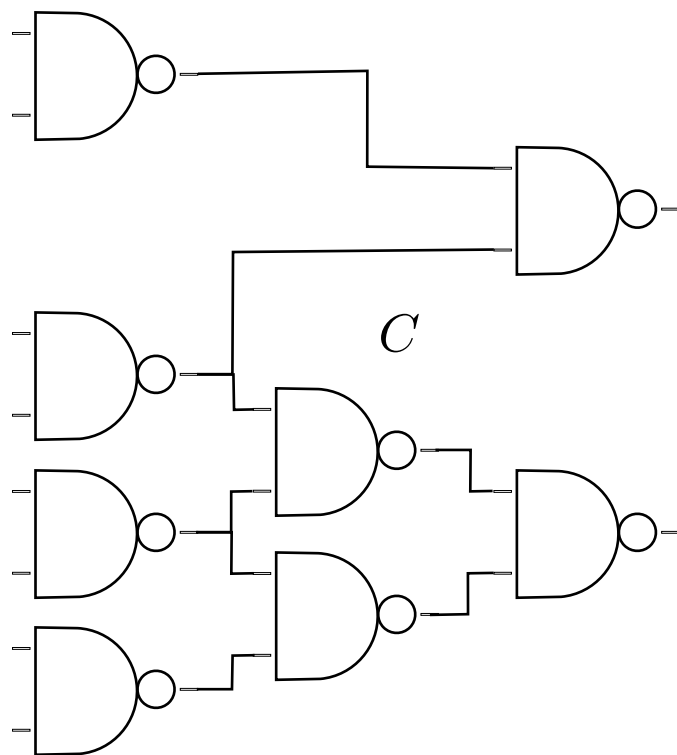
$$m \leftarrow e \cdot \frac{c_0^r \cdot \prod_{j \neq i} c_{j,x_j}}{c_1}$$

$$= e \cdot \frac{c_0^r \cdot \prod_{j \neq i} c_{j,x_j}}{h^s}$$

$$= e \cdot \frac{c_0^r \cdot \prod_{j \neq i} c_{j,x_j}}{g_{i,x_i}^s \cdot c_0^r \cdot \prod_{j \neq i} c_{j,x_j}}$$

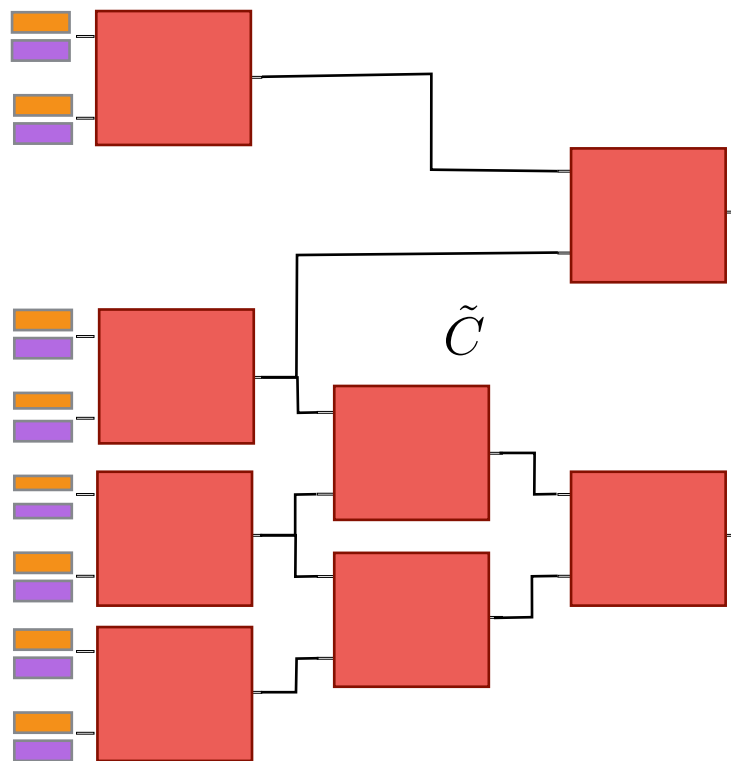
$$= m \cdot \frac{g_{i,b}^s}{g_{i,x_i}^s} = m$$

Building Block: Garbled Circuits

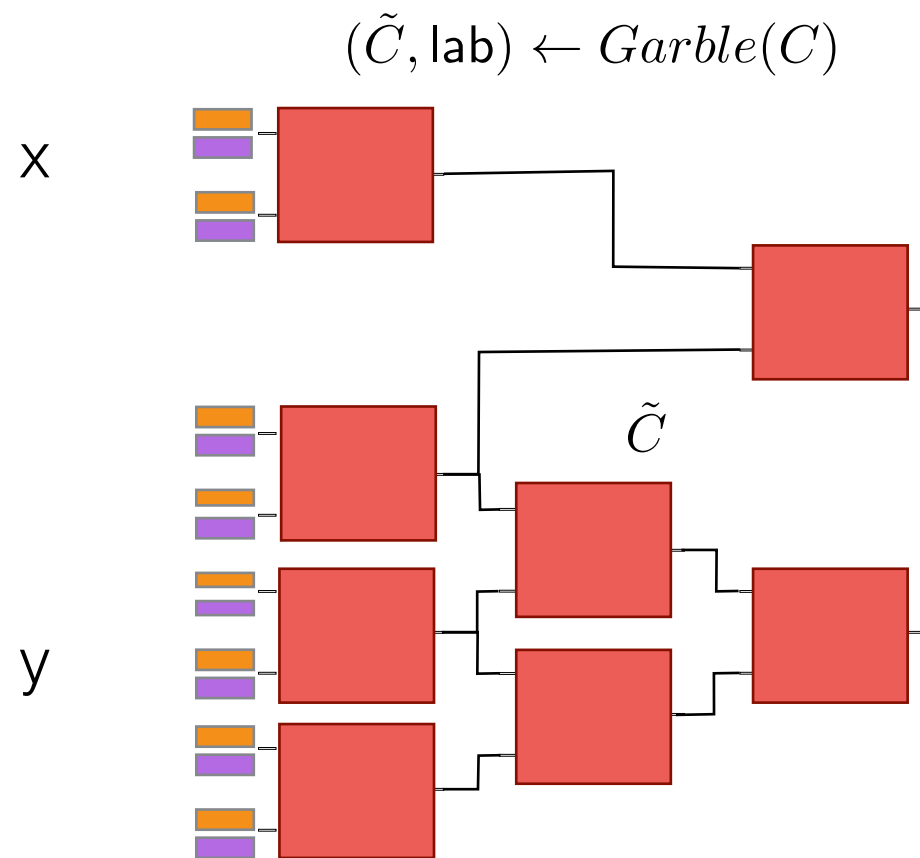


Building Block: Garbled Circuits

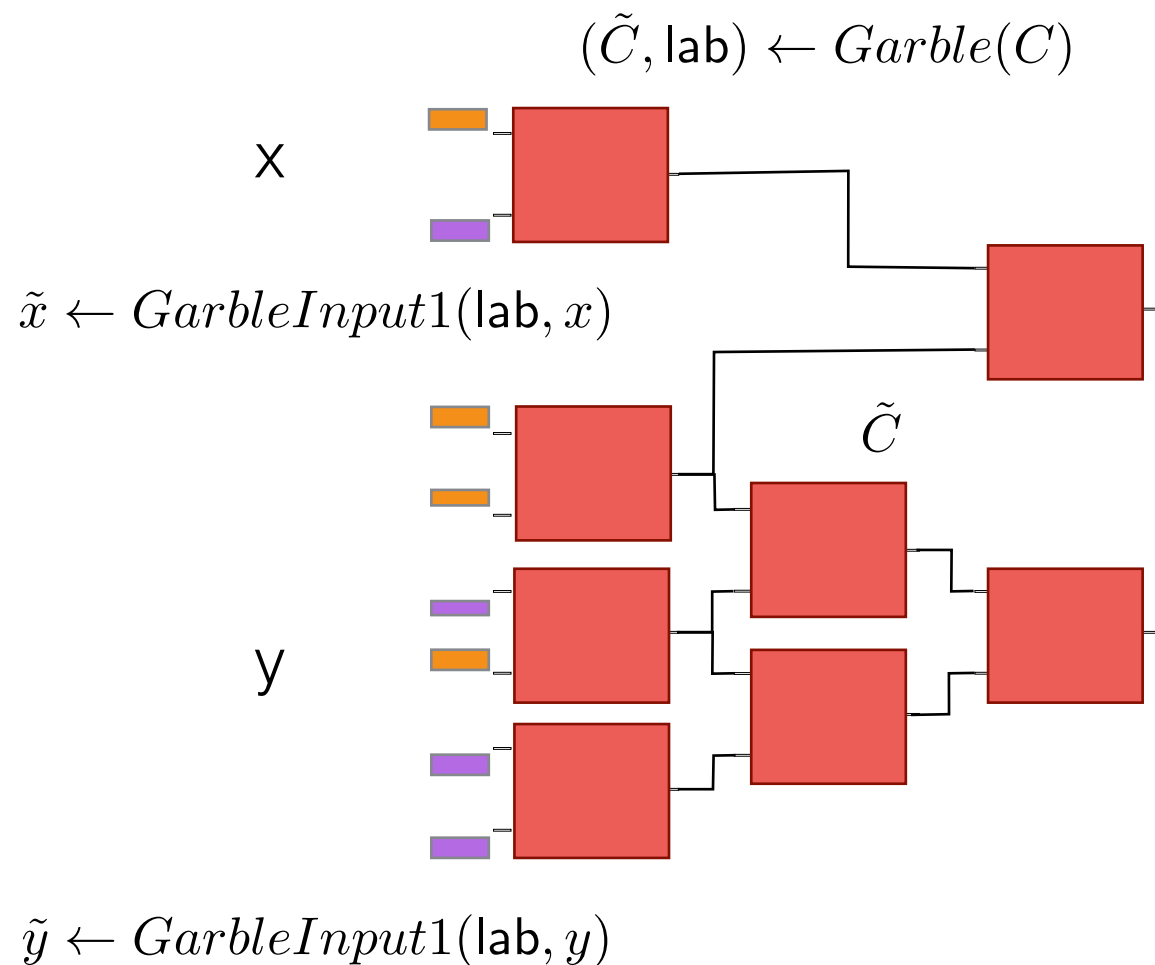
$$(\tilde{C}, \text{lab}) \leftarrow \text{Garble}(C)$$



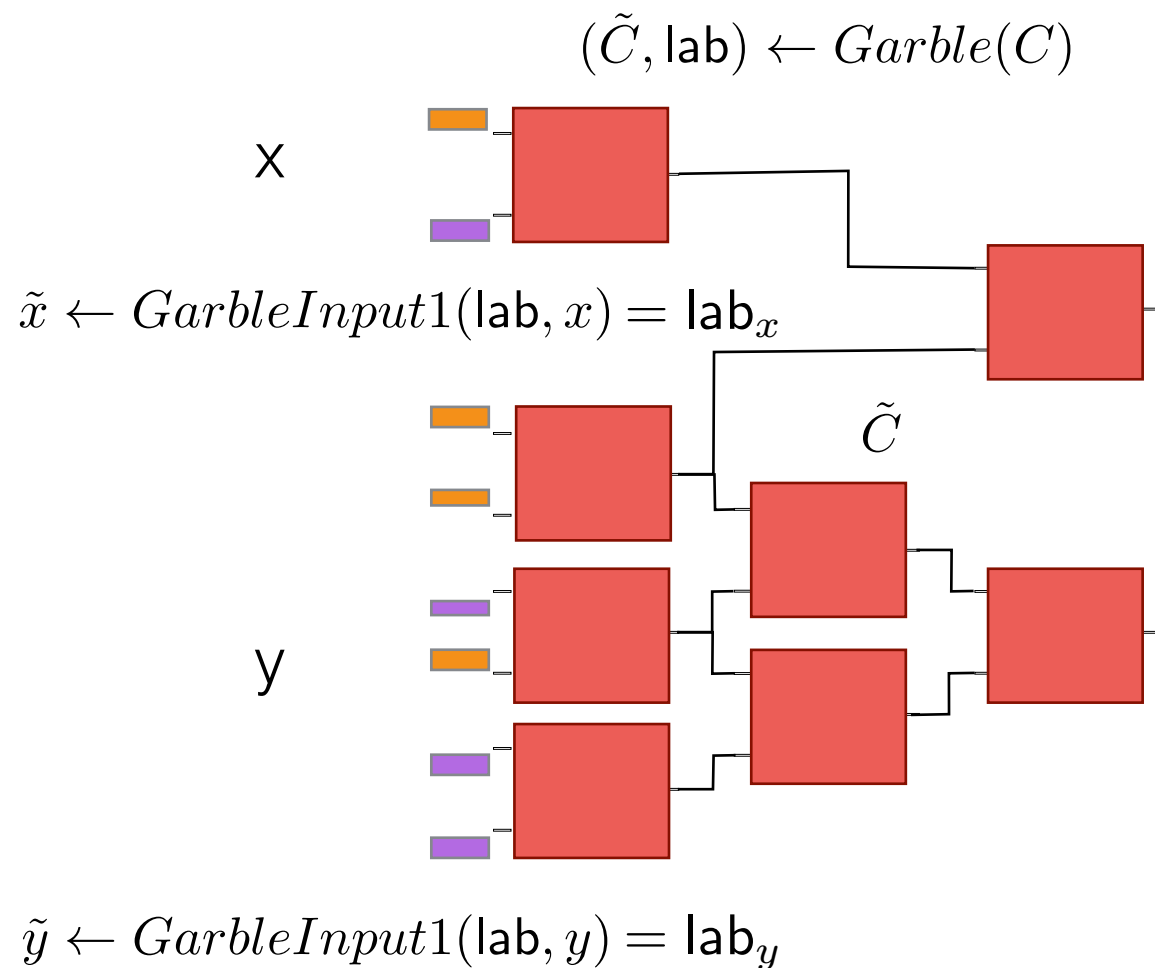
Building Block: Garbled Circuits



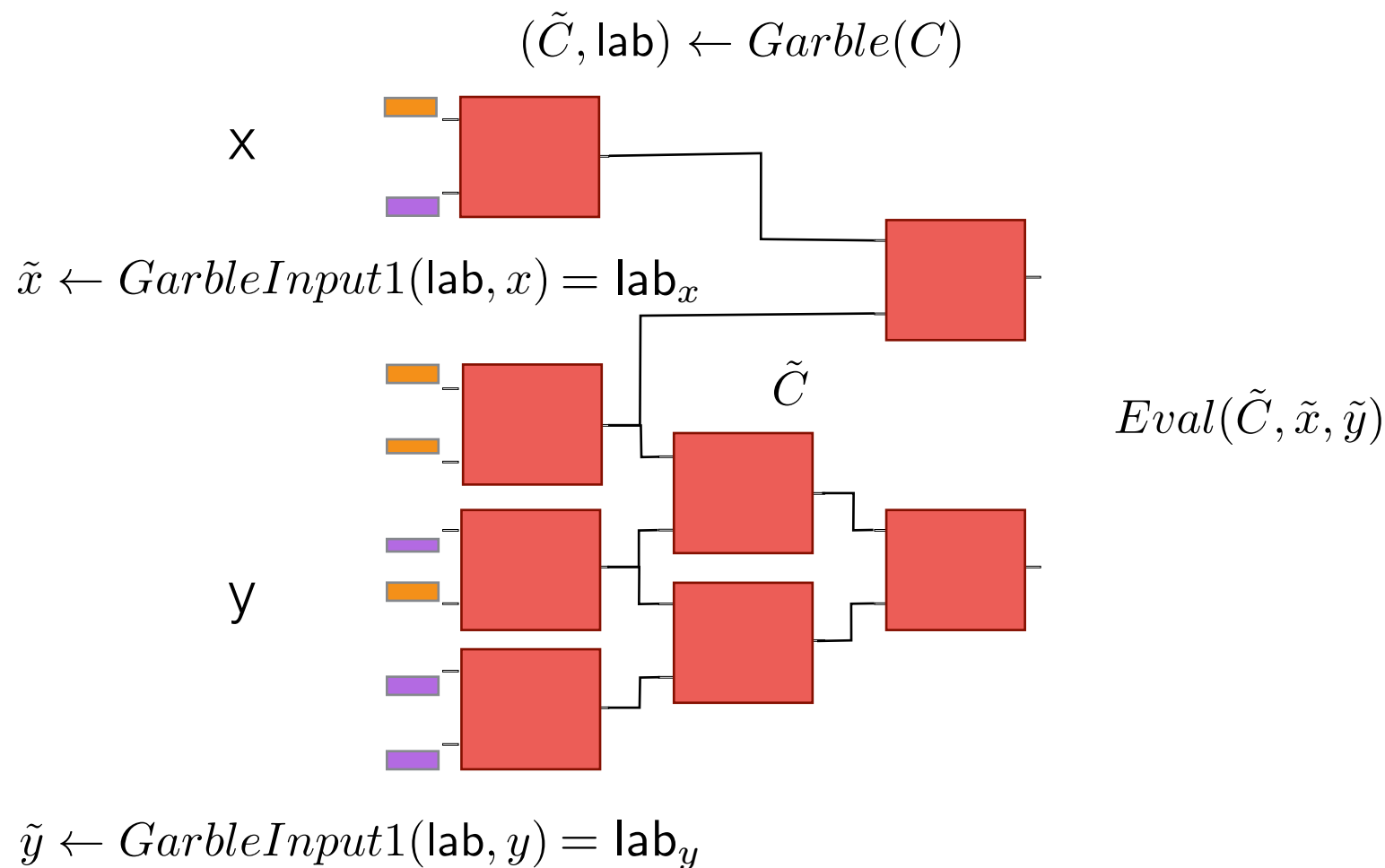
Building Block: Garbled Circuits



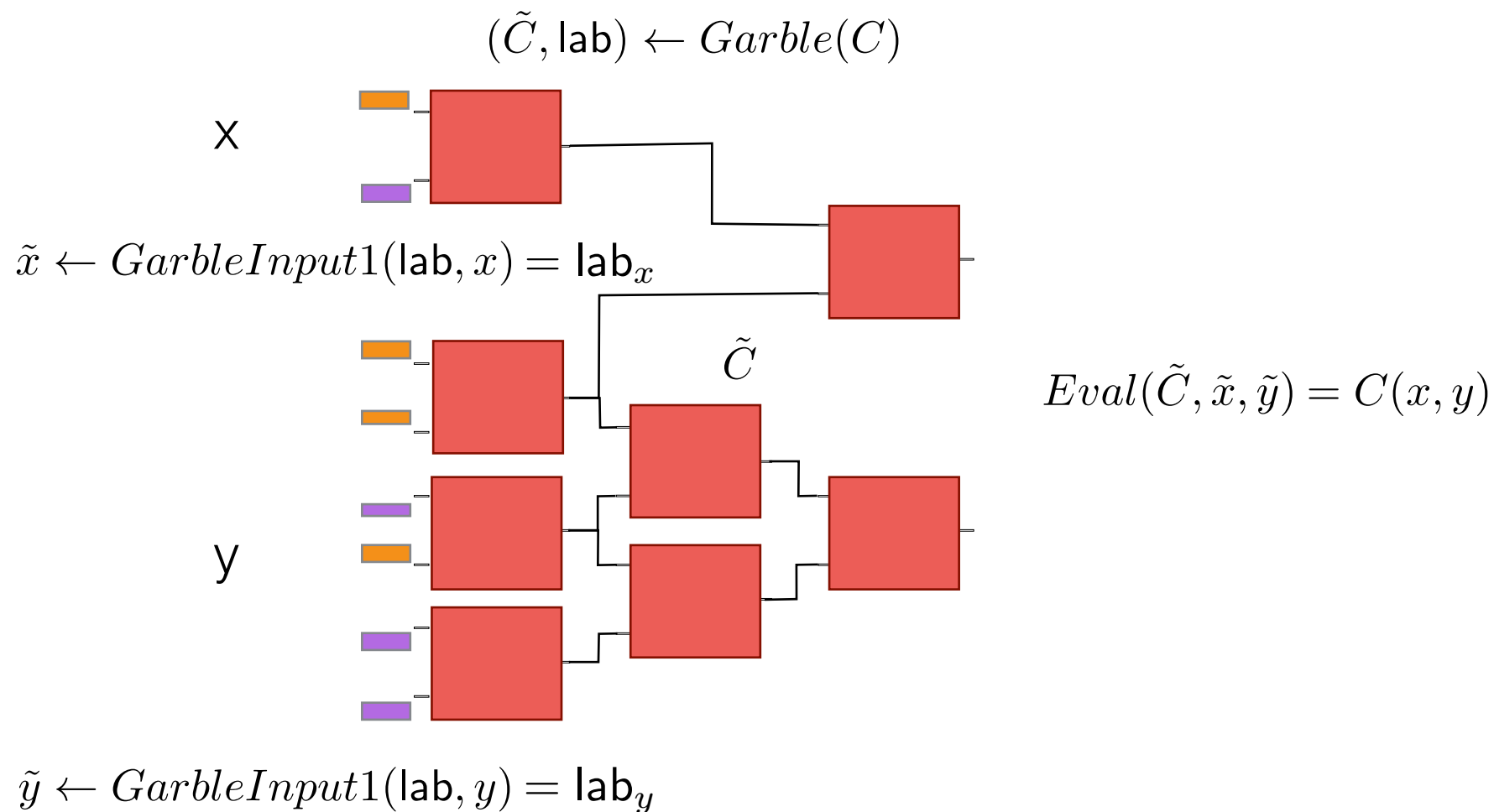
Building Block: Garbled Circuits



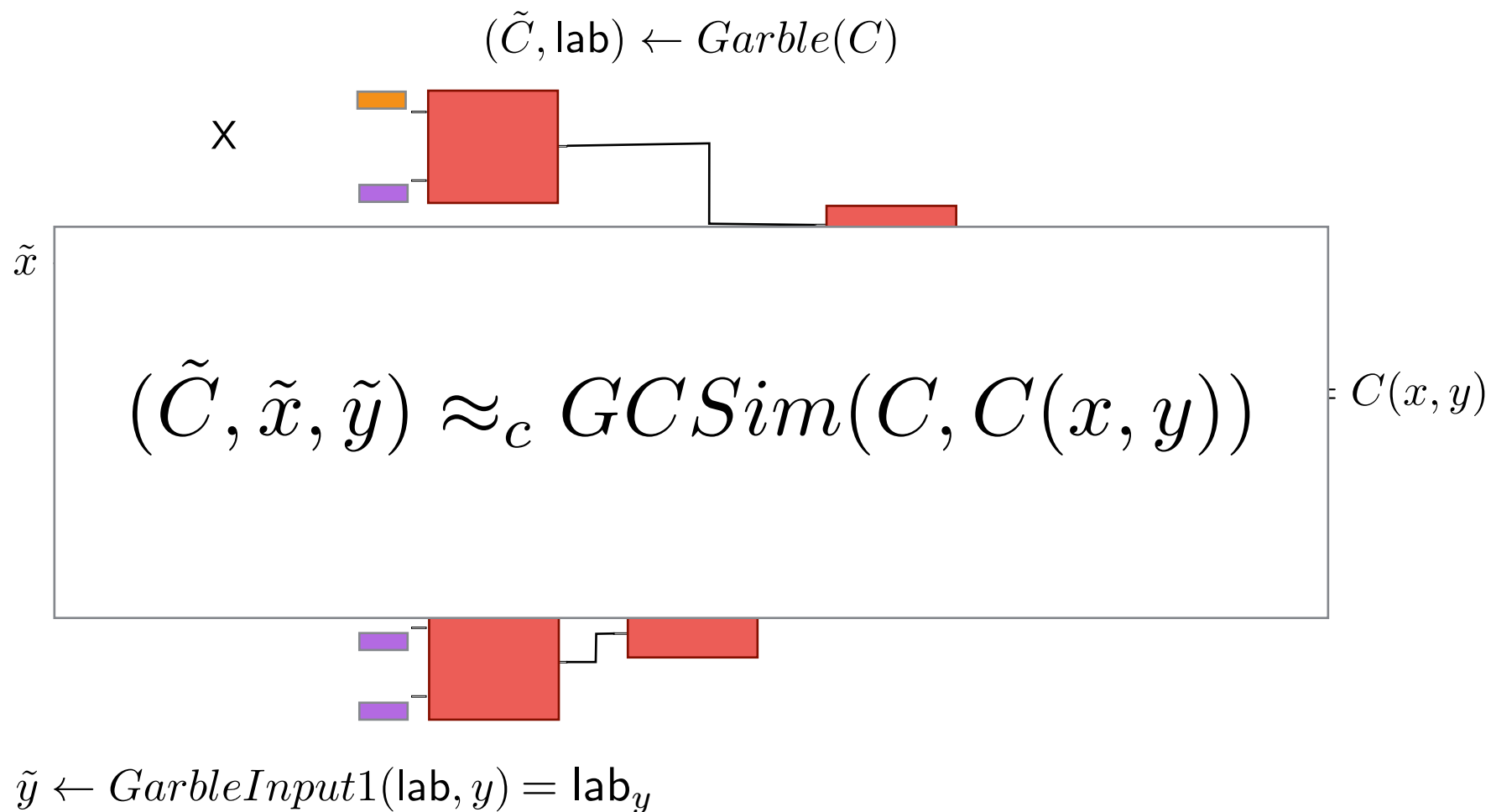
Building Block: Garbled Circuits



Building Block: Garbled Circuits



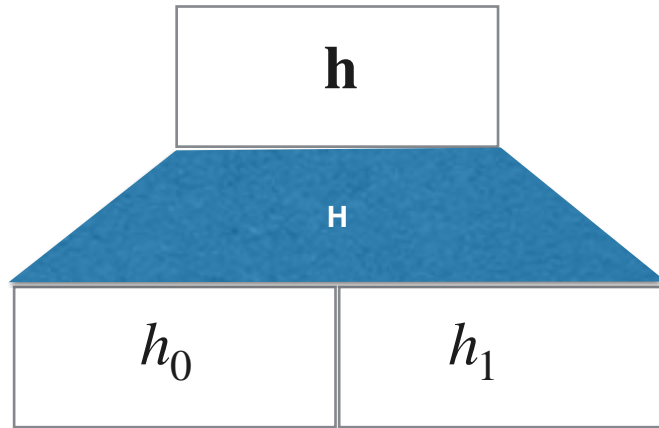
Building Block: Garbled Circuits



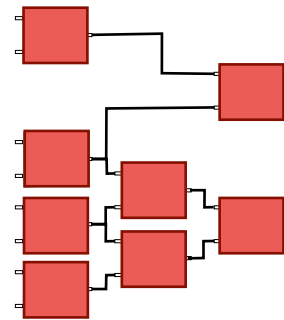


Bootstrapping/Recryption

$$c = \text{Enc}(h, lab)$$



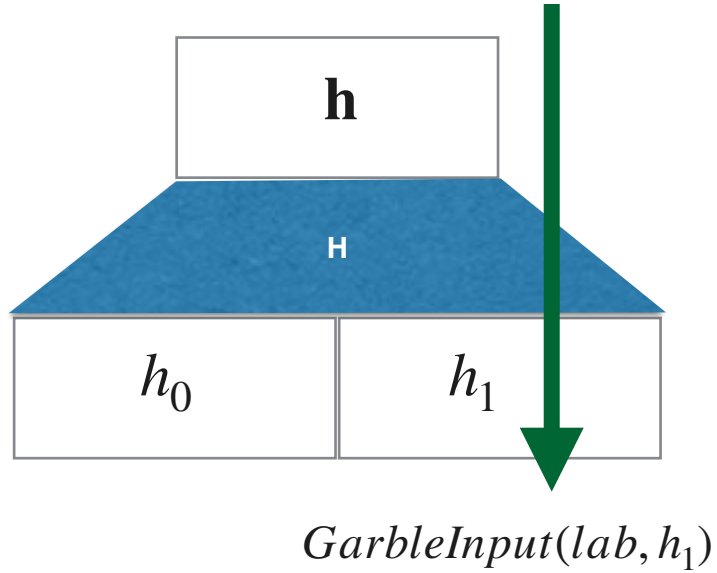
GC



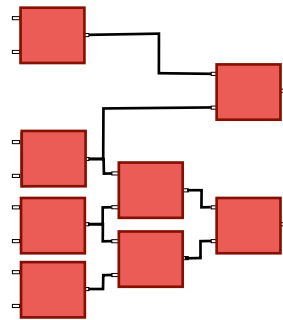


Bootstrapping/Recryption

$$c = \text{Enc}(h, lab)$$



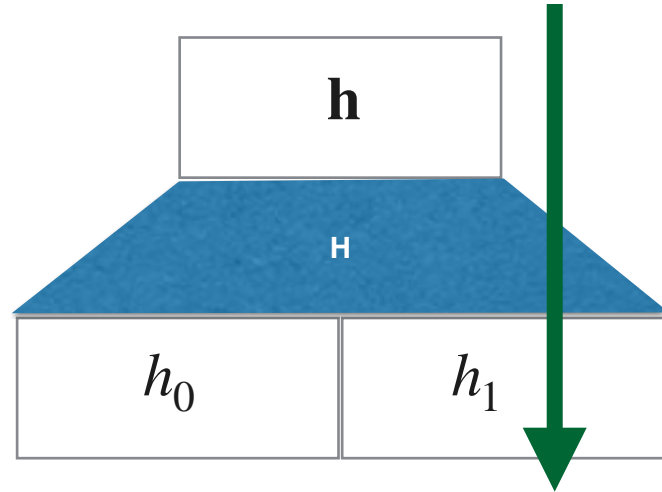
GC





Bootstrapping/Recryption

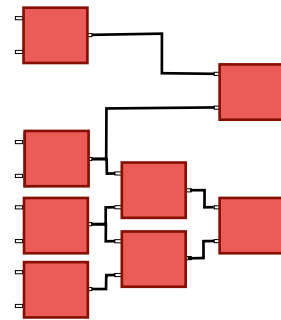
$$c = \text{Enc}(h, lab)$$



$\text{GarbleInput}(lab, h_1)$

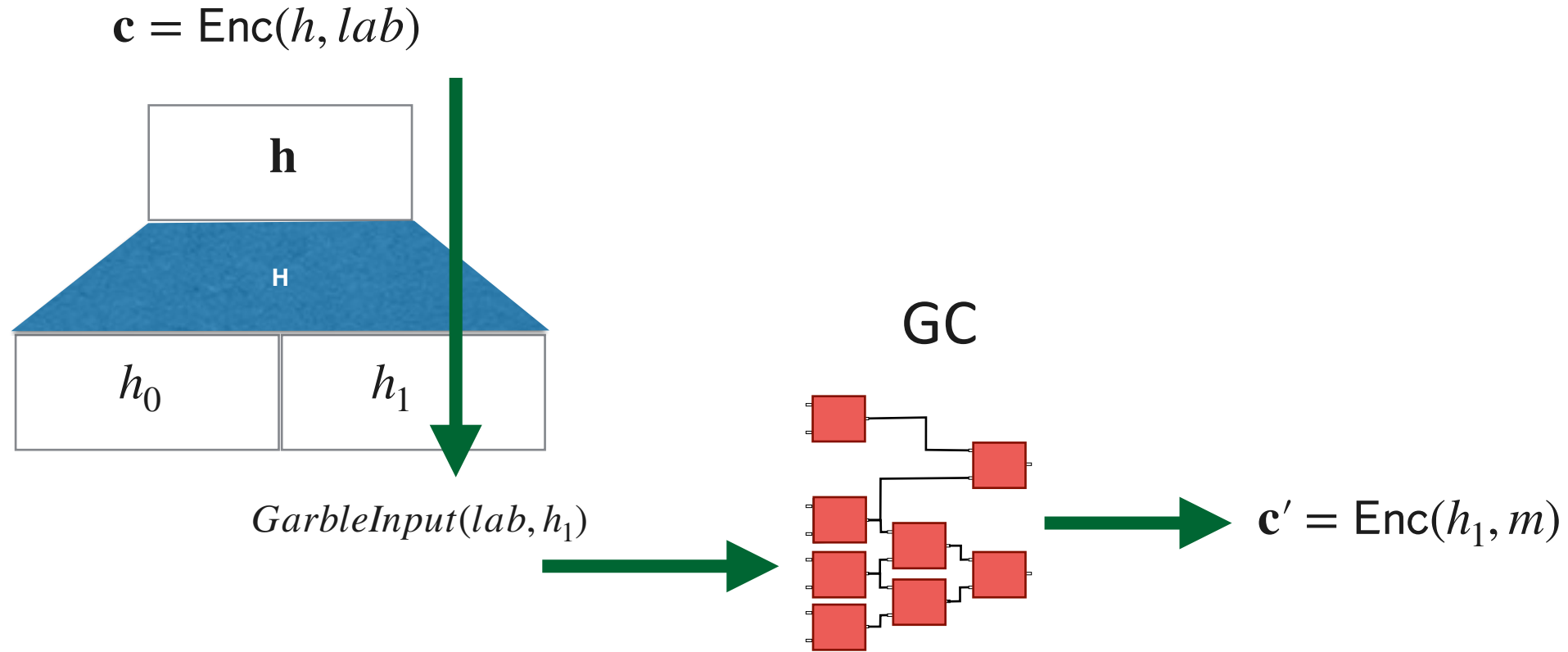


GC





Bootstrapping/Recryption

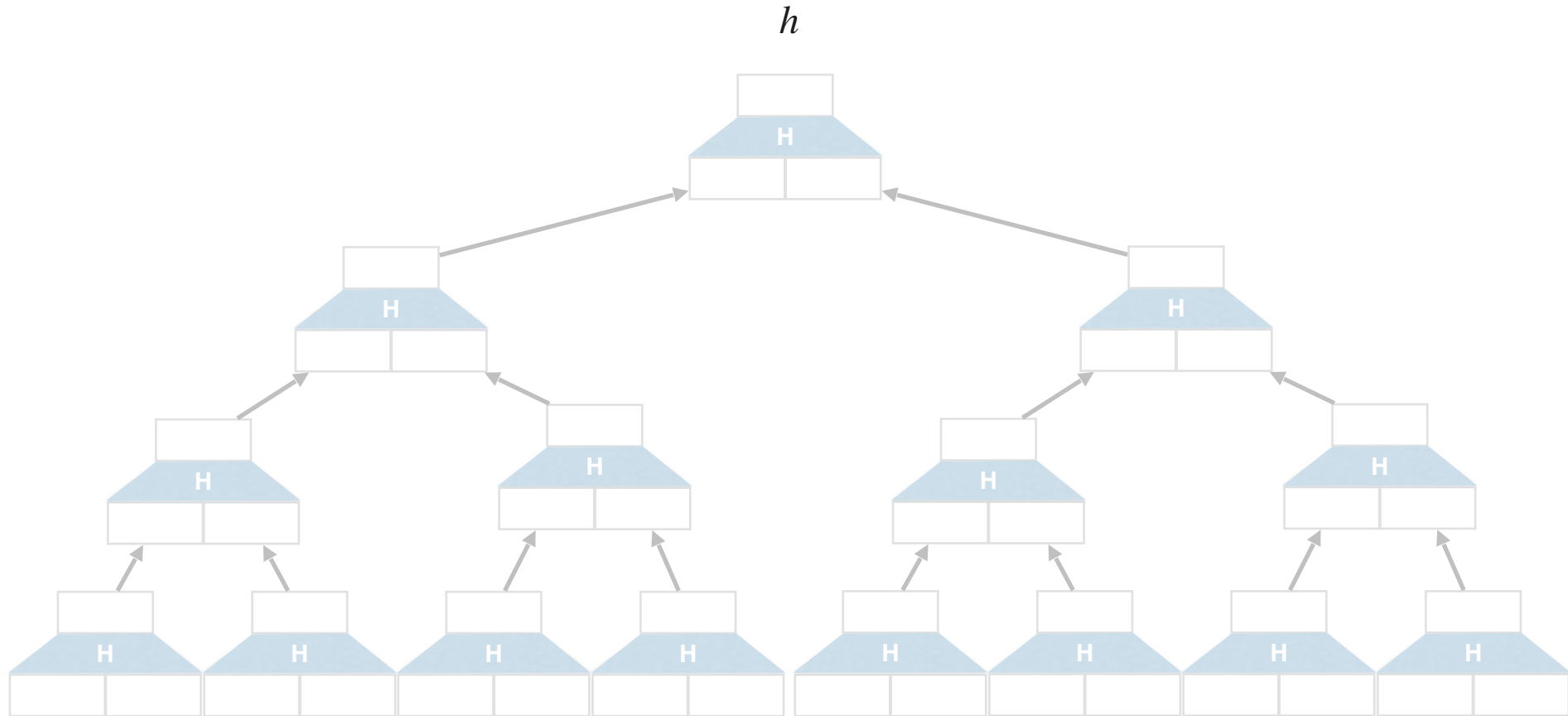




Laconic OT: Encryption



i m_0, m_1

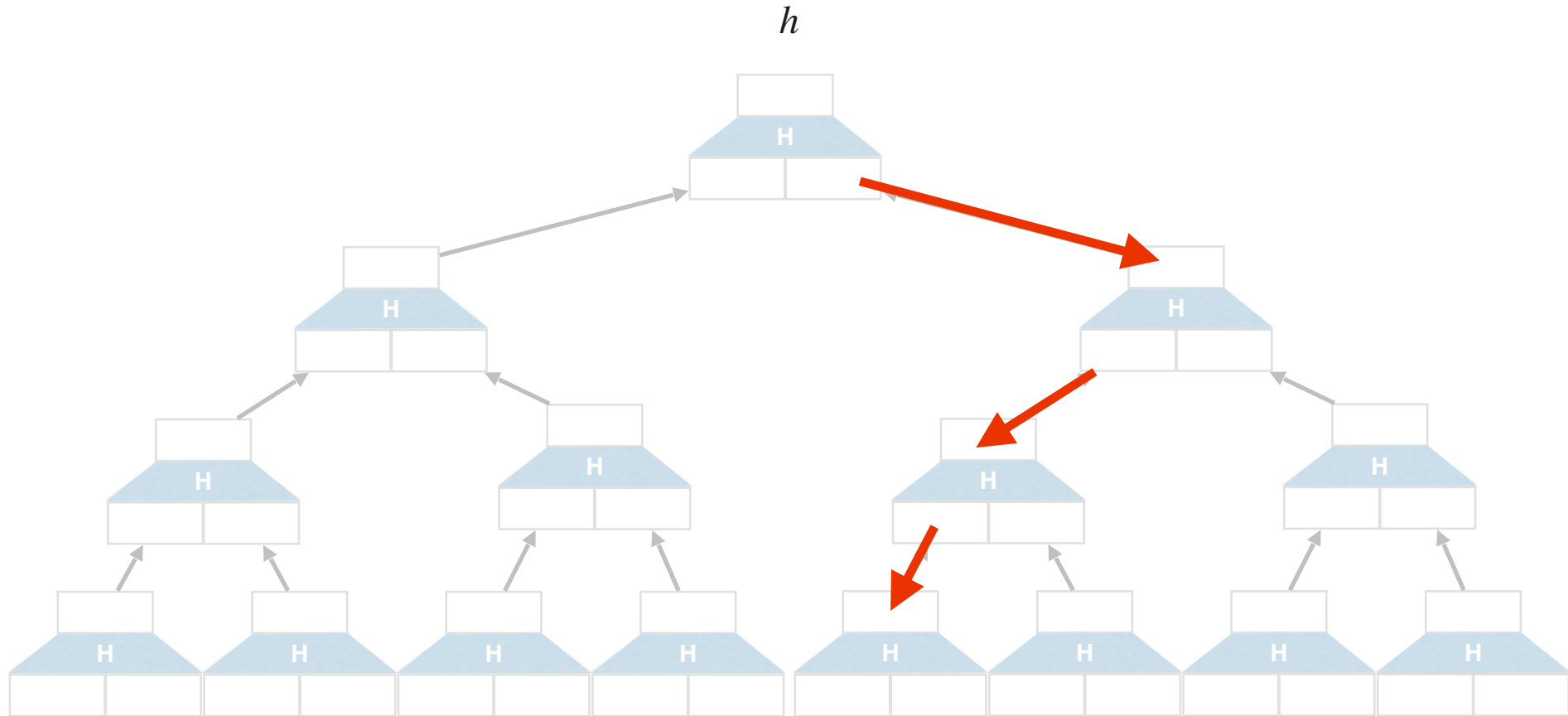




Laconic OT: Encryption



i m_0, m_1

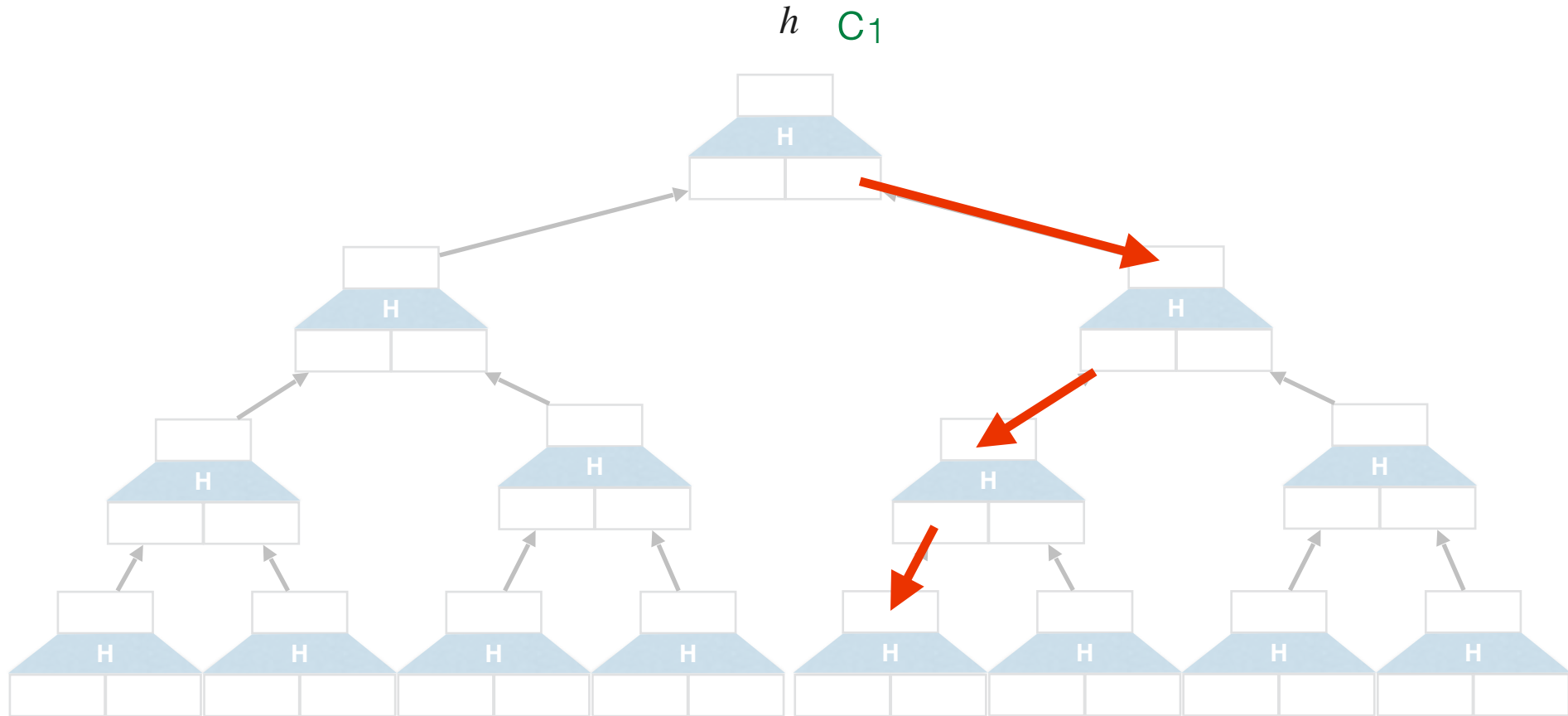




Laconic OT: Encryption



i m_0, m_1

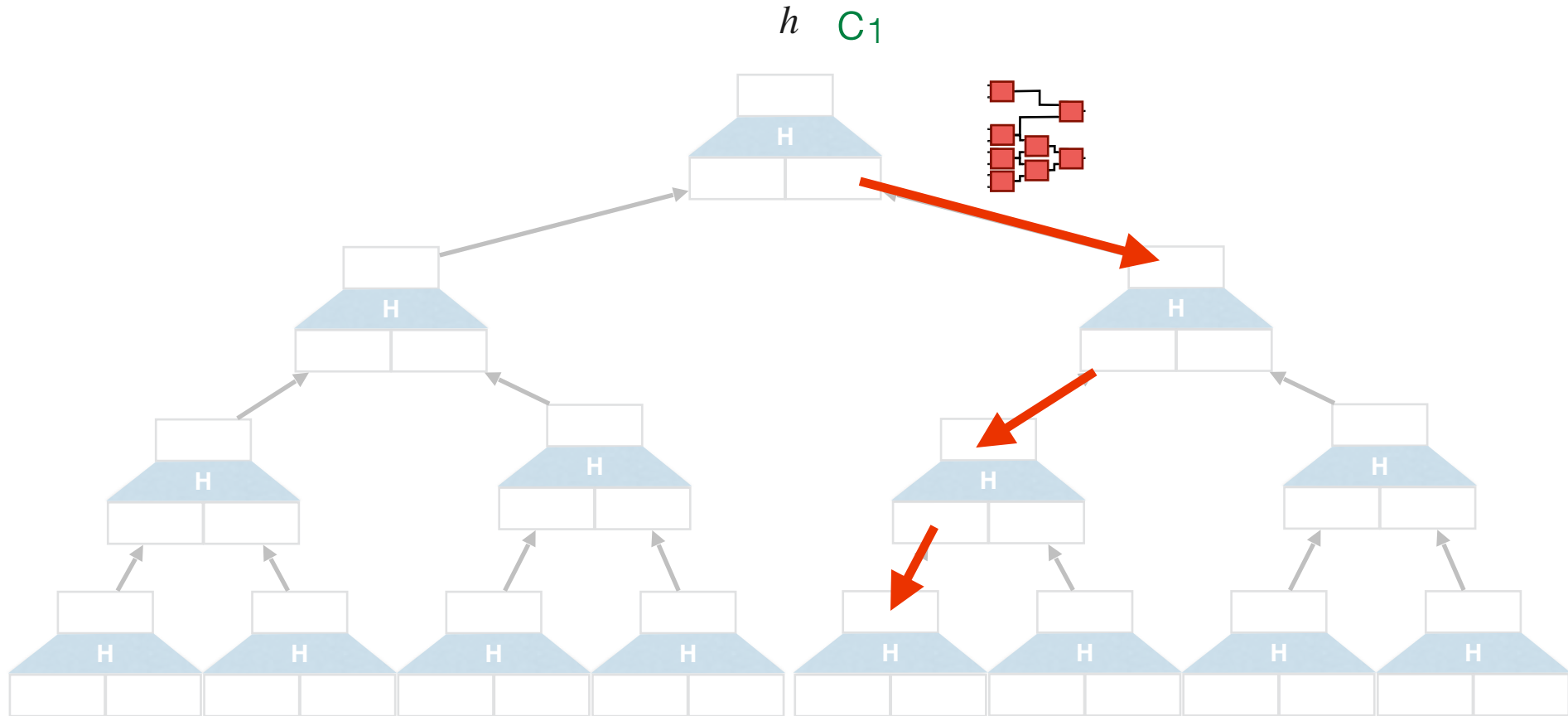




Laconic OT: Encryption



i m_0, m_1

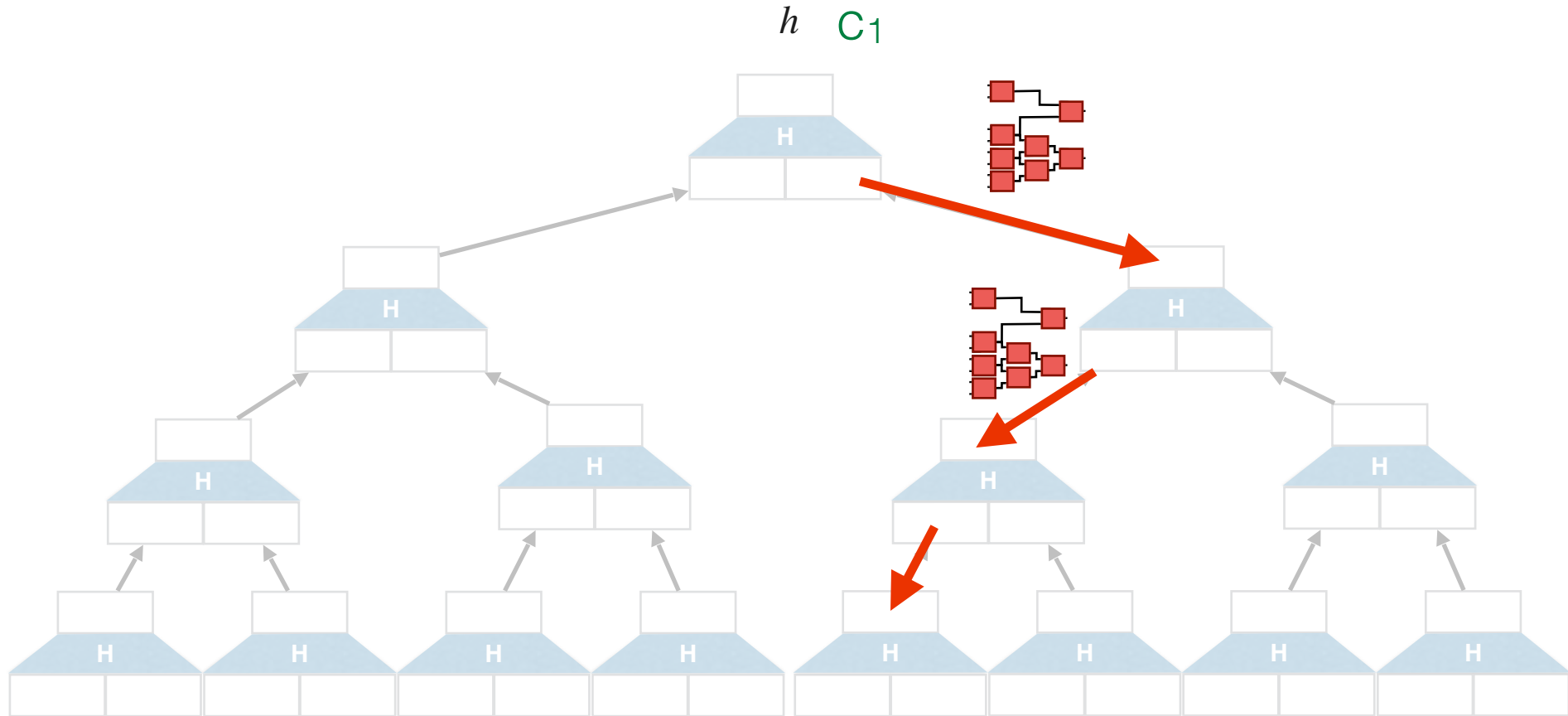




Laconic OT: Encryption



i m_0, m_1

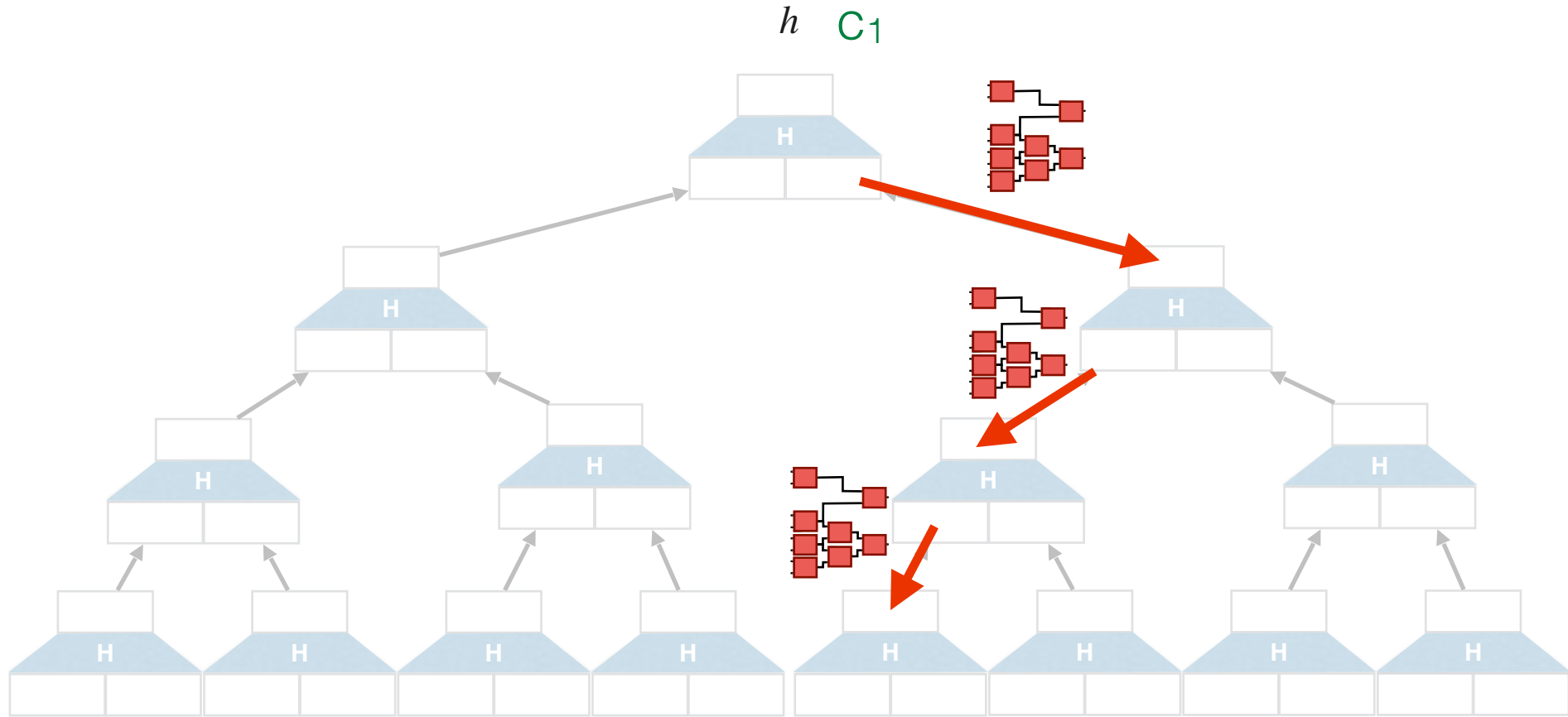




Laconic OT: Encryption



i m_0, m_1

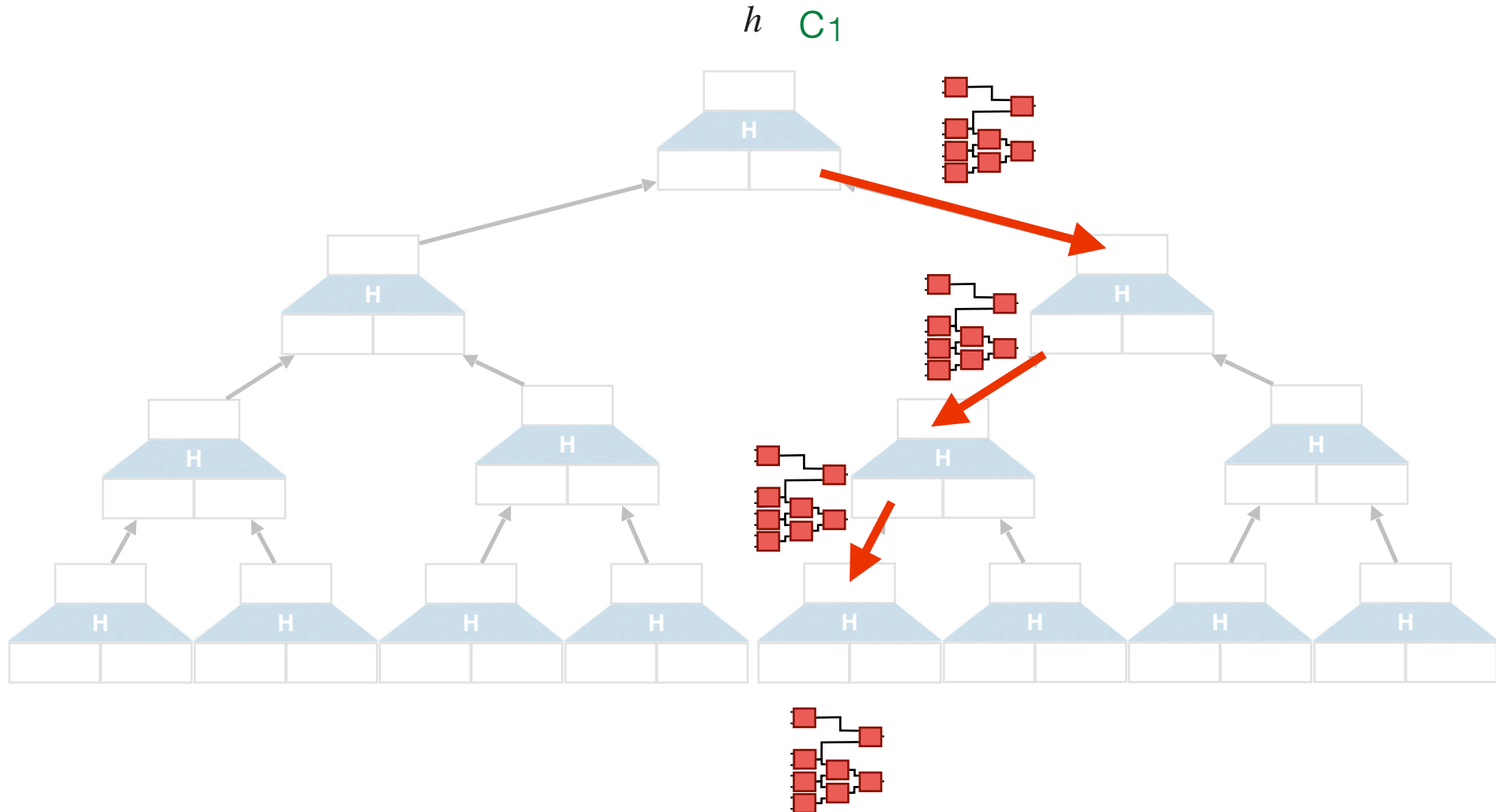




Laconic OT: Encryption



i m_0, m_1

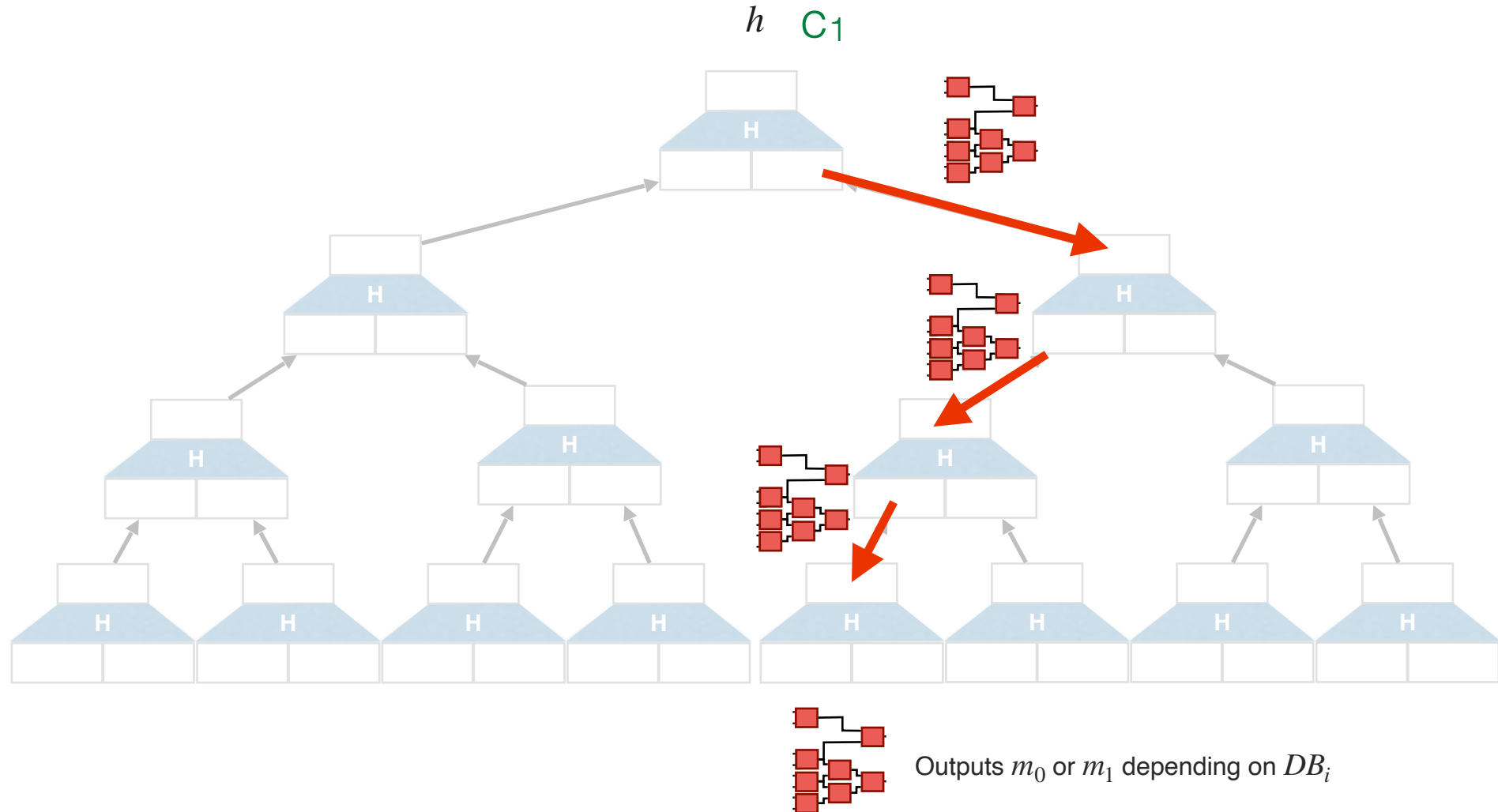




Laconic OT: Encryption



i m_0, m_1



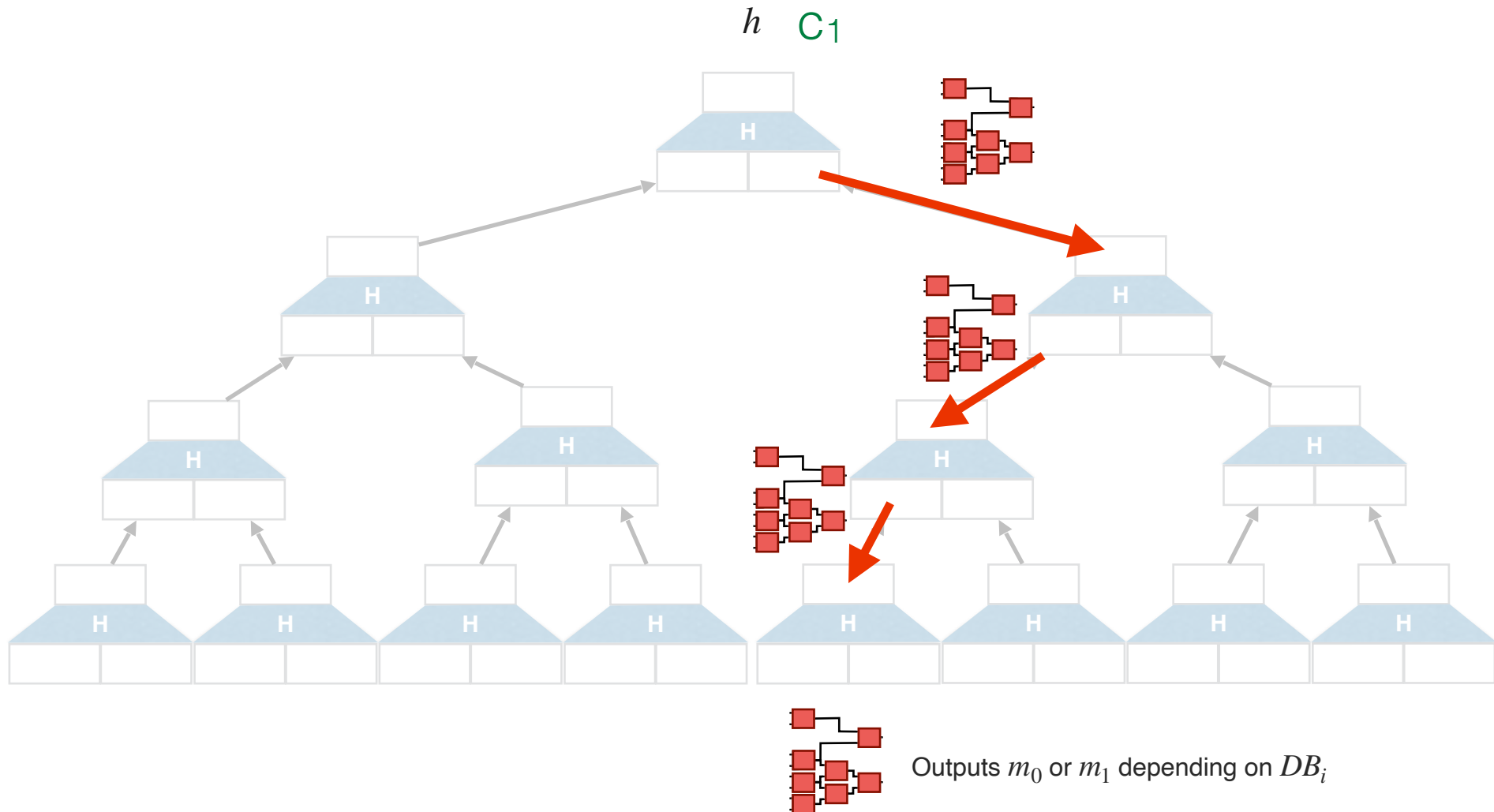


Laconic OT: Encryption

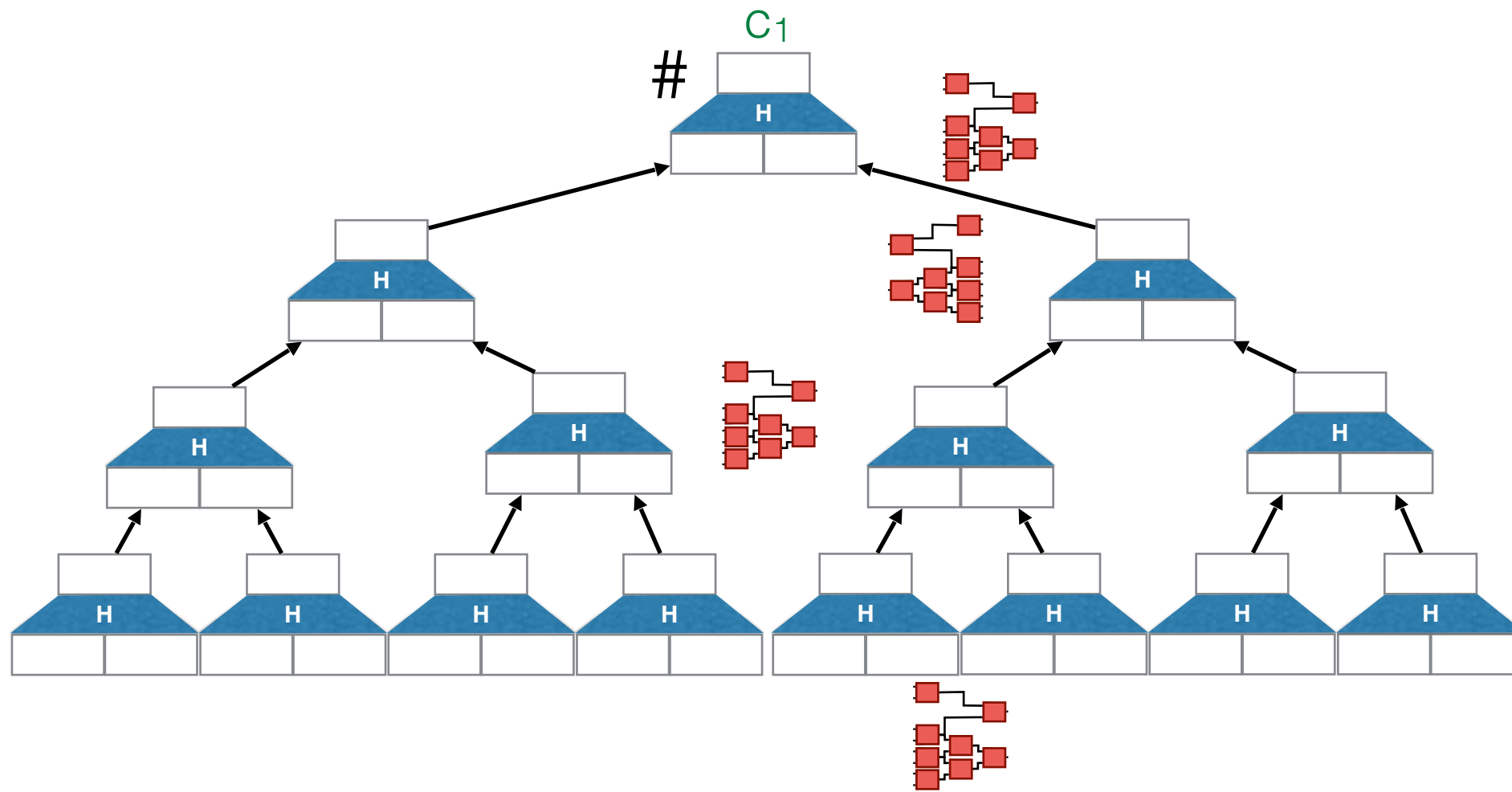
Core Paradigm: Delegate Work “into the Future”



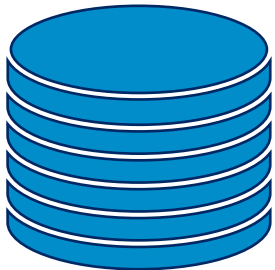
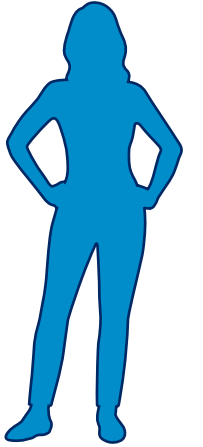
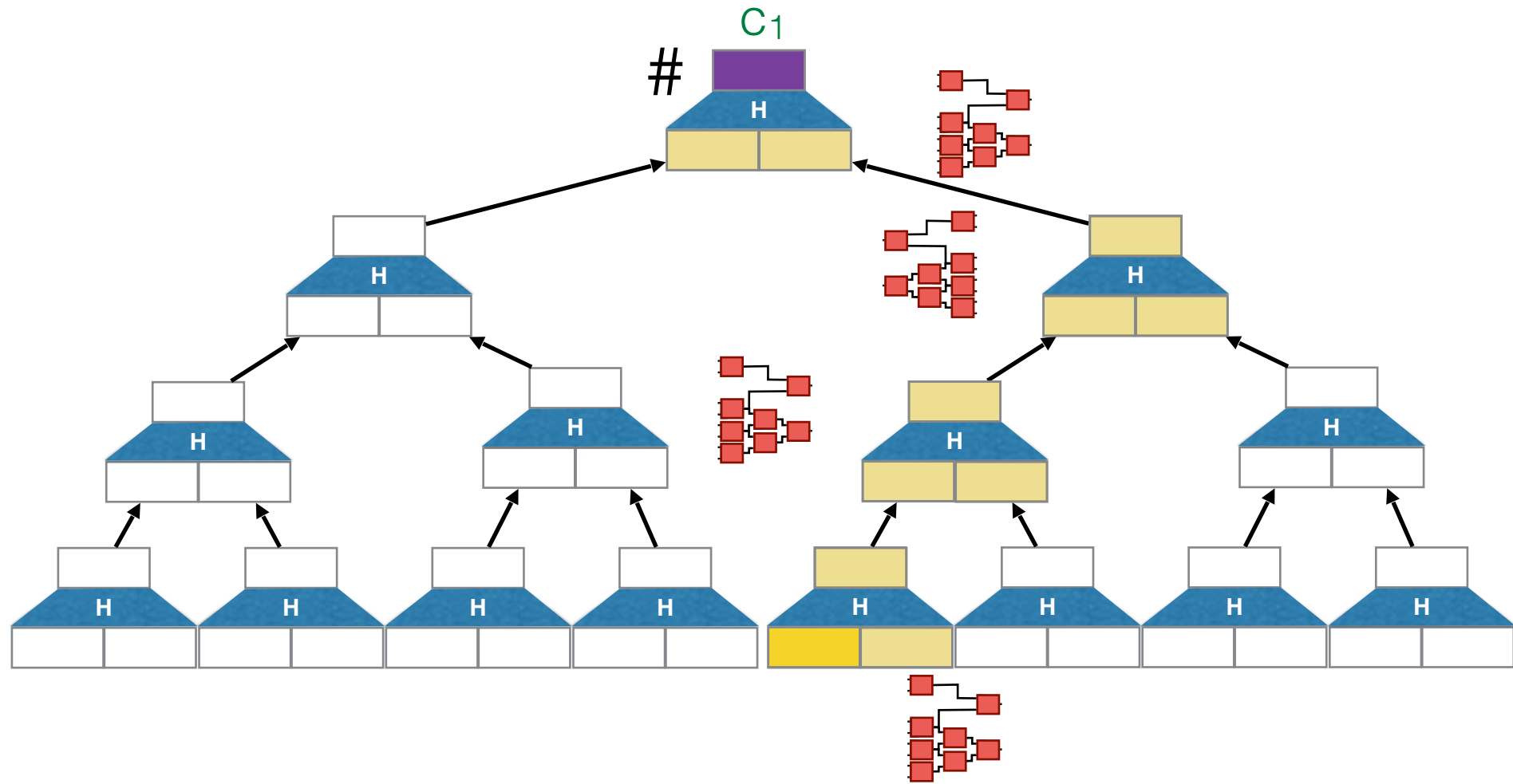
i m_0, m_1



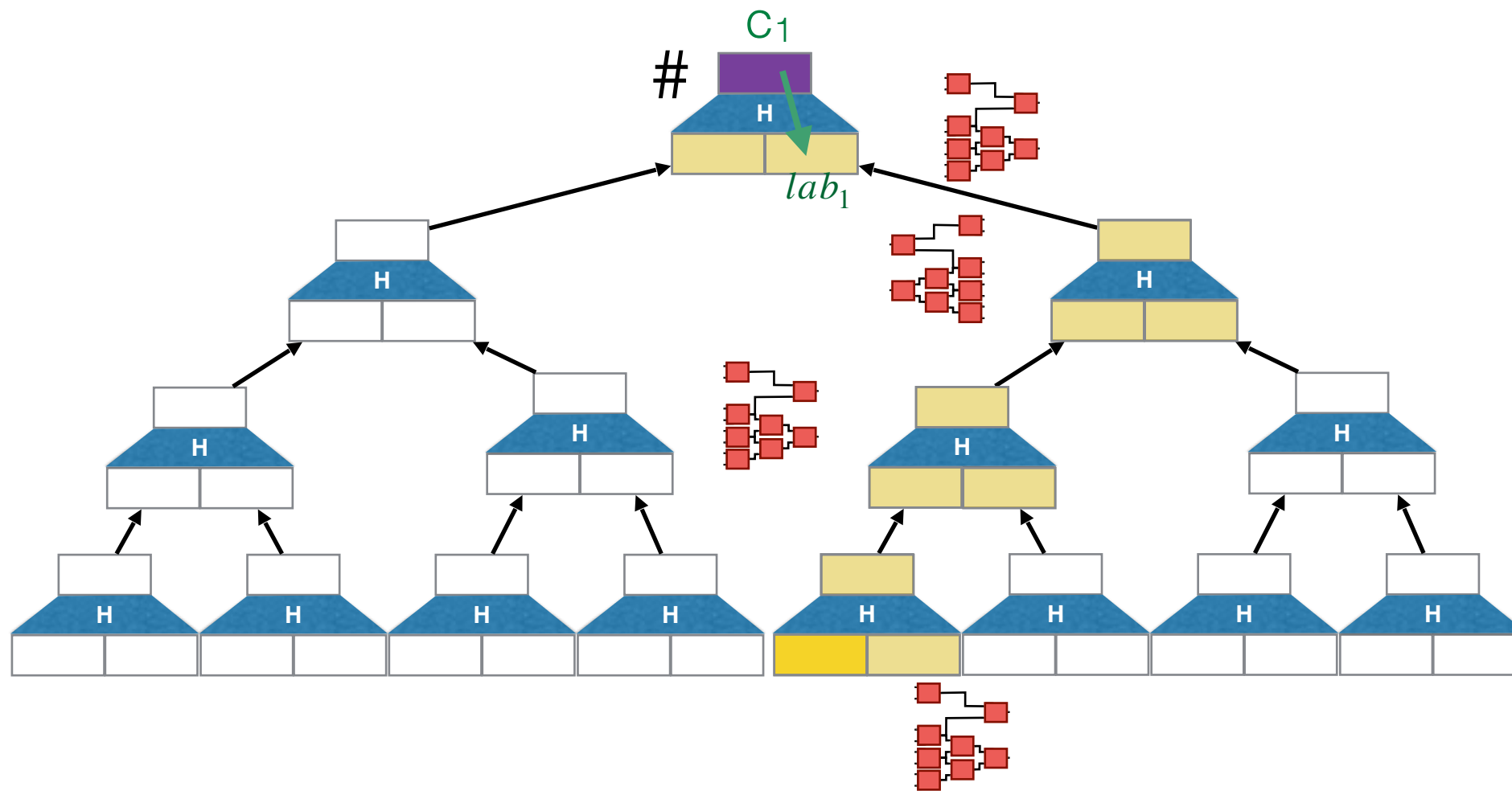
Laconic OT: Decryption



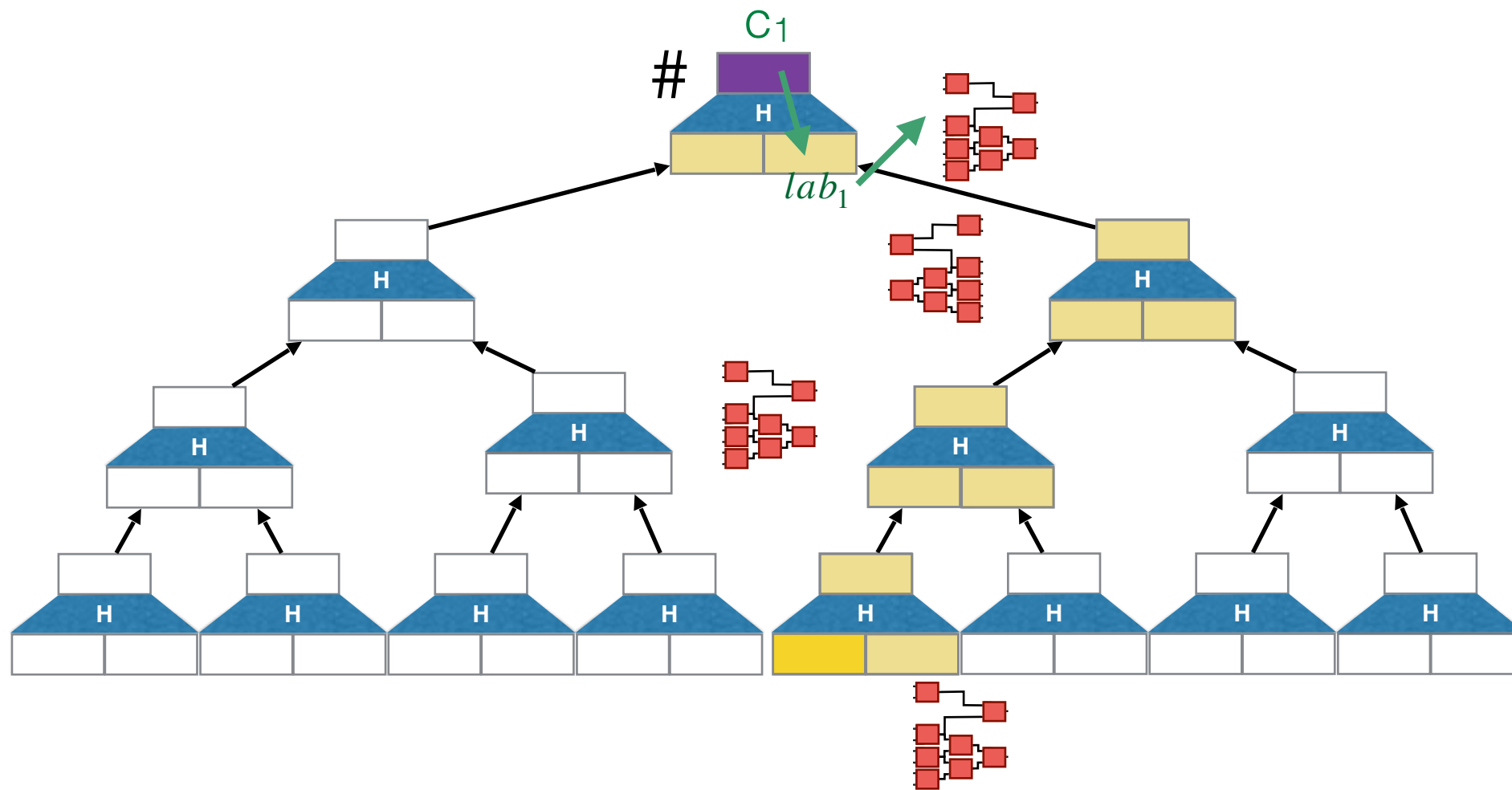
Laconic OT: Decryption



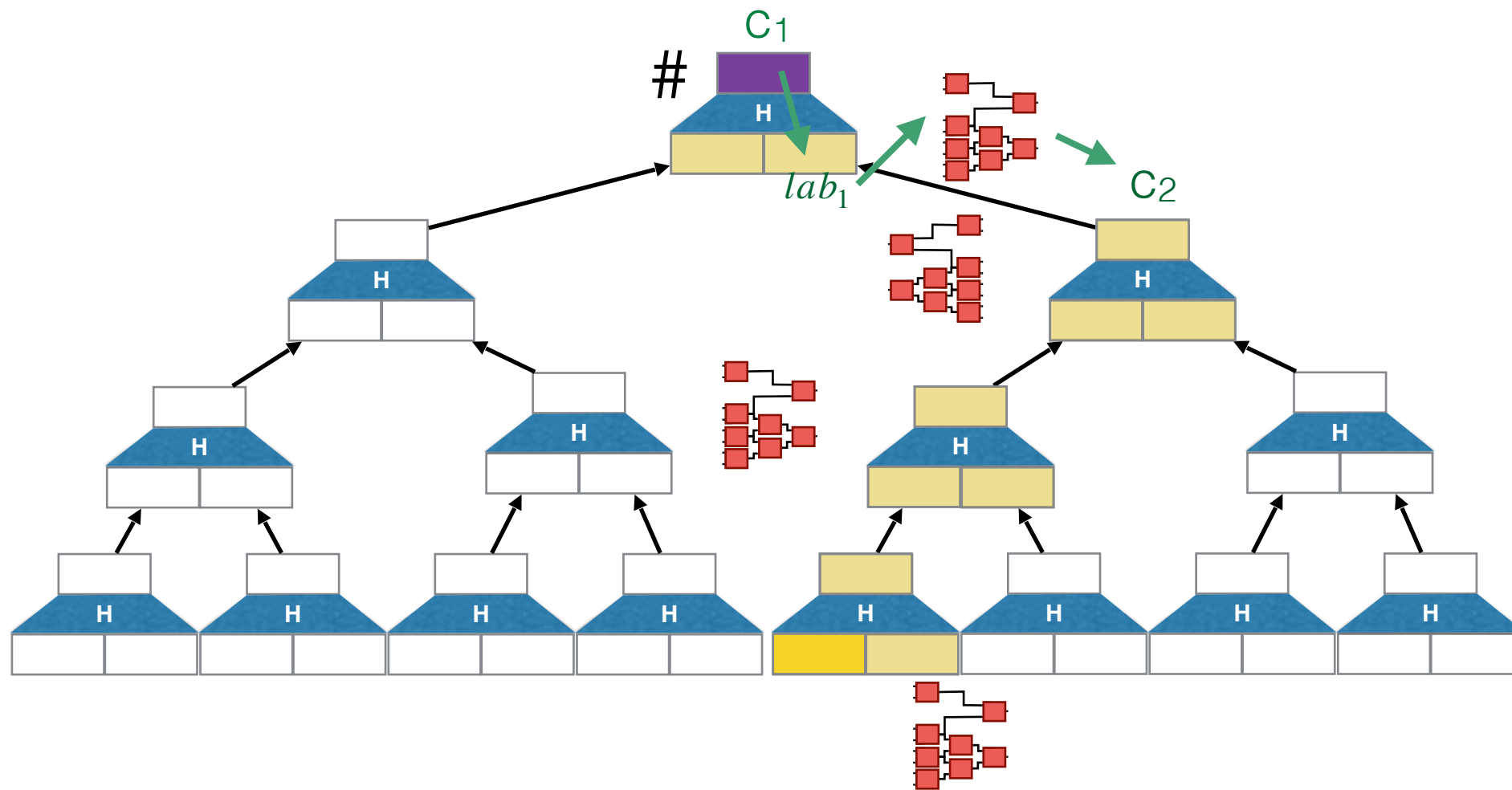
Laconic OT: Decryption



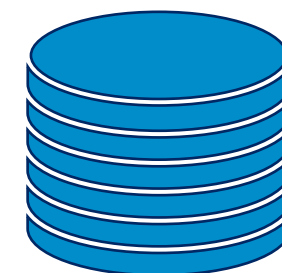
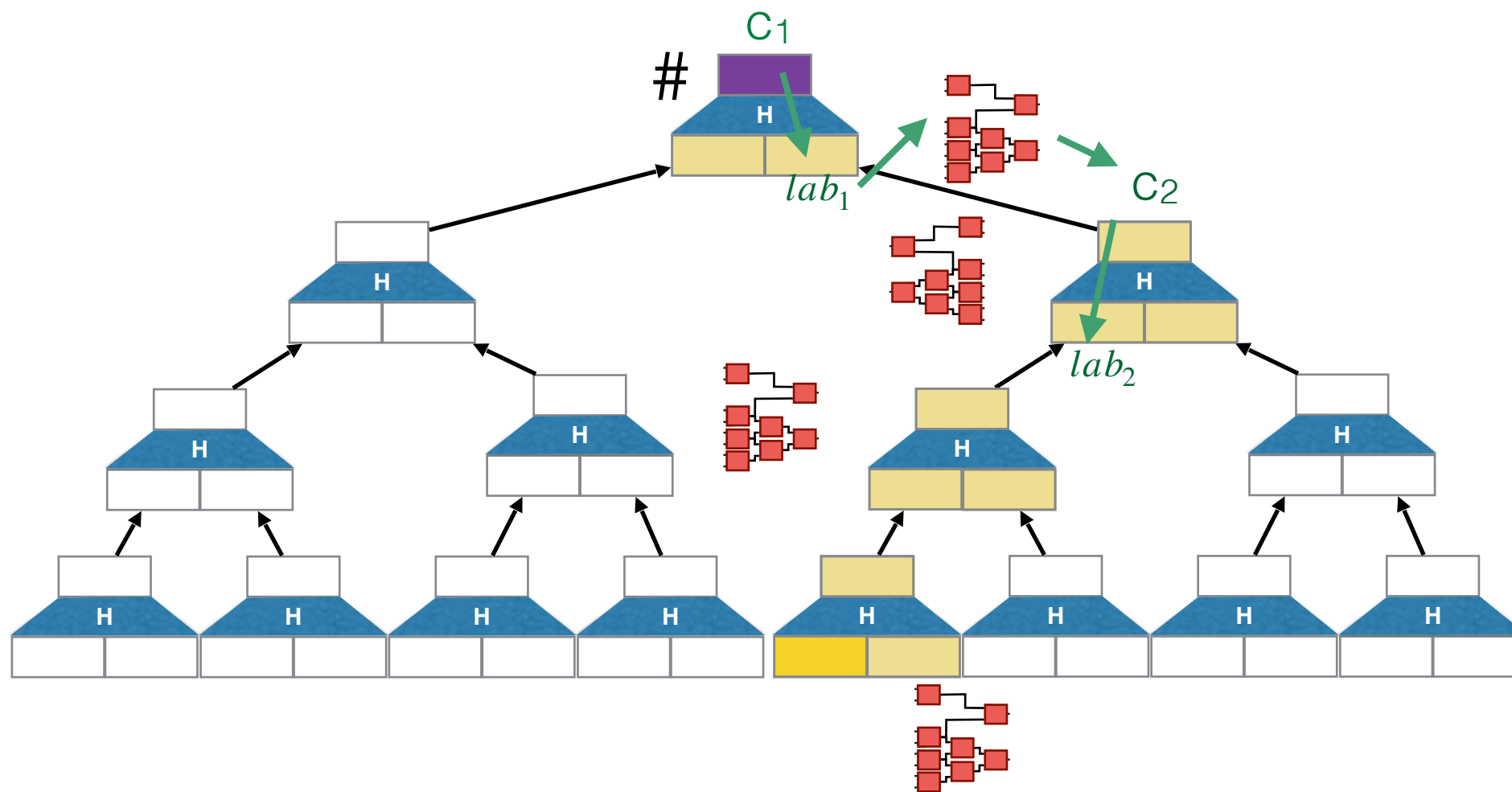
Laconic OT: Decryption



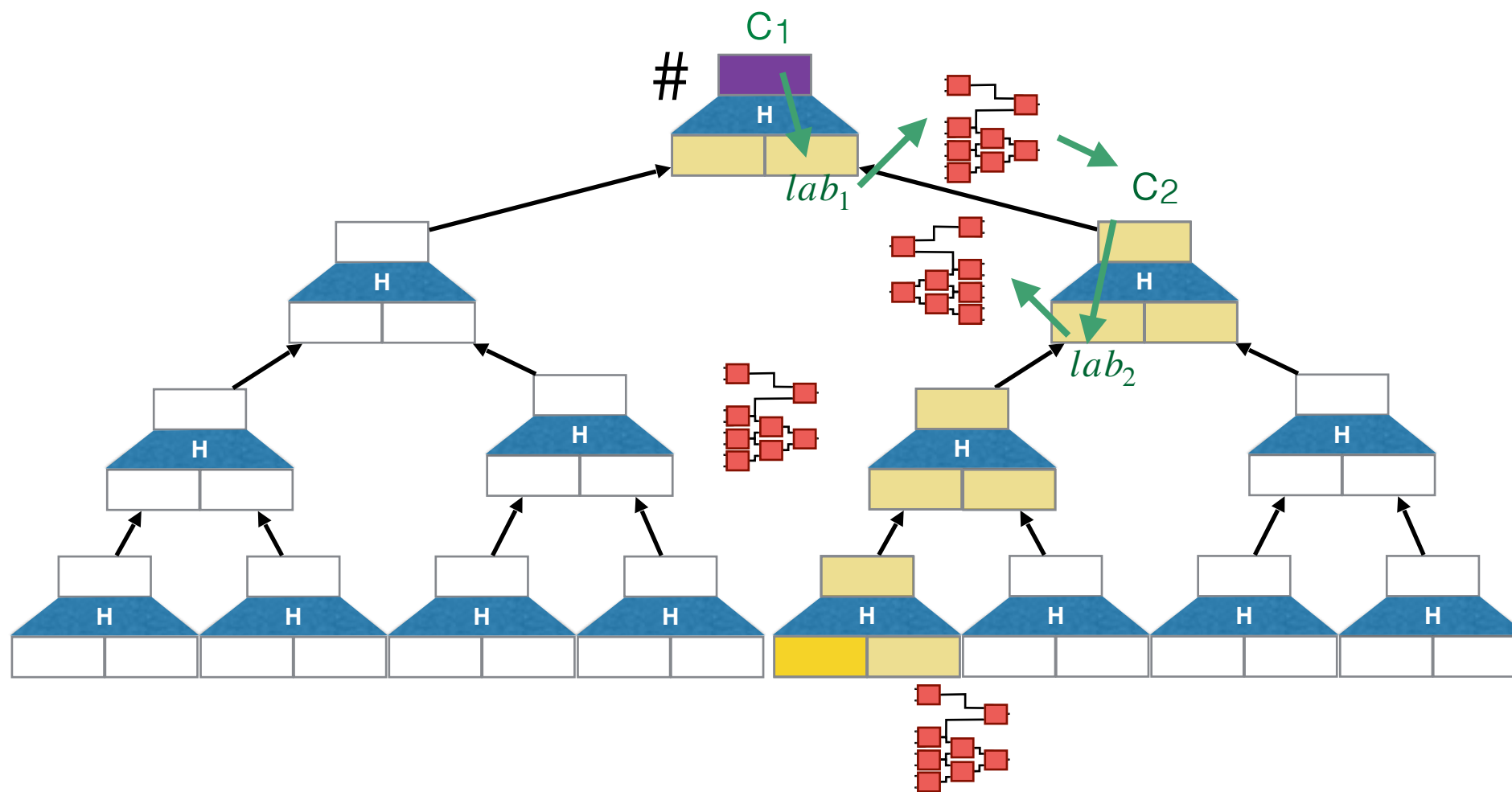
Laconic OT: Decryption



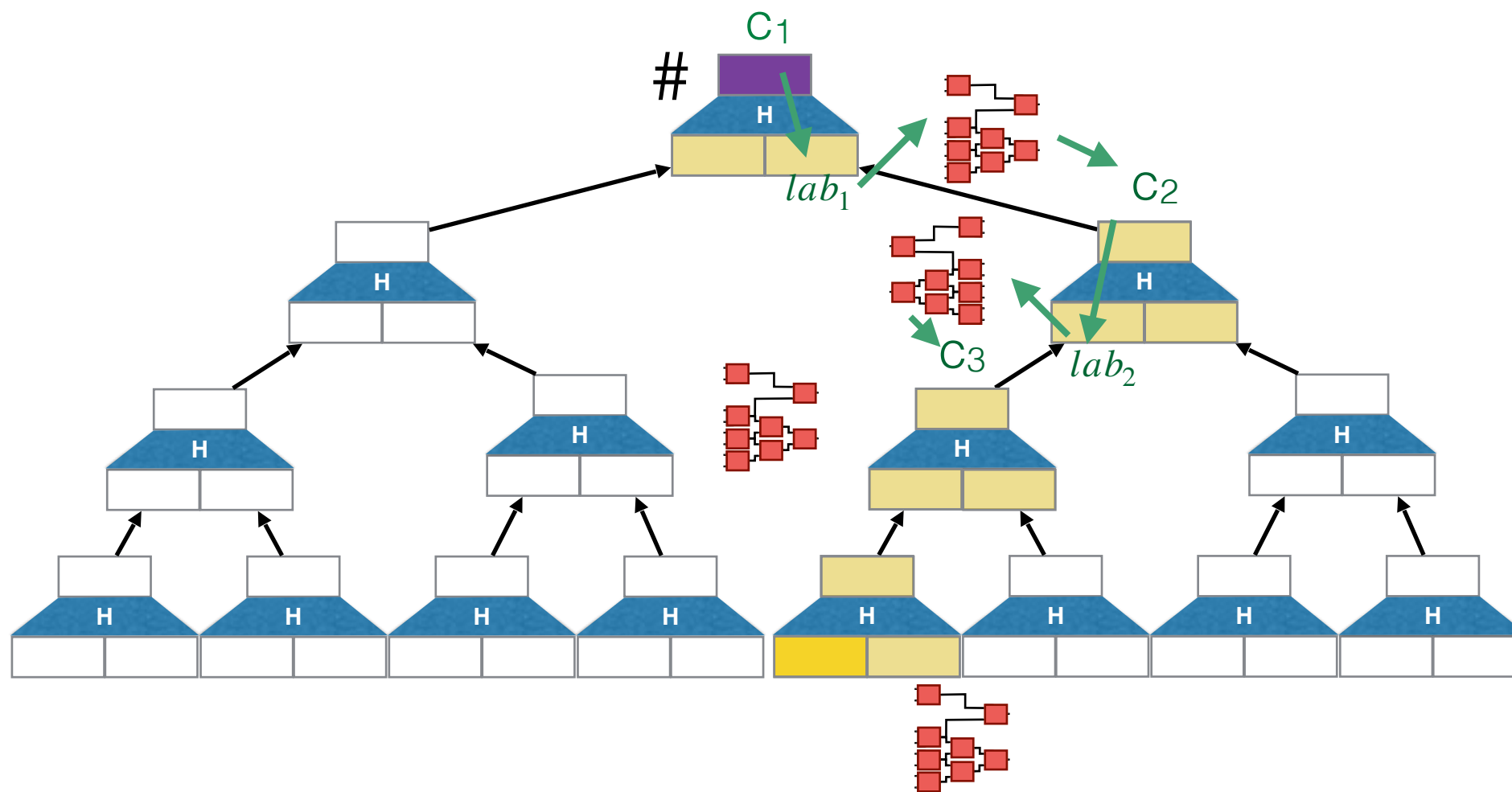
Laconic OT: Decryption



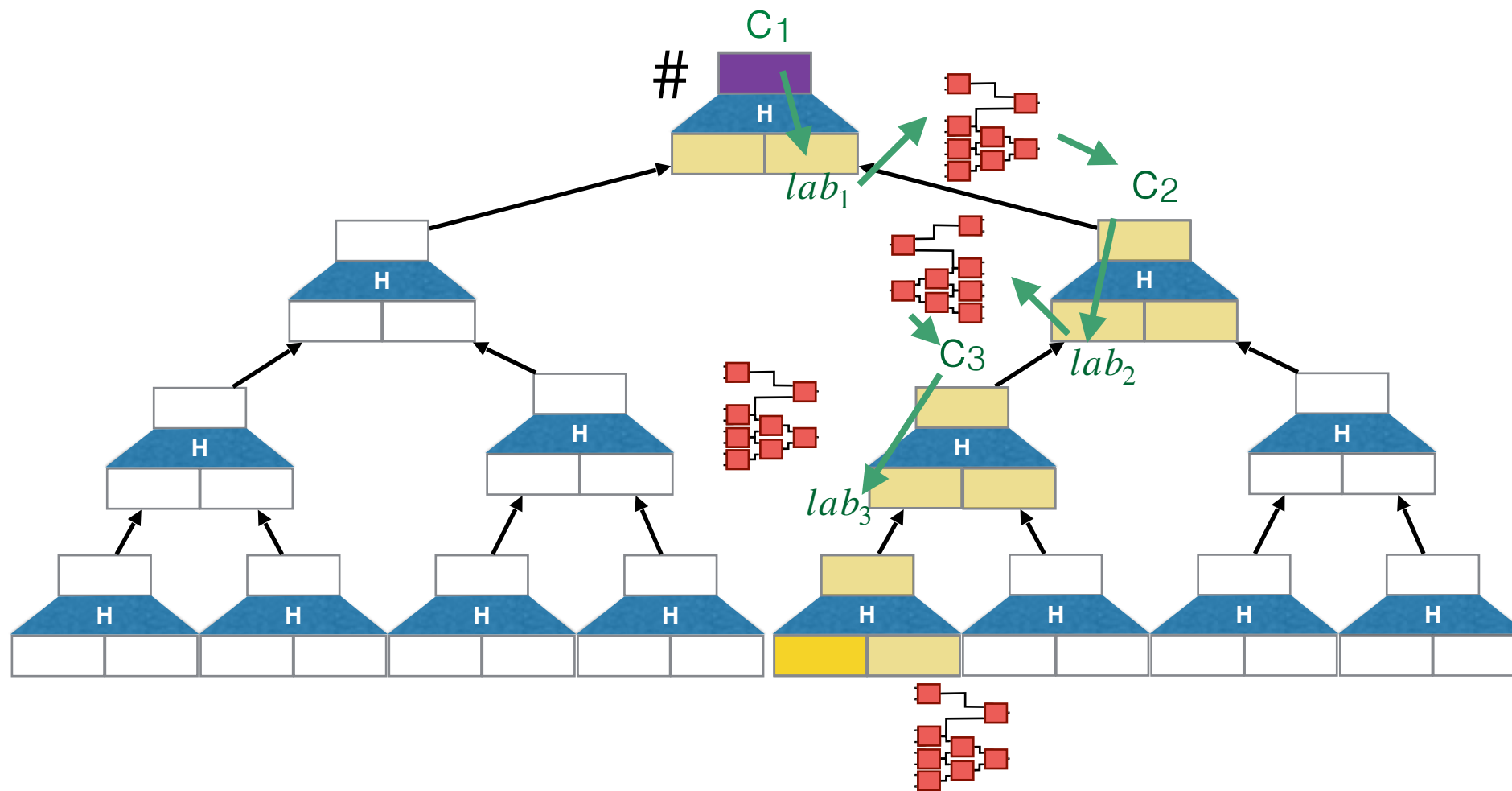
Laconic OT: Decryption



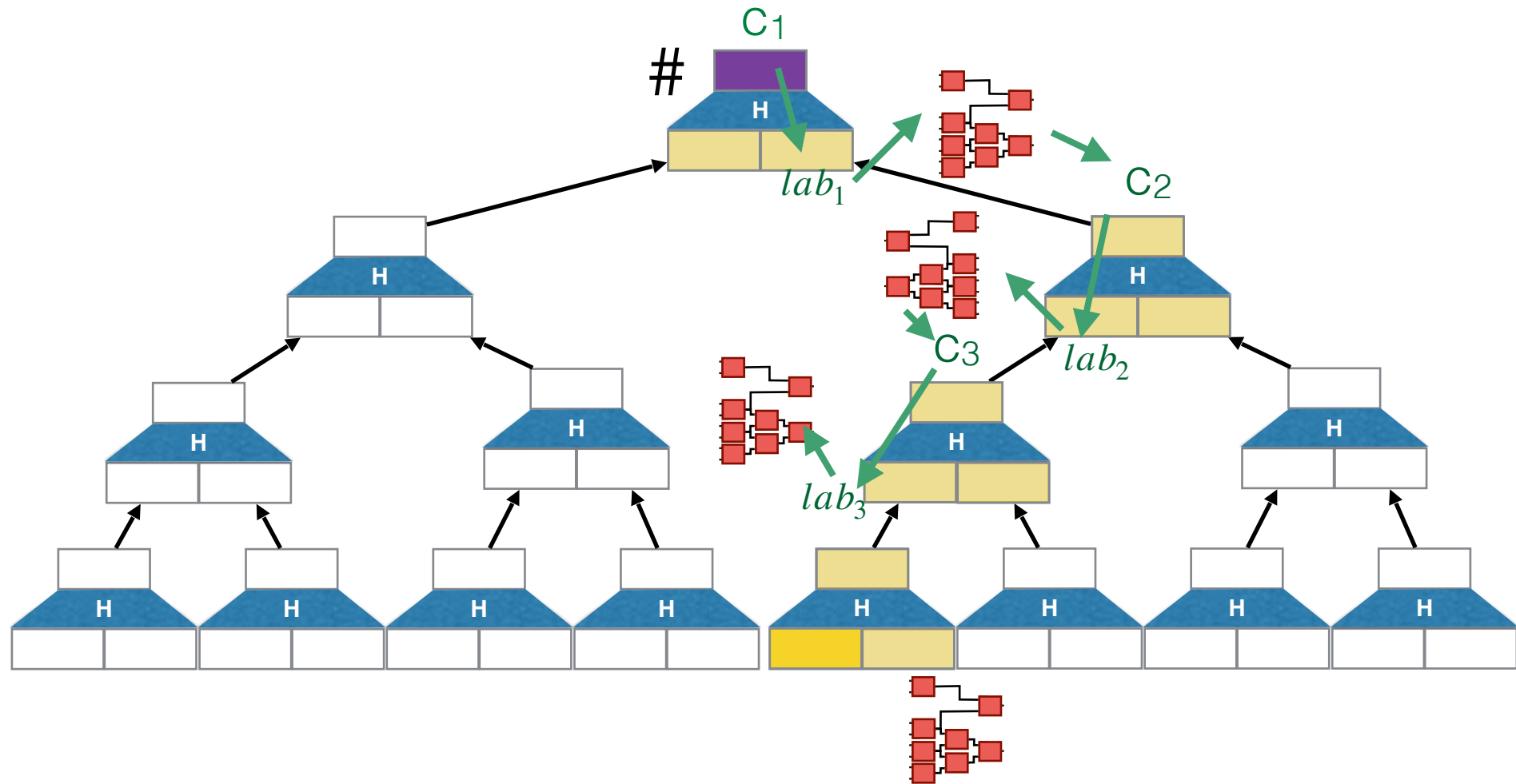
Laconic OT: Decryption



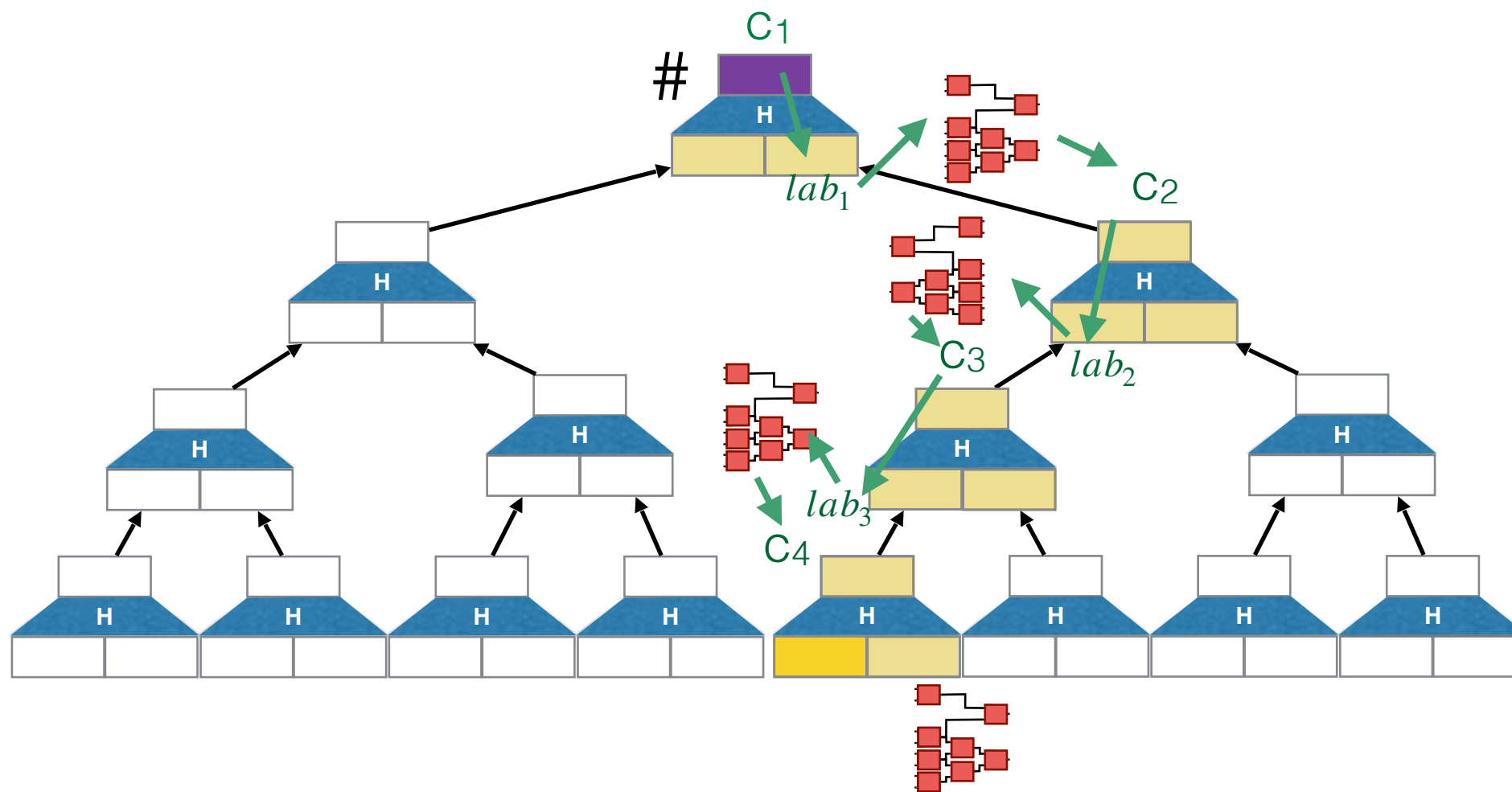
Laconic OT: Decryption



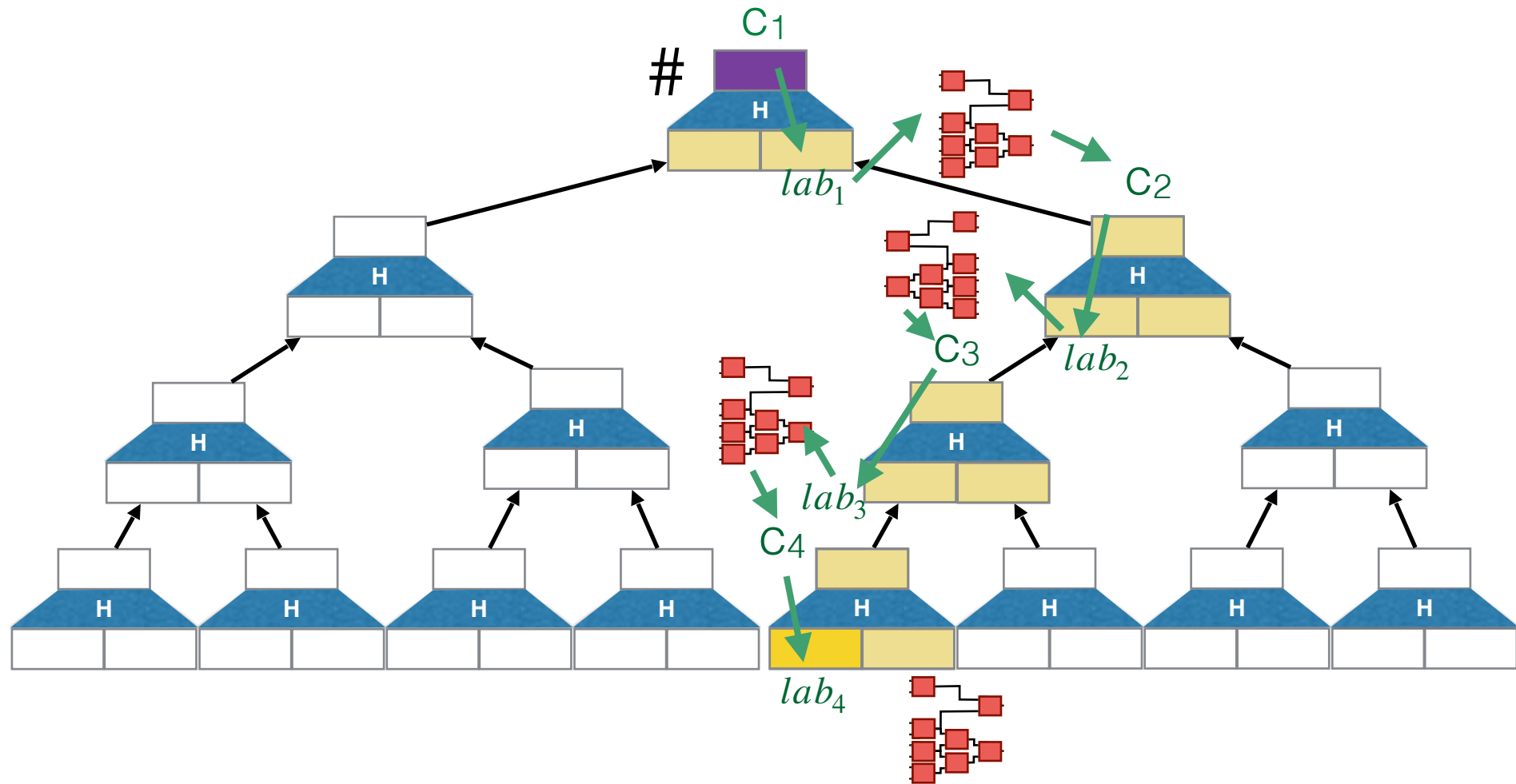
Laconic OT: Decryption



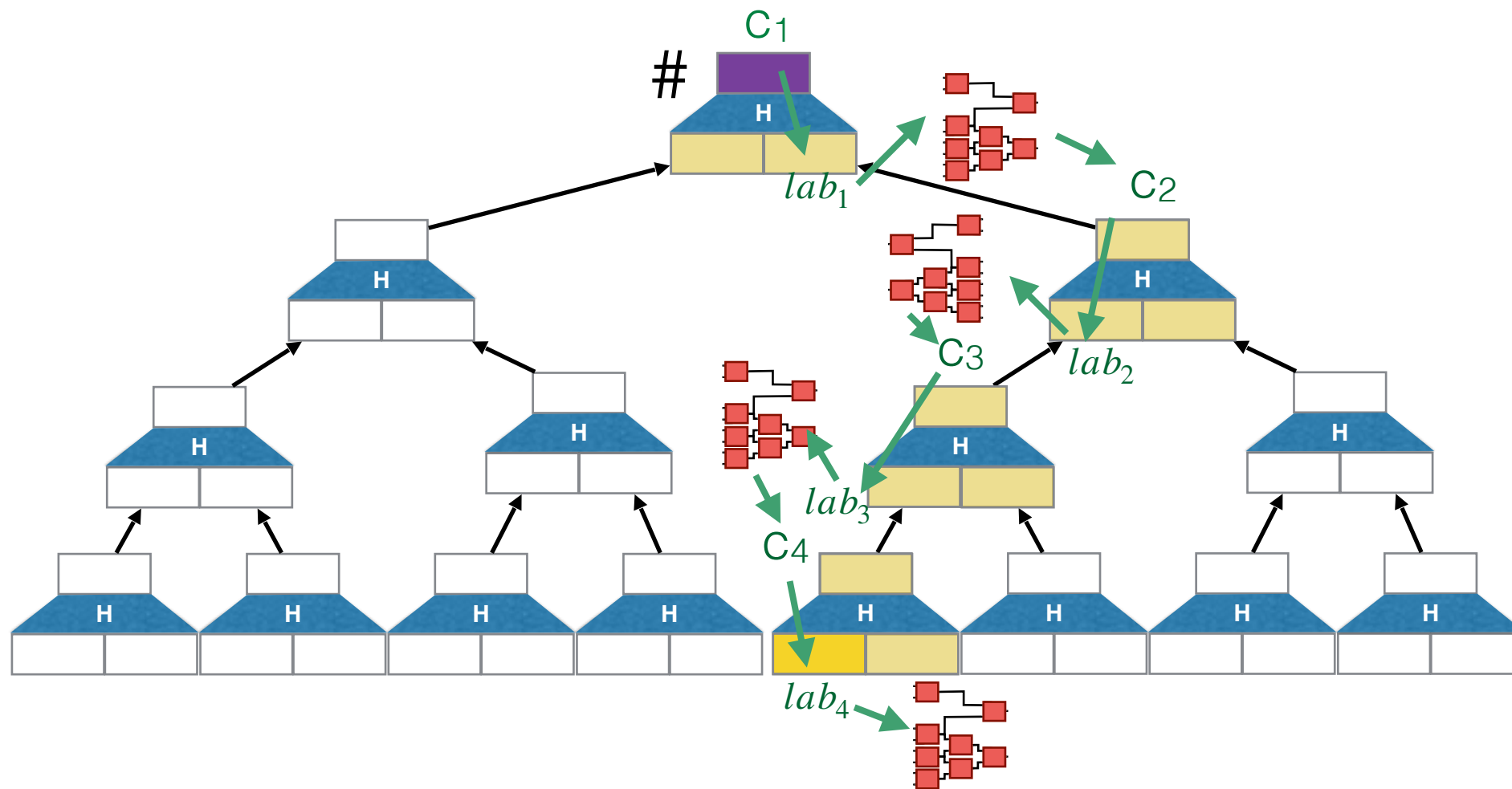
Laconic OT: Decryption



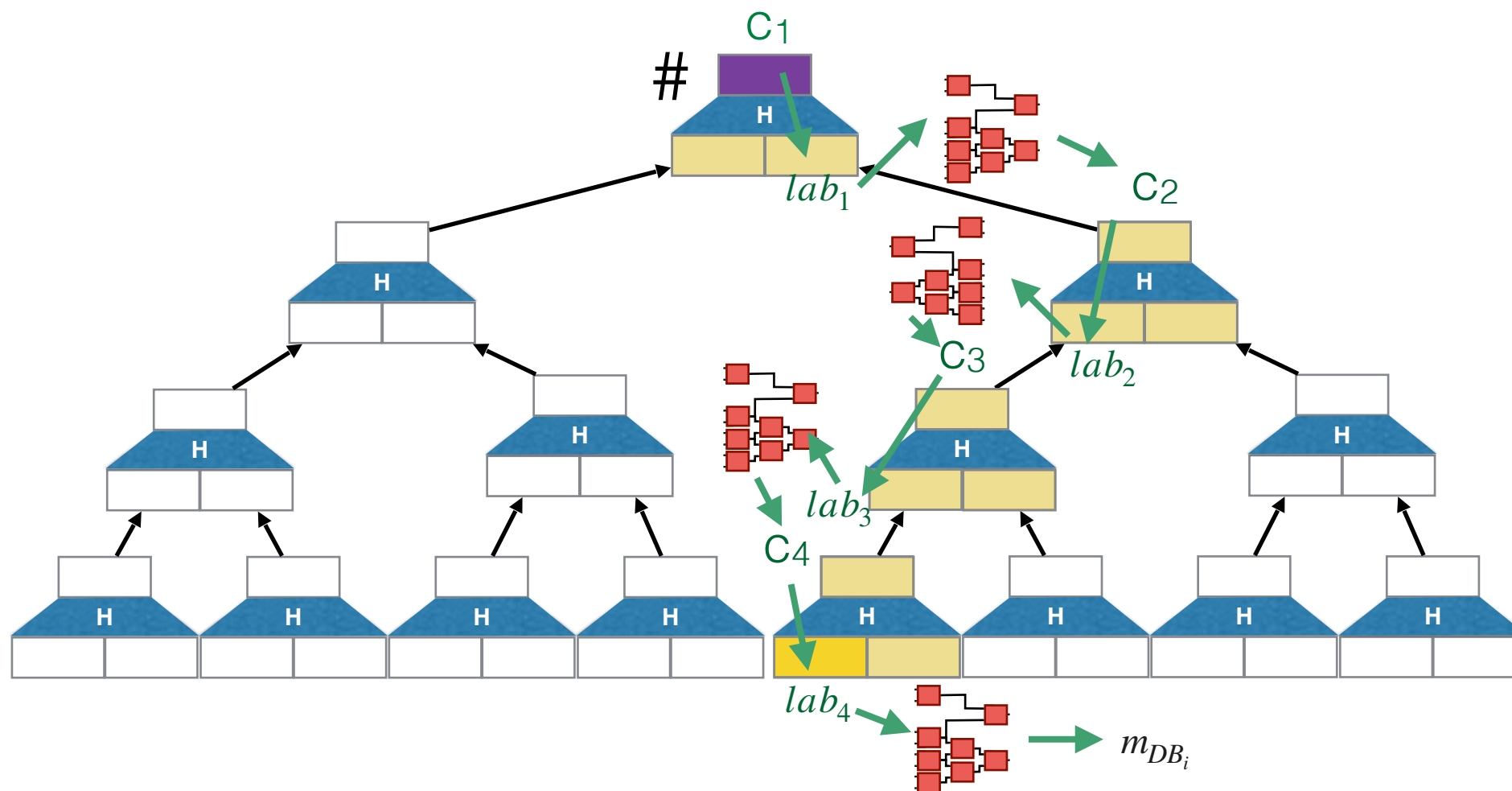
Laconic OT: Decryption



Laconic OT: Decryption



Laconic OT: Decryption





Advanced Constructions

Identity-Based Encryption [Sha84]

$(mpk, msk) \leftarrow Setup(1^\lambda)$



mpk



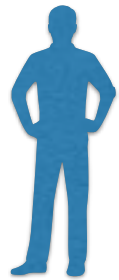
Identity-Based Encryption [Sha84]

$(mpk, msk) \leftarrow Setup(1^\lambda)$



“bob@nist.gov”

mpk



Identity-Based Encryption [Sha84]

$(mpk, msk) \leftarrow Setup(1^\lambda)$
 $sk_{id} \leftarrow KeyGen(msk, id)$



“bob@nist.gov”

mpk



Identity-Based Encryption [Sha84]

$$(mpk, msk) \leftarrow Setup(1^\lambda)$$
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$sk_{bob@nist.gov}$

“bob@nist.gov”

mpk



Identity-Based Encryption [Sha84]

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$$c \leftarrow Encrypt(mpk, id, m)$$



Identity-Based Encryption [Sha84]

$$(mpk, msk) \leftarrow Setup(1^\lambda)$$
$$sk_{id} \leftarrow KeyGen(msk, id)$$



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mpk



$$c \leftarrow Encrypt(mpk, id, m)$$



Identity-Based Encryption [Sha84]

$(mpk, msk) \leftarrow Setup(1^\lambda)$
 $sk_{id} \leftarrow KeyGen(msk, id)$



$sk_{bob@nist.gov}$

“bob@nist.gov”

mpk



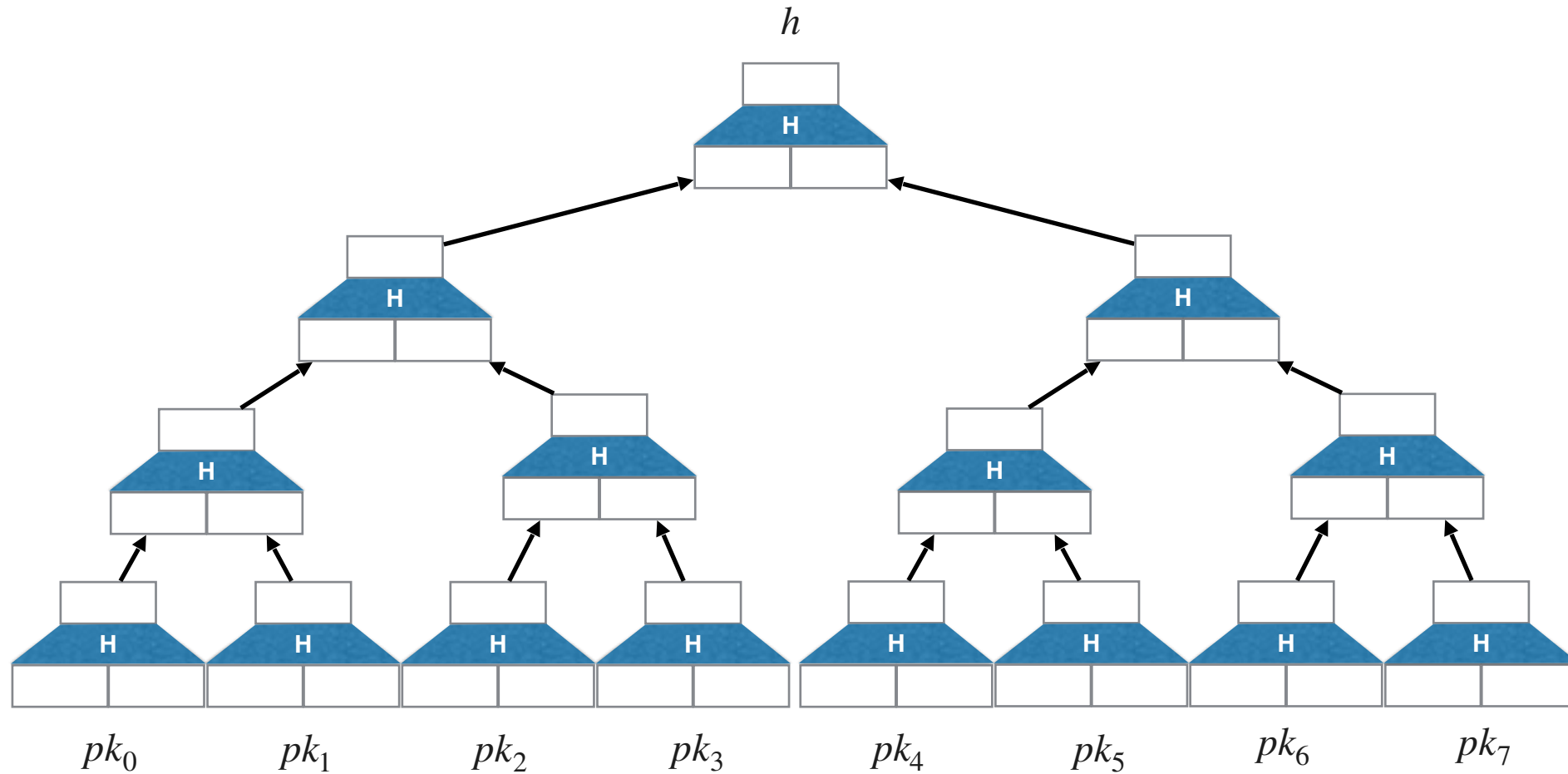
$c \leftarrow Encrypt(mpk, id, m)$

$m \leftarrow Decrypt(sk_{id}, c)$





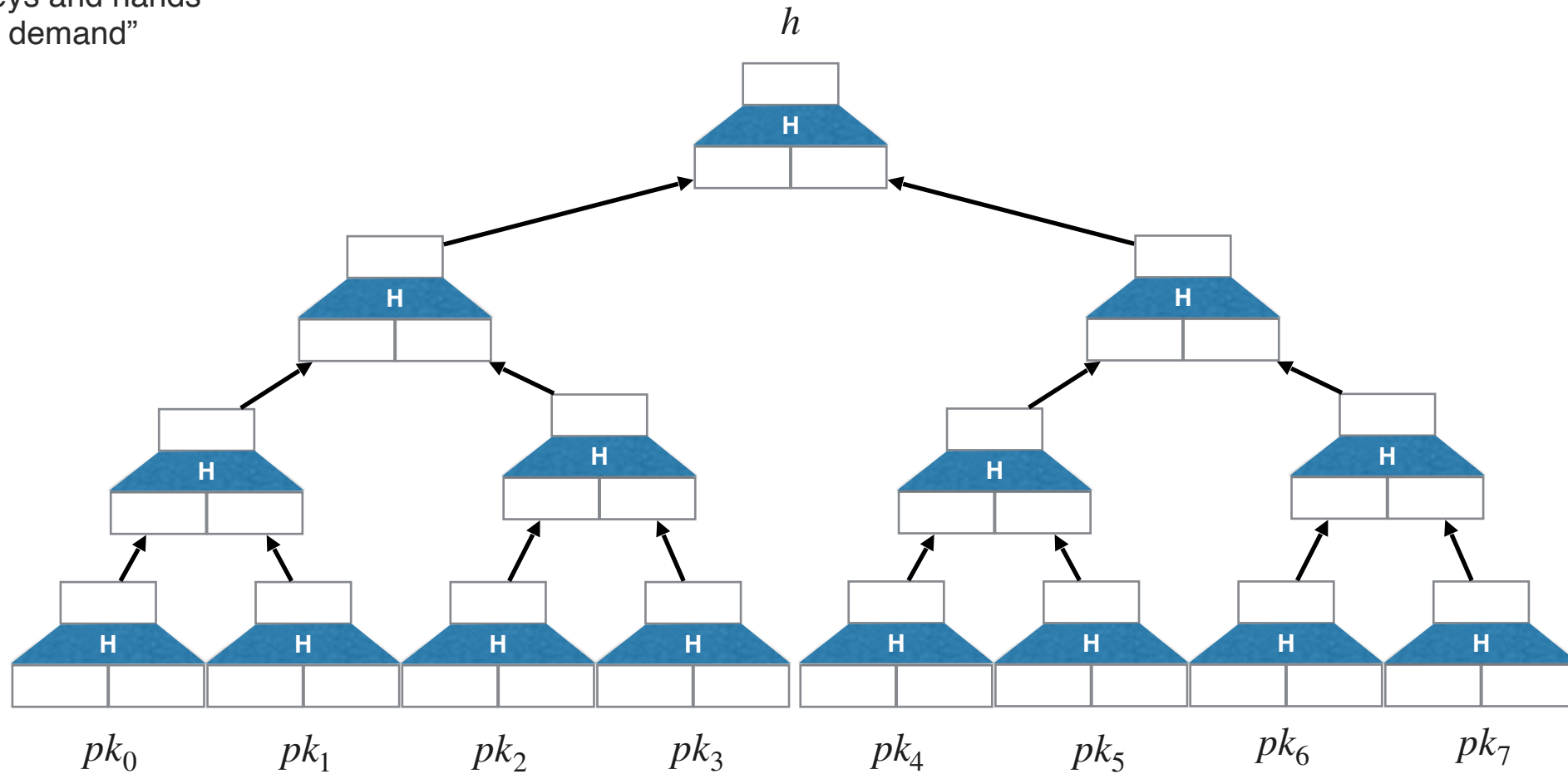
Identity-Based Encryption [DG17]: Setup





Identity-Based Encryption [DG17]: Setup

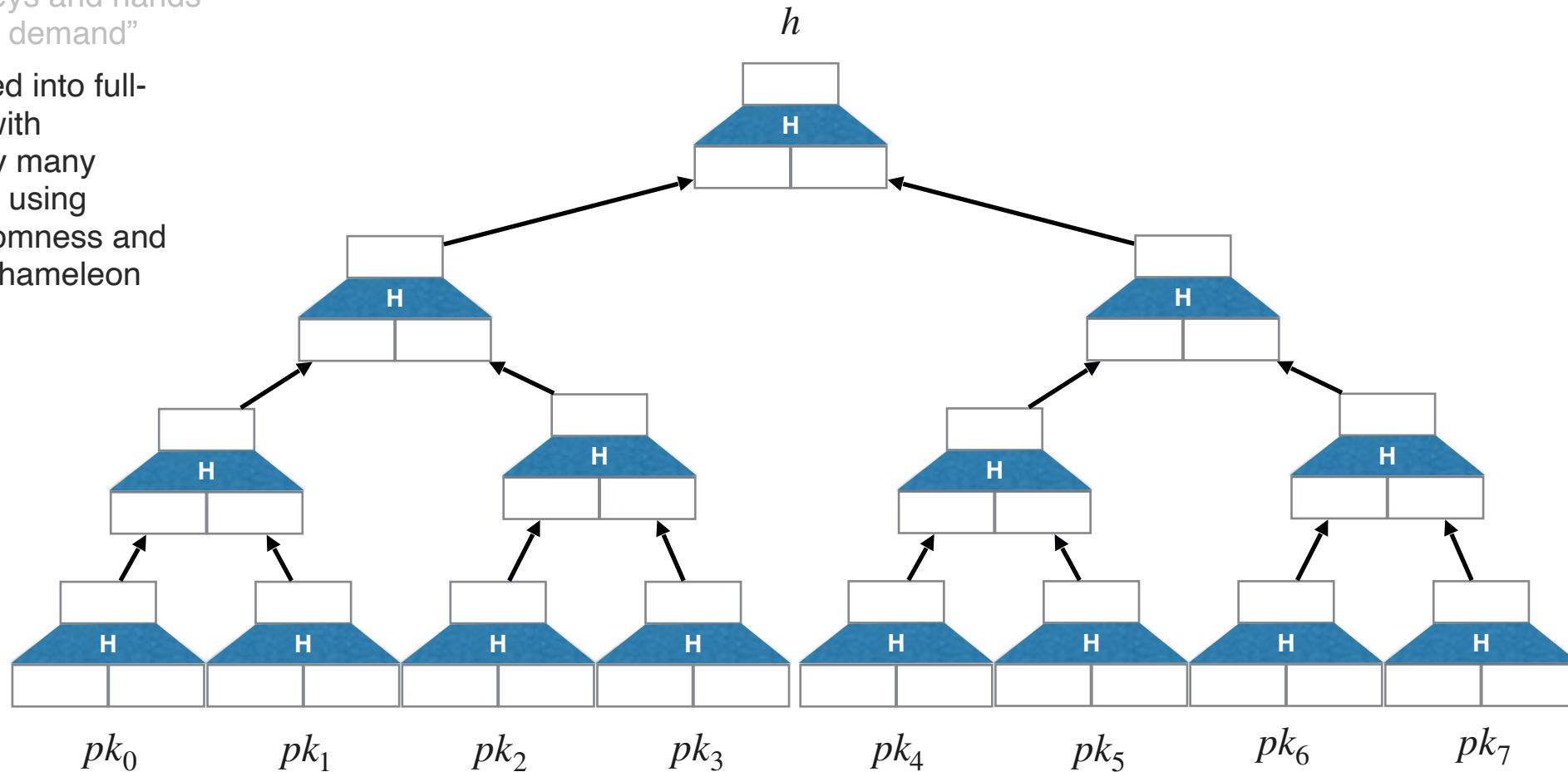
- Simpler Setting: Key generator has “pre-generated” a polynomial number of keys and hands them out “on demand”





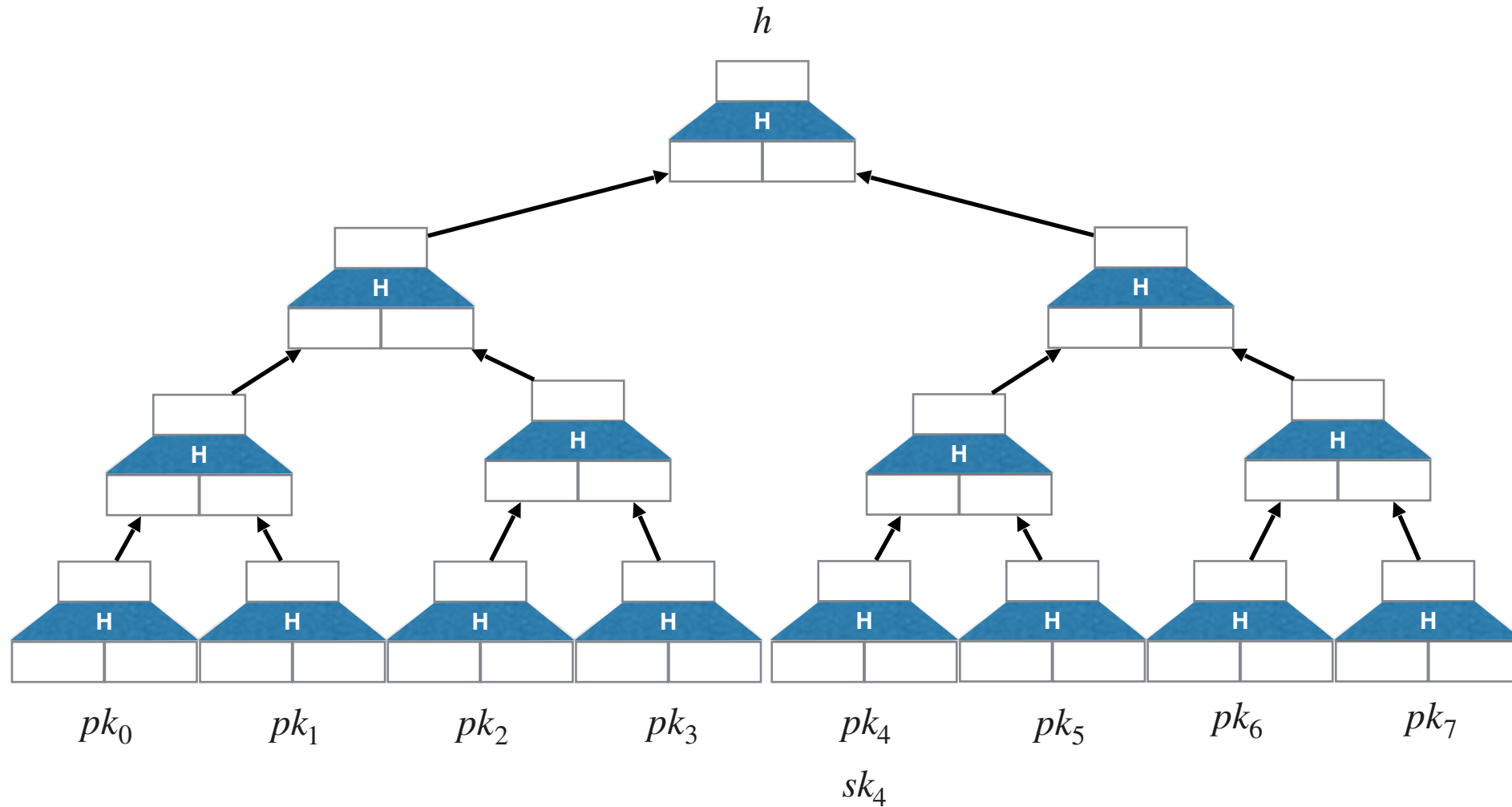
Identity-Based Encryption [DG17]: Setup

- Simpler Setting: Key generator has “pre-generated” a polynomial number of keys and hands them out “on demand”
- Can be turned into full-blown IBE (with exponentially many identities) by using pseudorandomness and trapdoors (Chameleon encryption)



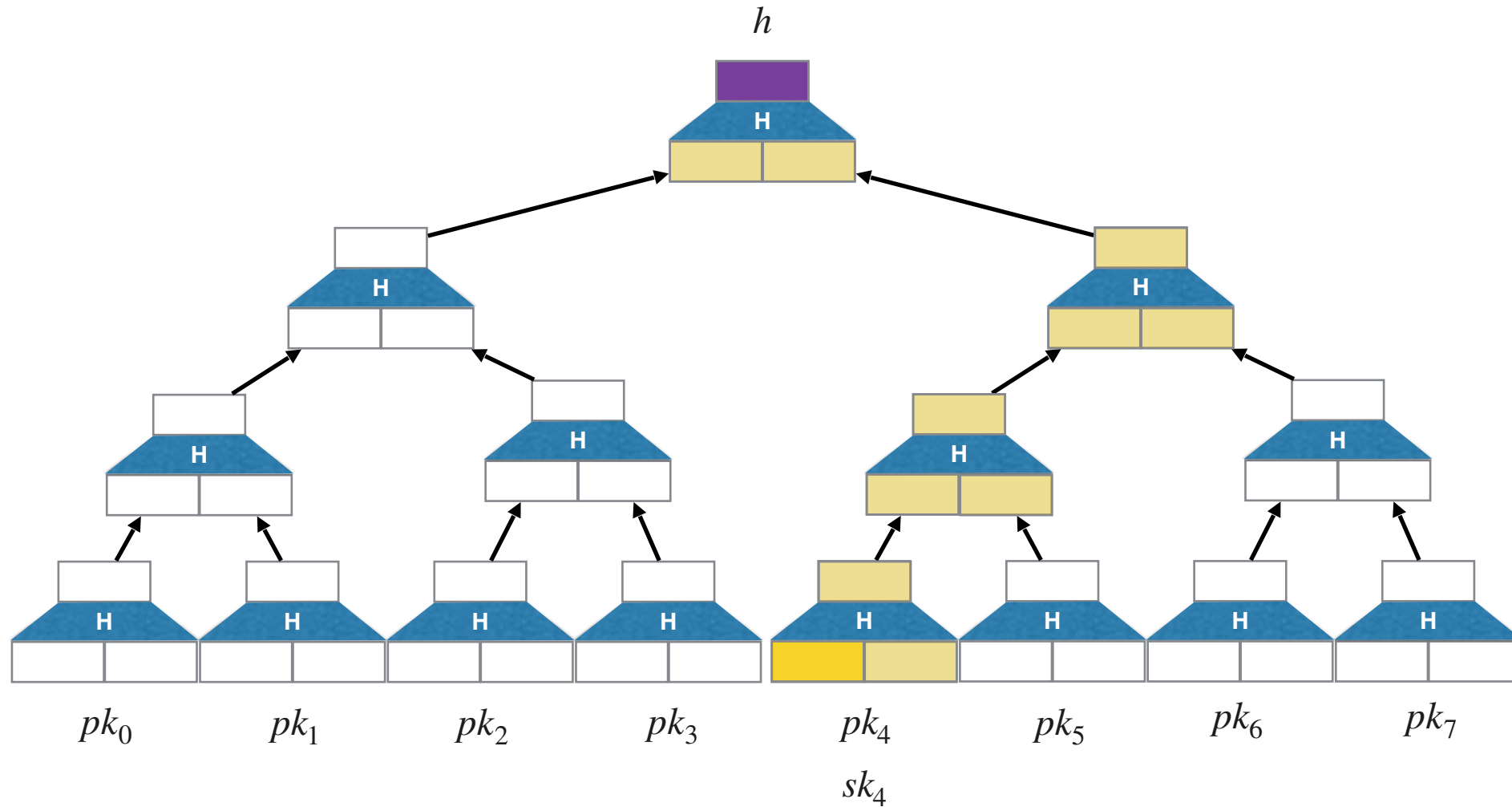


Identity-Based Encryption [DG17]: KeyGen





Identity-Based Encryption [DG17]: KeyGen



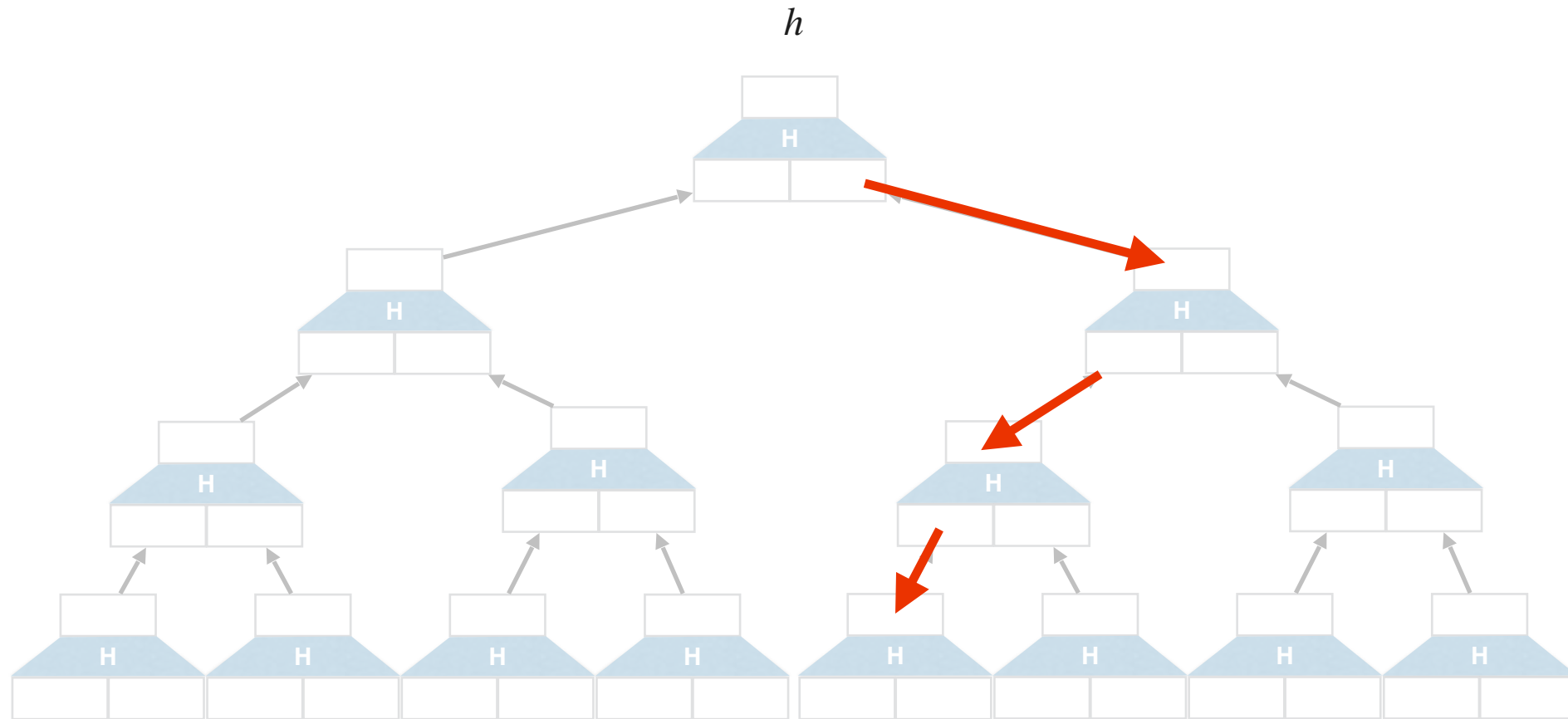


Identity-Based Encryption [DG17]: Encryption

Reverse Delegation as in Laconic OT



id m



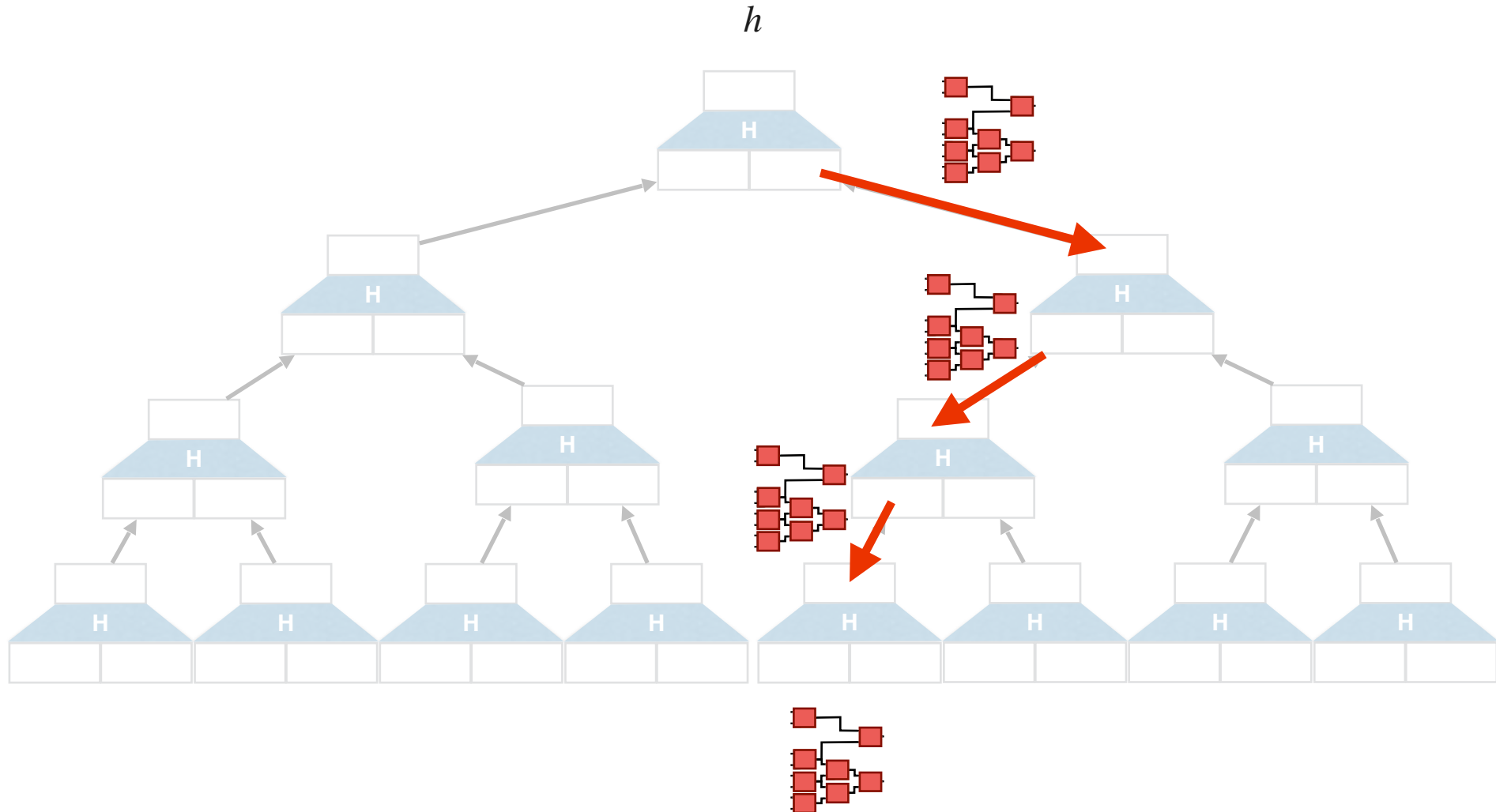


Identity-Based Encryption [DG17]: Encryption

Reverse Delegation as in Laconic OT



id m



Registration-based Encryption [GHMR18]



$(pk, sk) \leftarrow \text{KeyGen}()$

Registration-based Encryption [GHMR18]

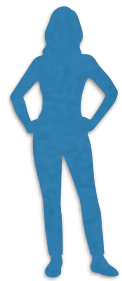
- Master Secret Key msk is single point of failure in IBE



$(pk, sk) \leftarrow \text{KeyGen}()$

Registration-based Encryption [GHMR18]

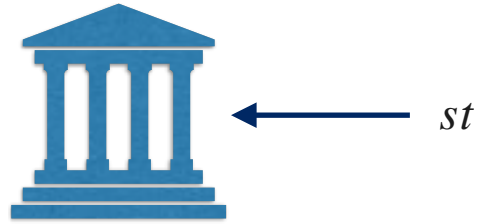
- Master Secret Key msk is single point of failure in IBE
- Idea: Replace Key-Authority with Key-Curator



$(pk, sk) \leftarrow \text{KeyGen}()$

Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
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$(pk, sk) \leftarrow \text{KeyGen}()$

Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
- Idea: Replace Key-Authority with Key-Curator



st

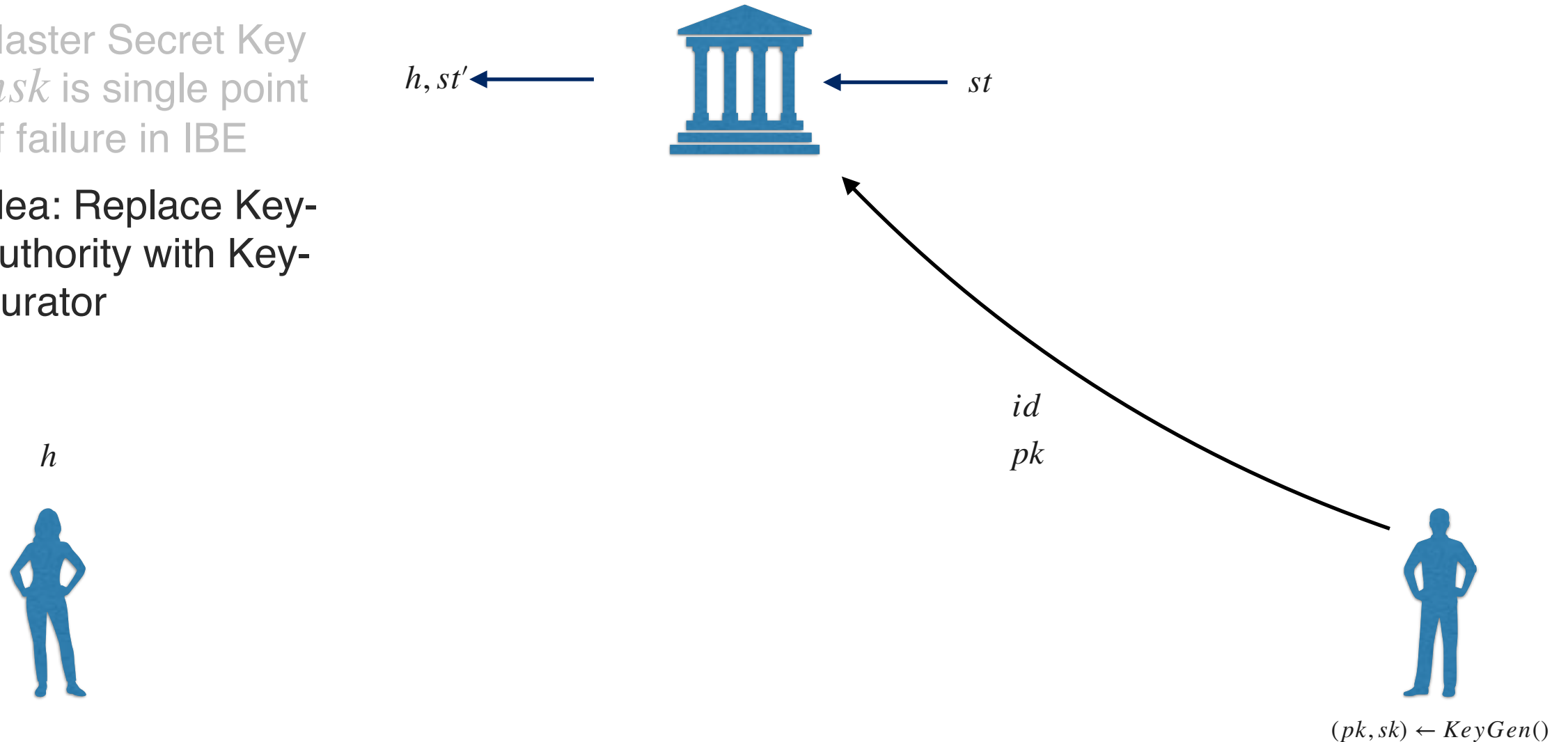
id
 pk



$(pk, sk) \leftarrow \text{KeyGen}()$

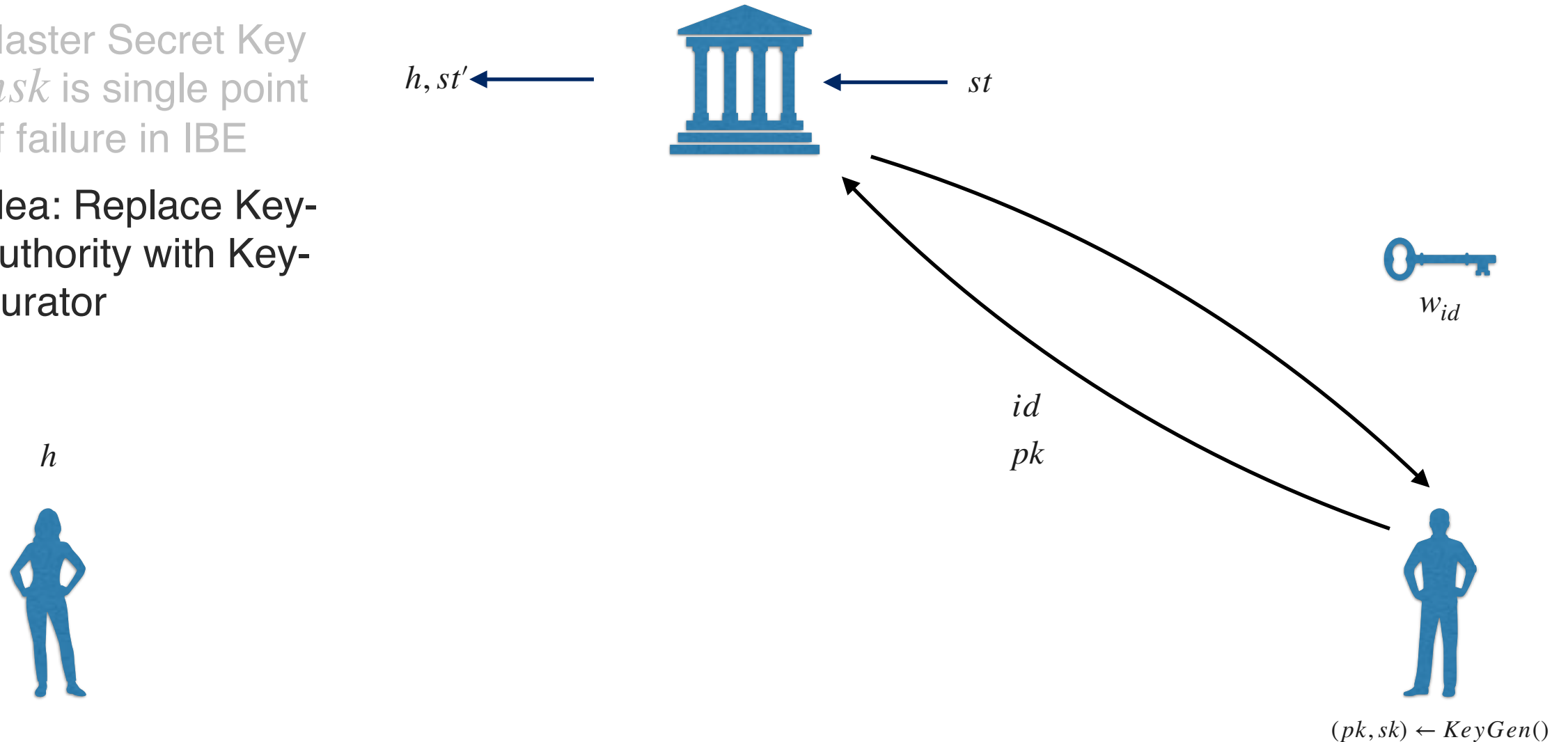
Registration-based Encryption [GHMR18]

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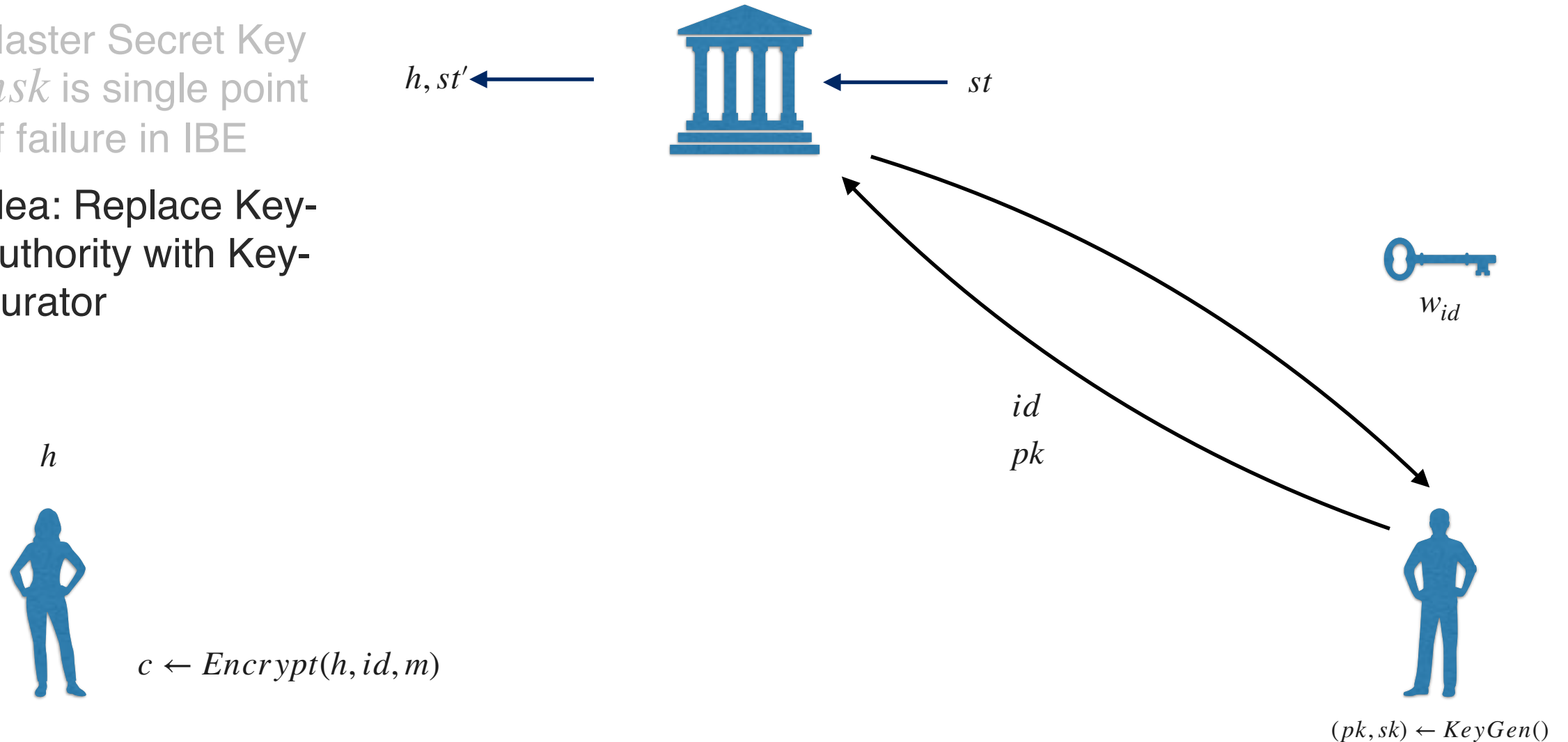
Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
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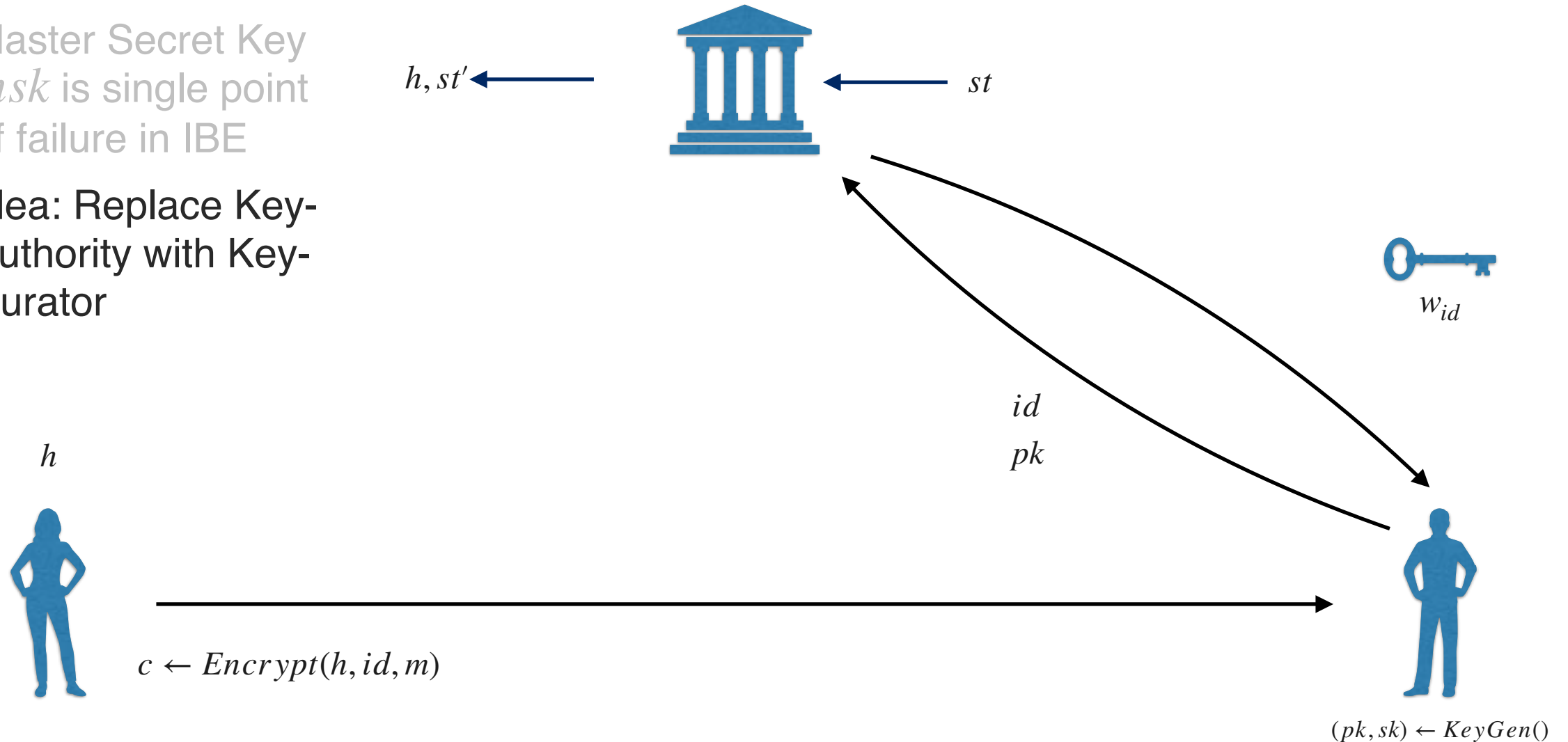
Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
- Idea: Replace Key-Authority with Key-Curator



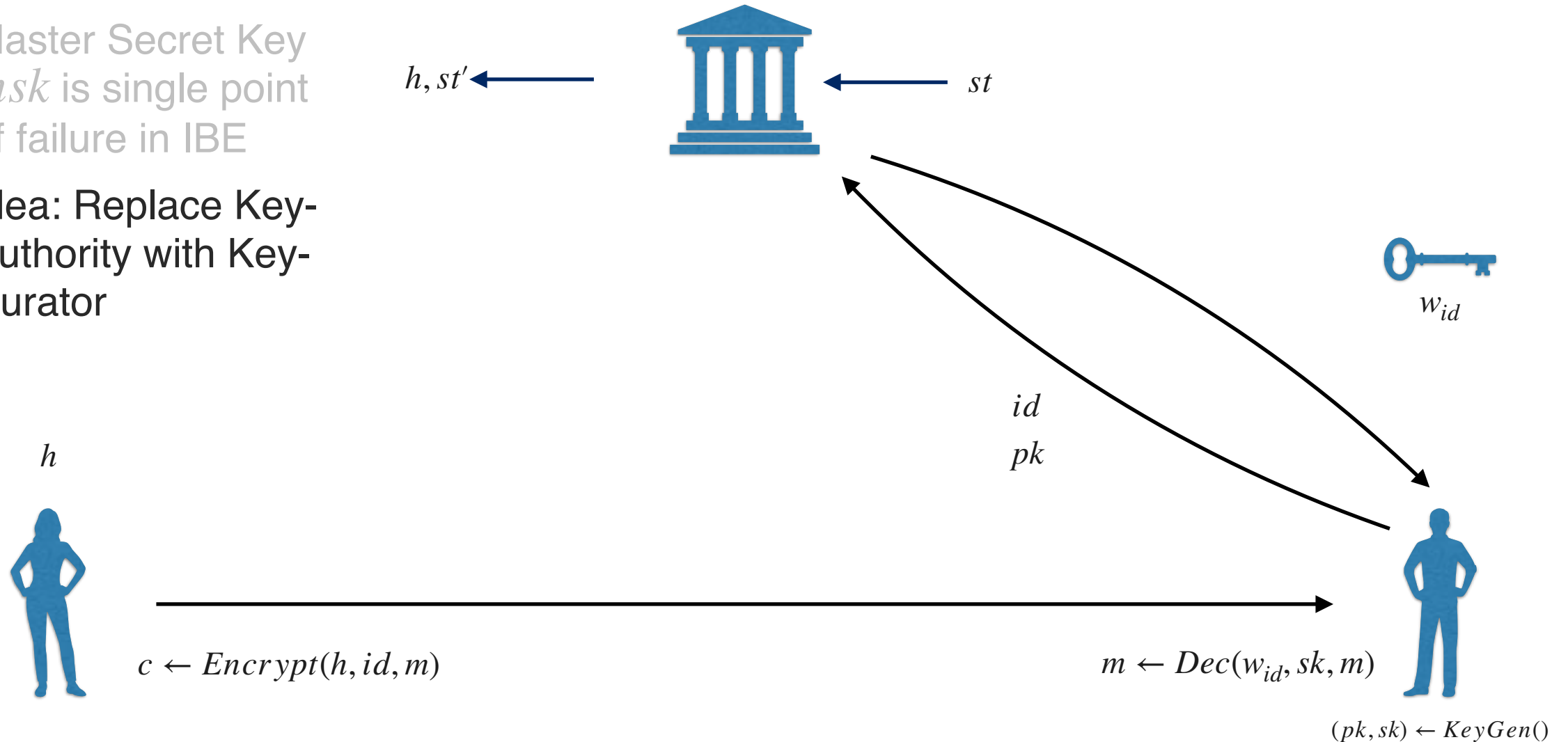
Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
- Idea: Replace Key-Authority with Key-Curator



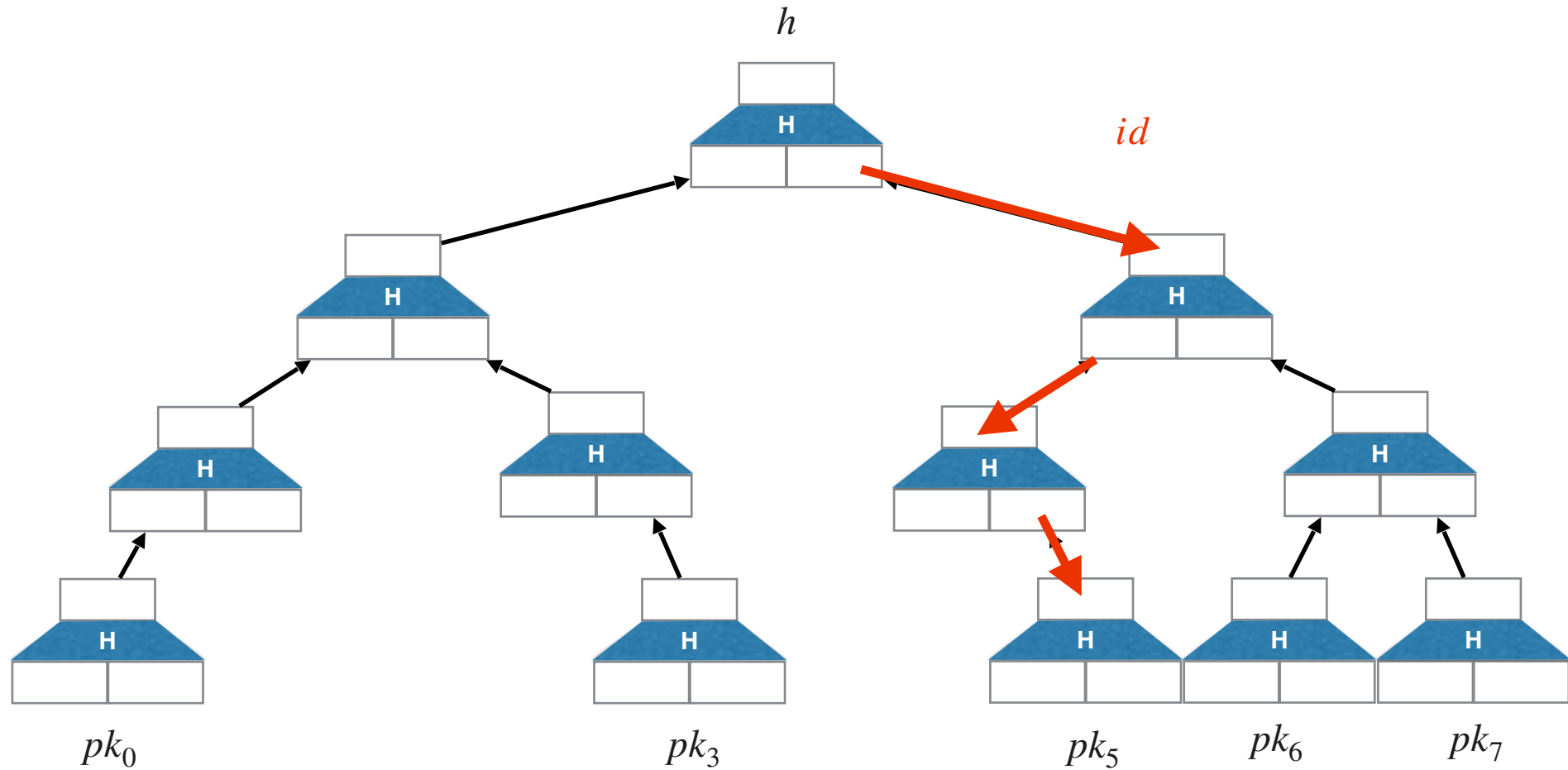
Registration-based Encryption [GHMR18]

- Master Secret Key msk is single point of failure in IBE
- Idea: Replace Key-Authority with Key-Curator





Registration-based Encryption: Registration

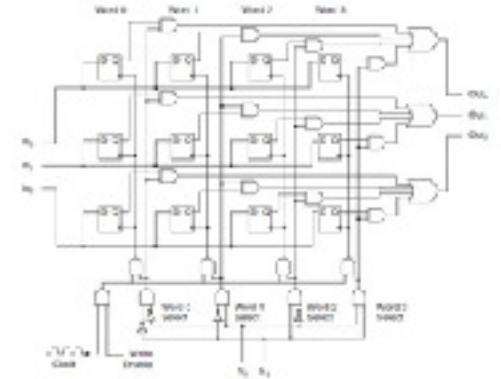




Laconic Function Evaluation [QWW18]



x



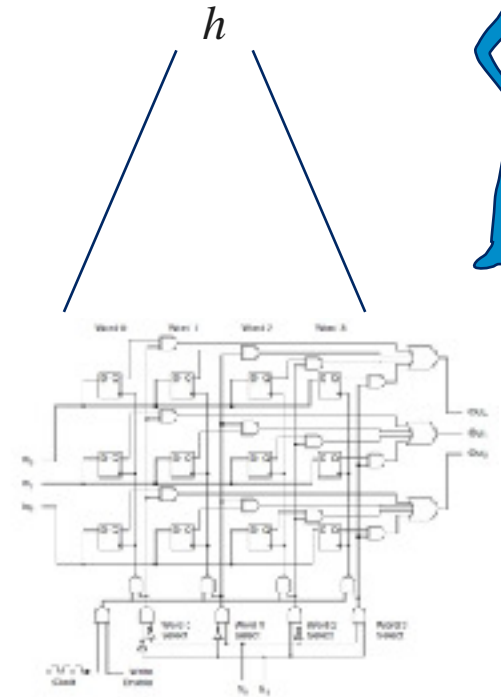
C



Laconic Function Evaluation [QWW18]



x



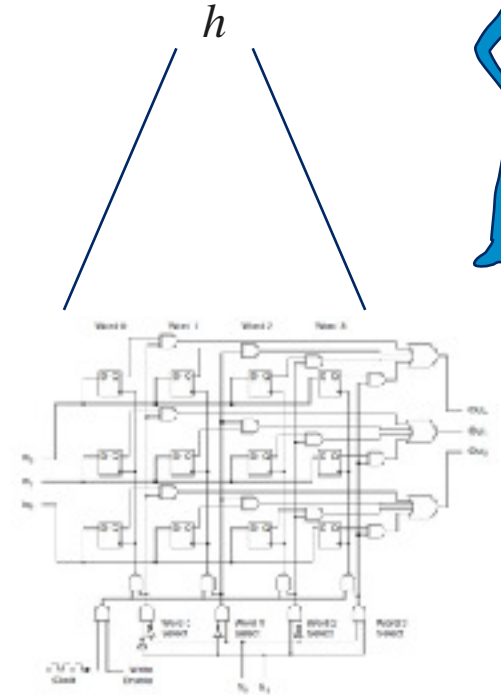
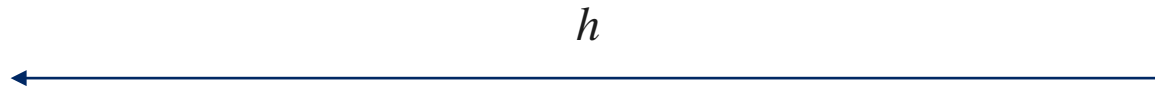
C



Laconic Function Evaluation [QWW18]



x



C



Laconic Function Evaluation [QWW18]

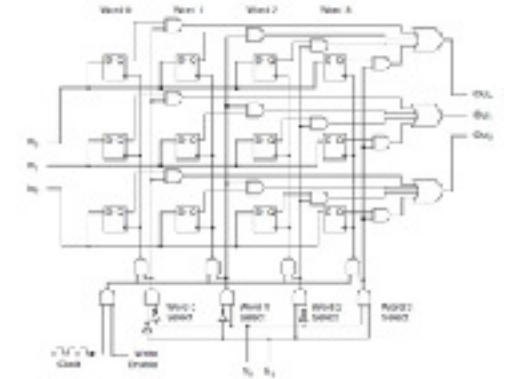


x



h

h



C

$$c = Enc(h, x)$$



Laconic Function Evaluation [QWW18]

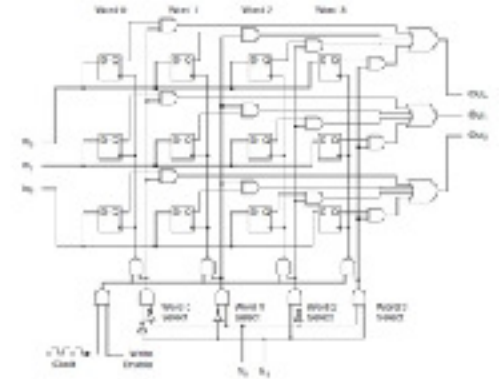


x



h

h



C

c



$$c = Enc(h, x)$$



Laconic Function Evaluation [QWW18]



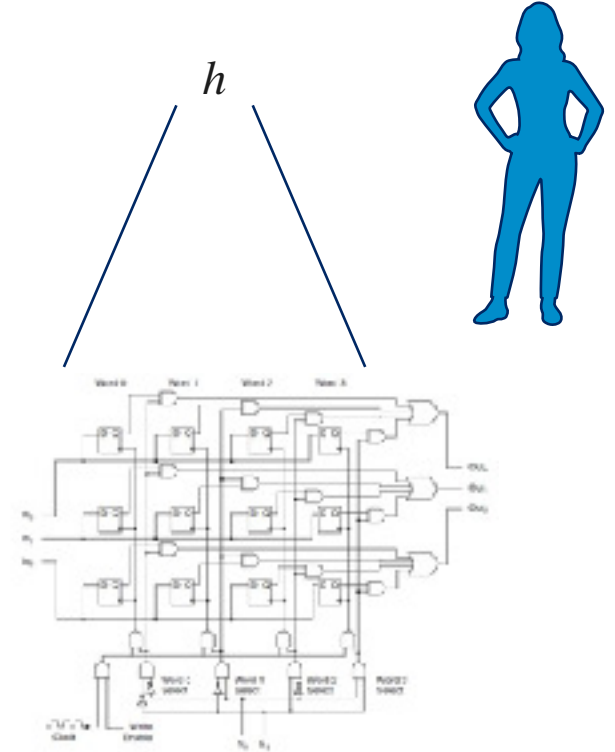
x

h



$$c = \text{Enc}(h, x)$$

c



C

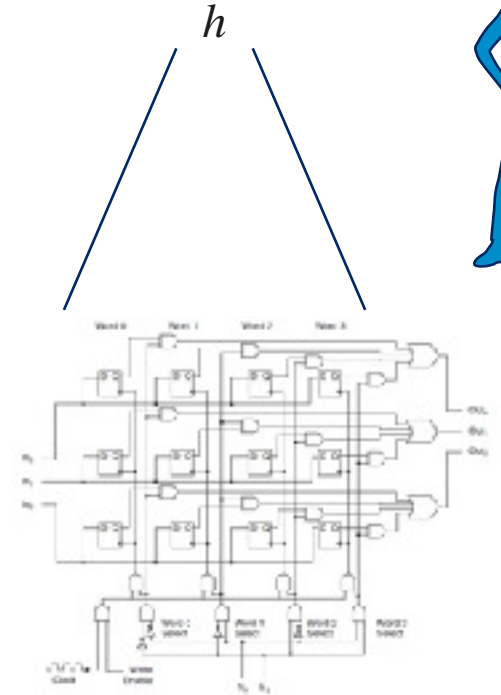
$$y = \text{Dec}(C, c) = C(x)$$



Laconic Function Evaluation [QWW18]



x



h



$$c = Enc(h, x)$$

c



$$y = Dec(C, c) = C(x)$$

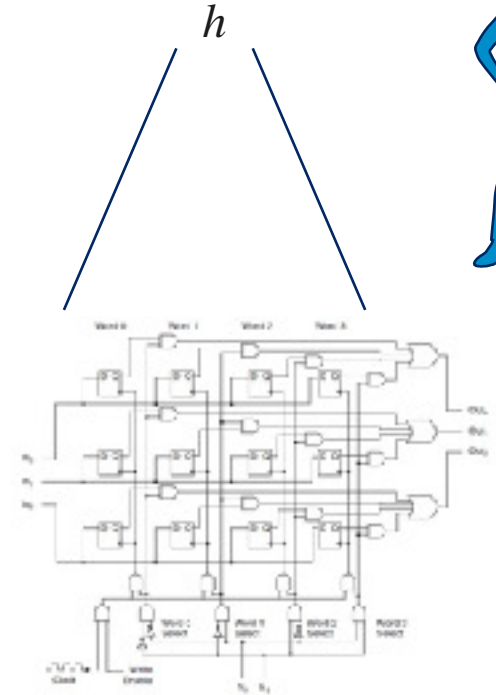
Learns nothing about x except $C(x)$



Laconic Function Evaluation [QWW18]



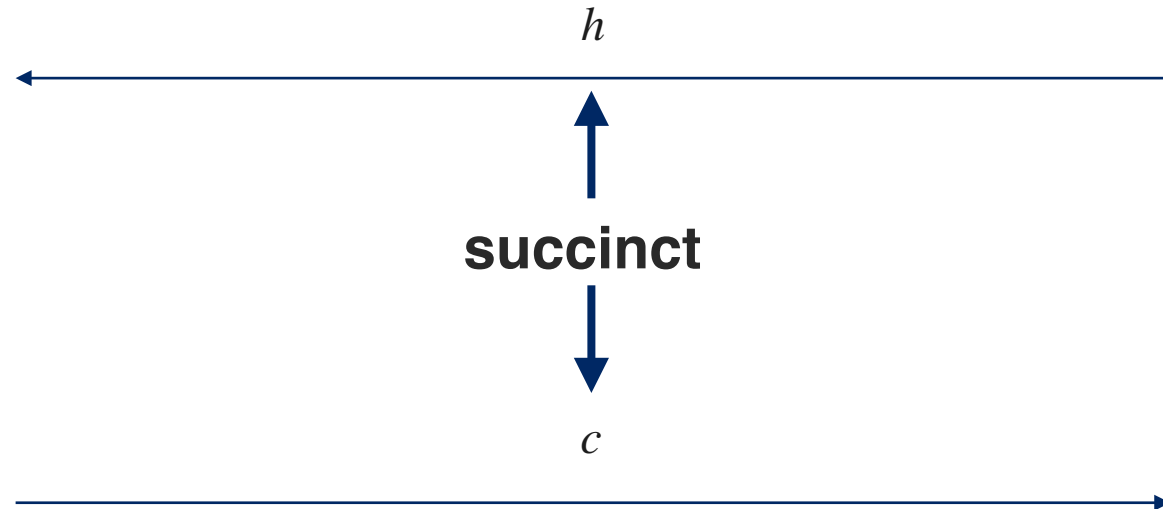
x



C

$y = Dec(C, c) = C(x)$

$c = Enc(h, x)$



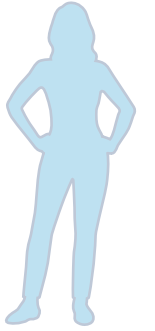
Learns nothing about x except $C(x)$



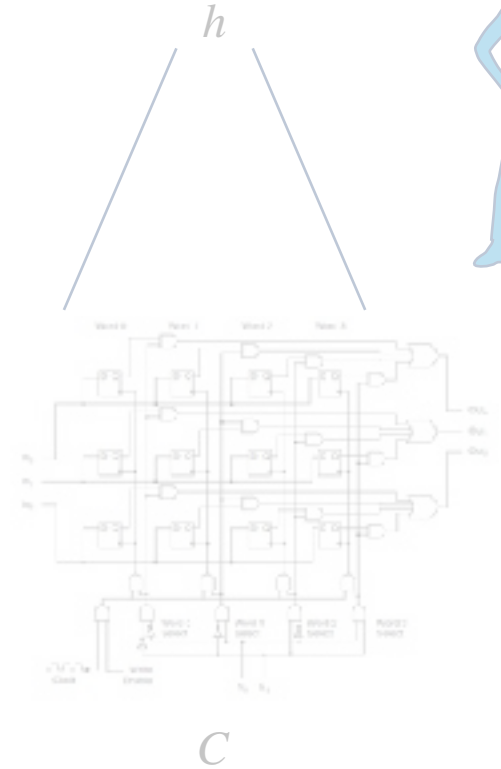
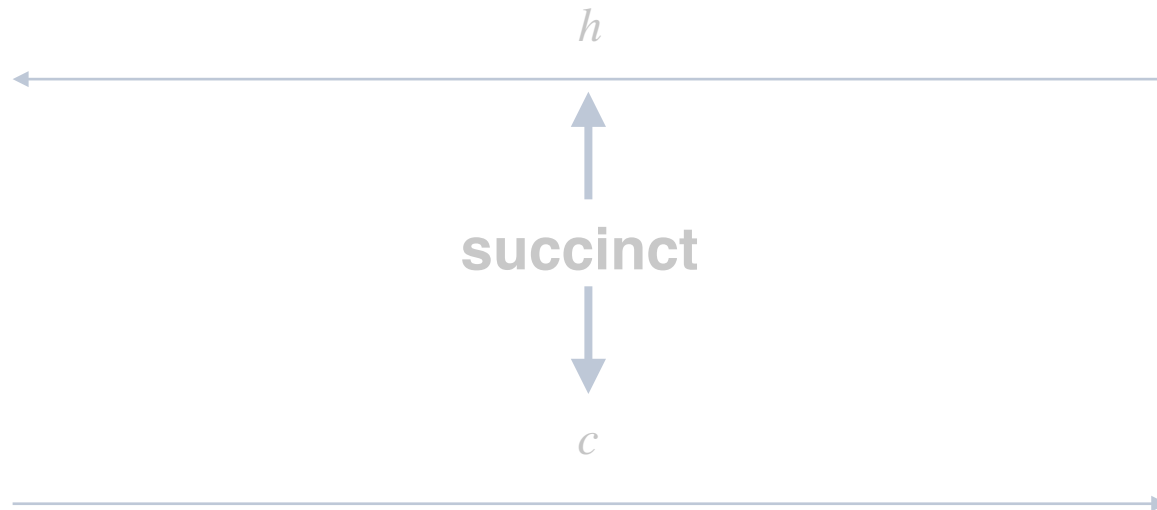
Laconic Function Evaluation [QWW18]



x



$$c = \text{Enc}(h, x)$$



$$y = \text{Dec}(C, c) = C(x)$$

Learns nothing about x except $C(x)$

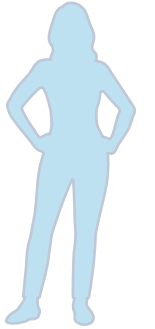


Laconic Function Evaluation [QWW18]

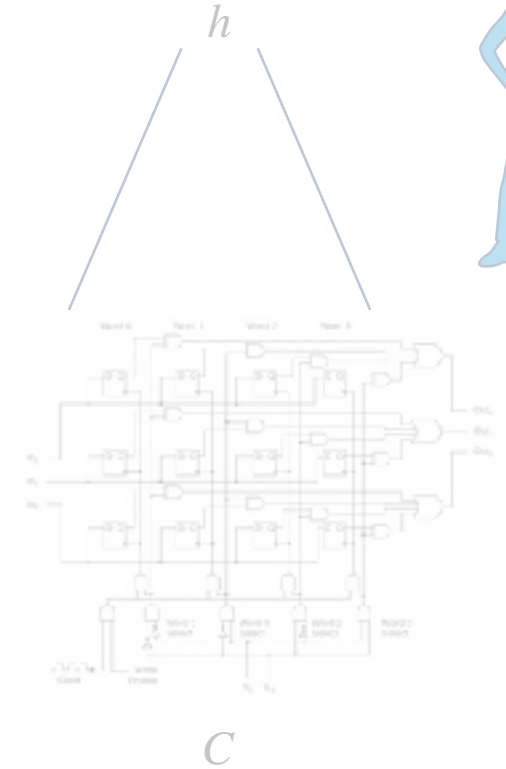
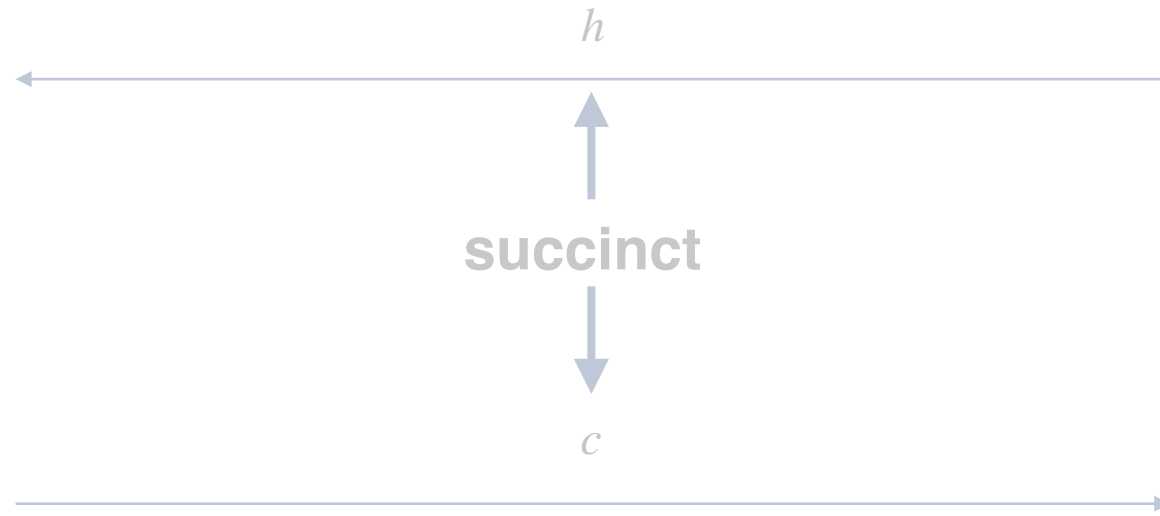


x

- Receiver commits to large function instead of database



$c = Enc(h, x)$



$y = Dec(C, c) = C(x)$

Learns nothing about x except $C(x)$



Laconic Function Evaluation [QWW18]



x

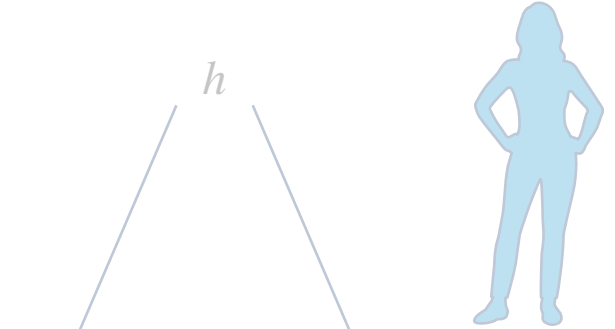
- Receiver commits to large function instead of database

- Laconic OT is a special case of LFE: Hashed function is selection function

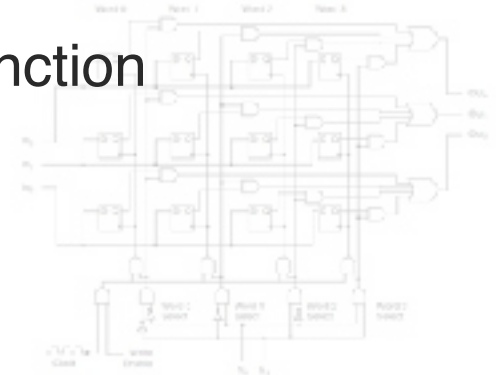
$c = Enc(h, x)$

succinct

c



h



C

$y = Dec(C, c) = C(x)$

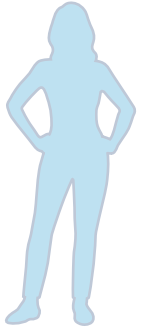
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Laconic Function Evaluation [QWW18]



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- Receiver commits to large function instead of database

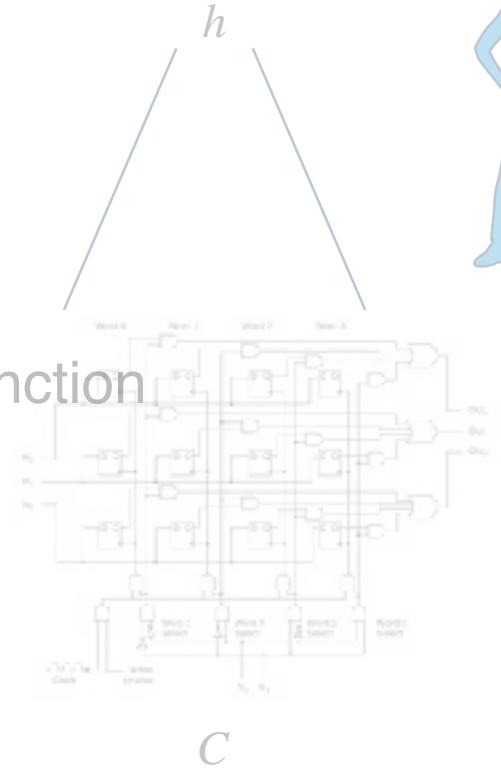
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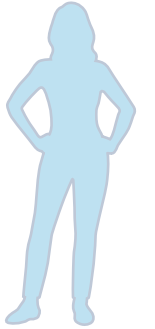
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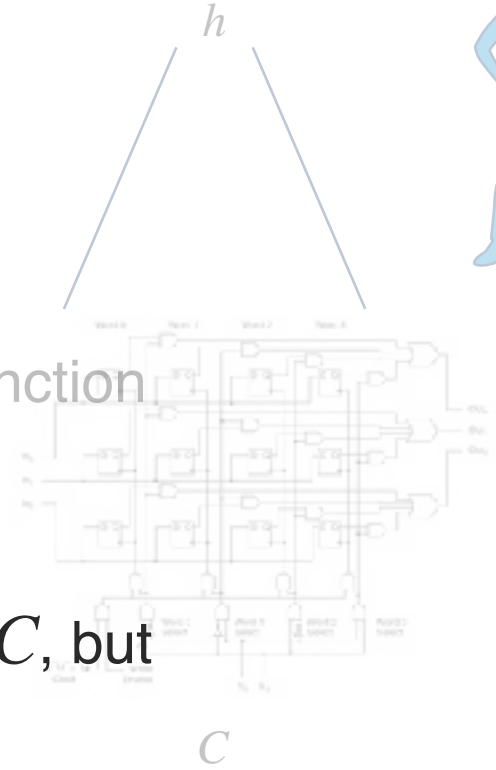


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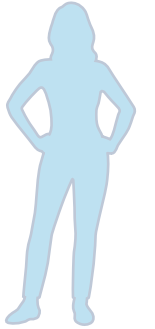
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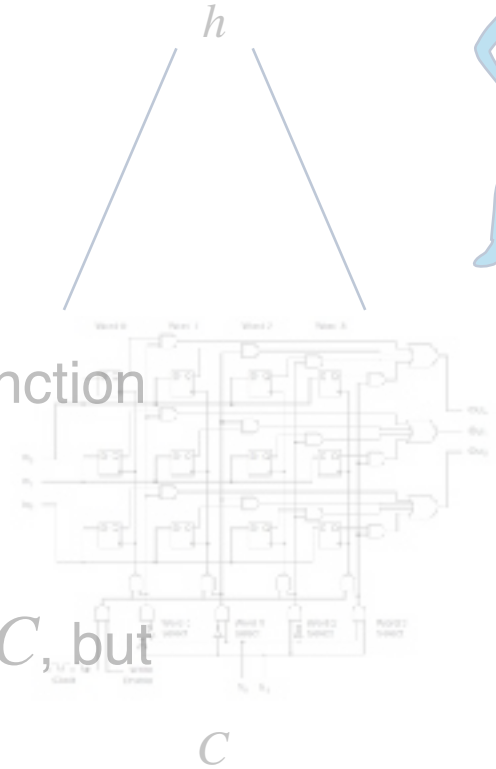


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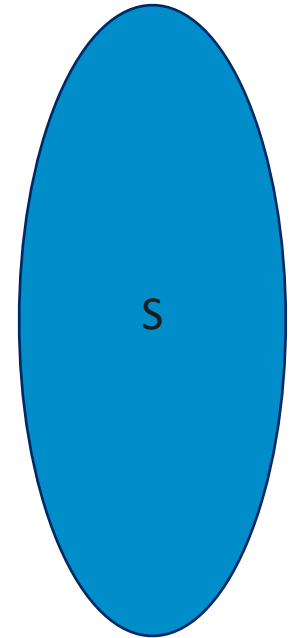
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Laconic Private Set Intersection (LPSI) [ABDGHP21]



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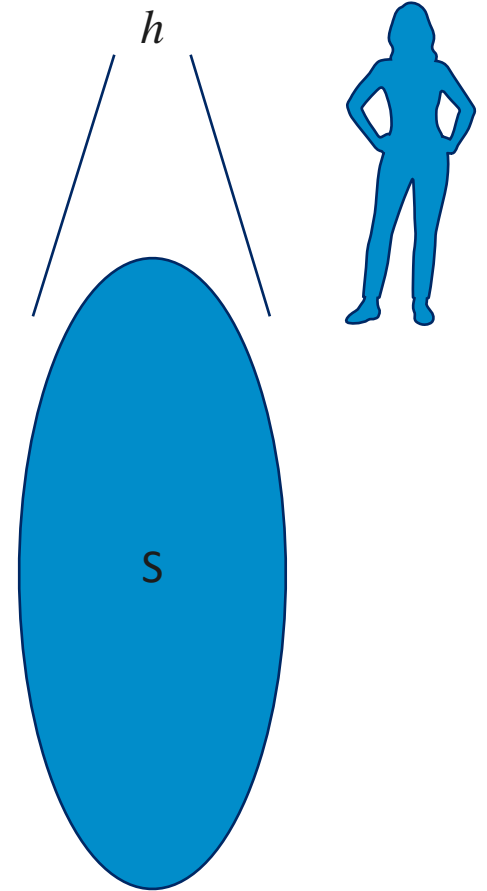




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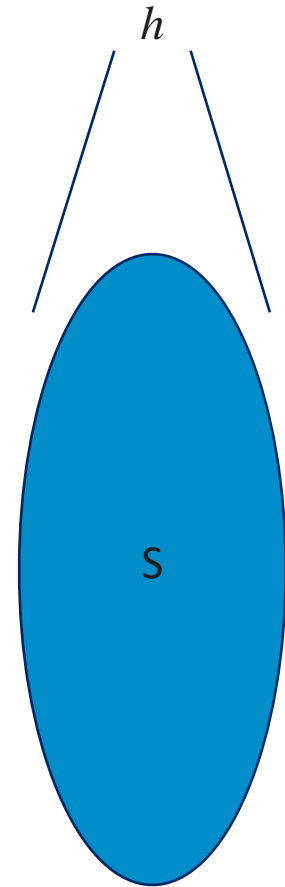
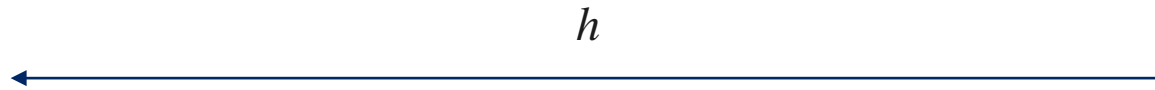




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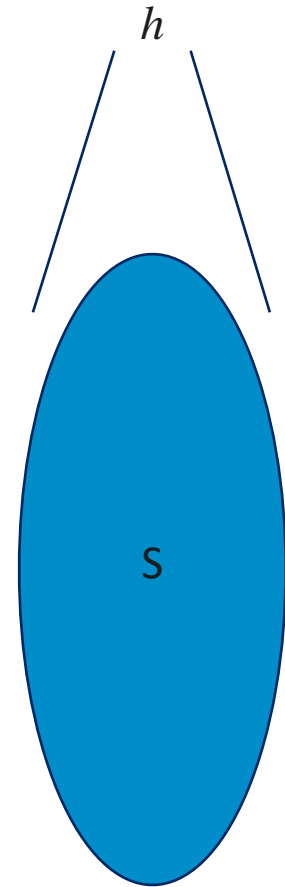


x

h



$$c = \text{Enc}(h, x)$$





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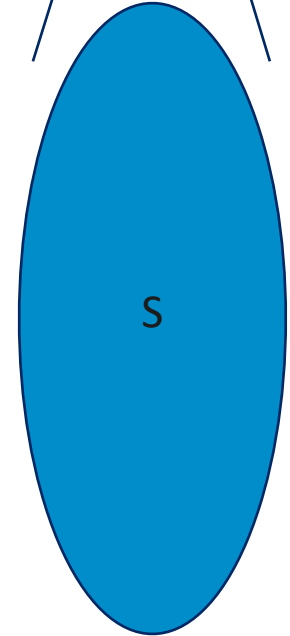


x

h



h



S

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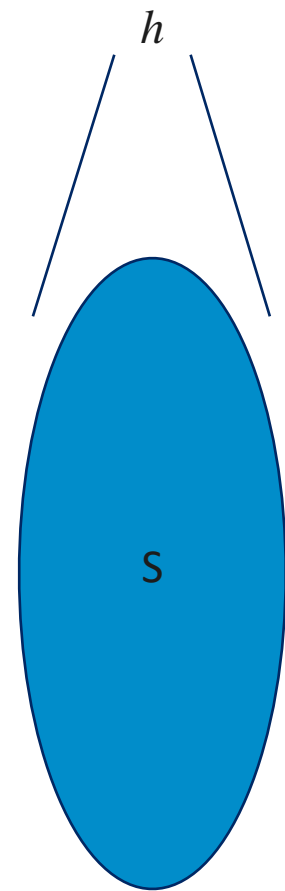
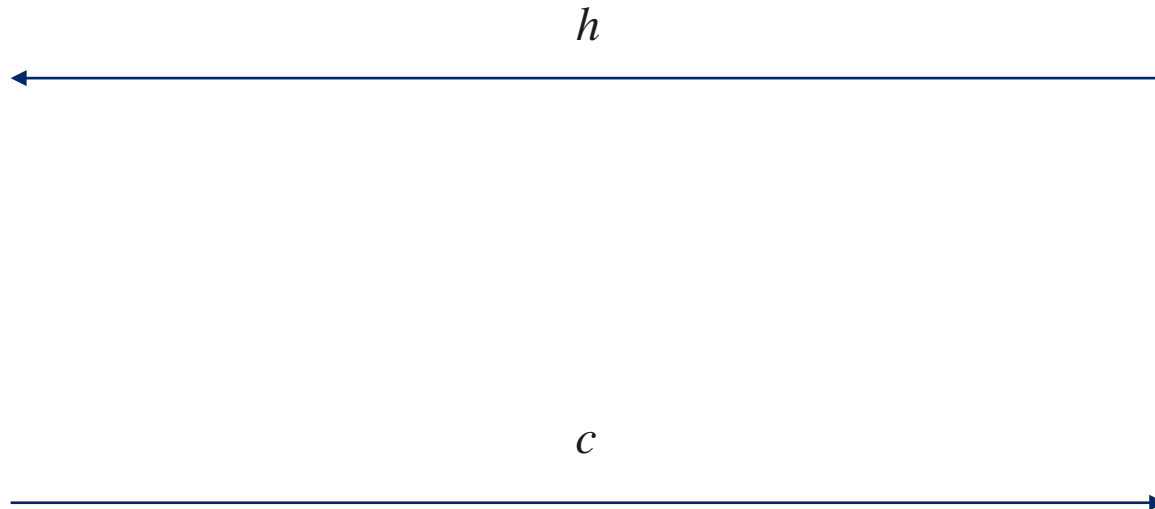


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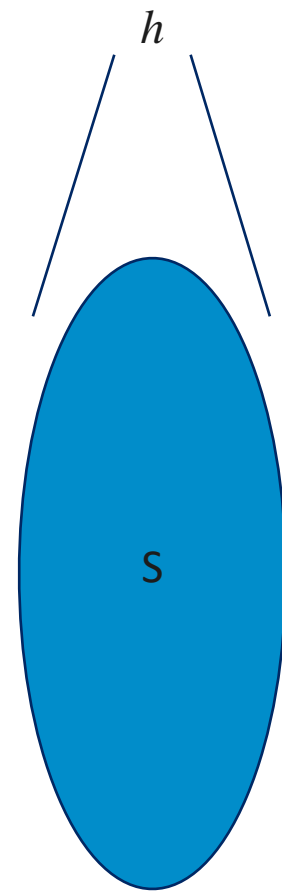
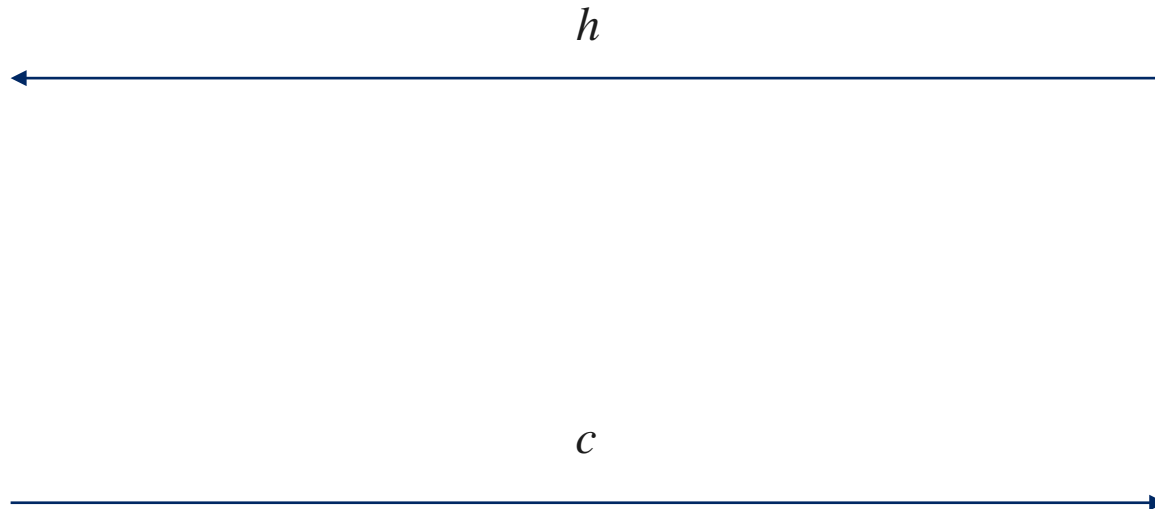


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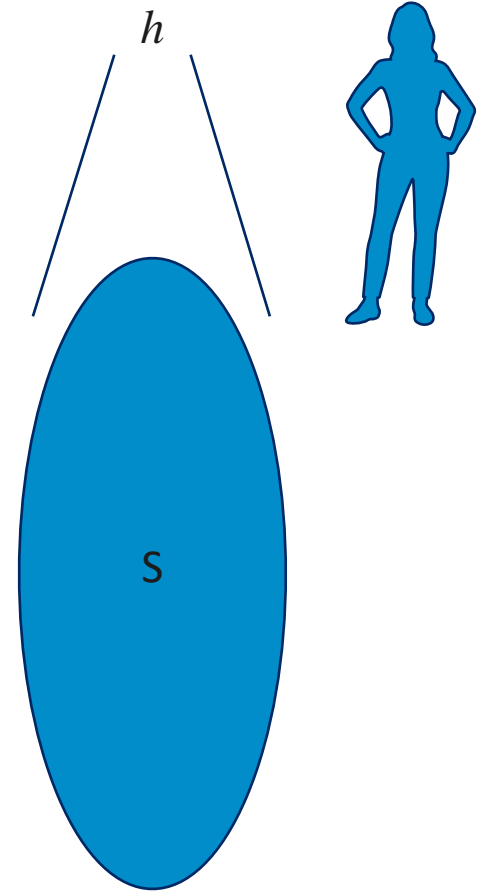
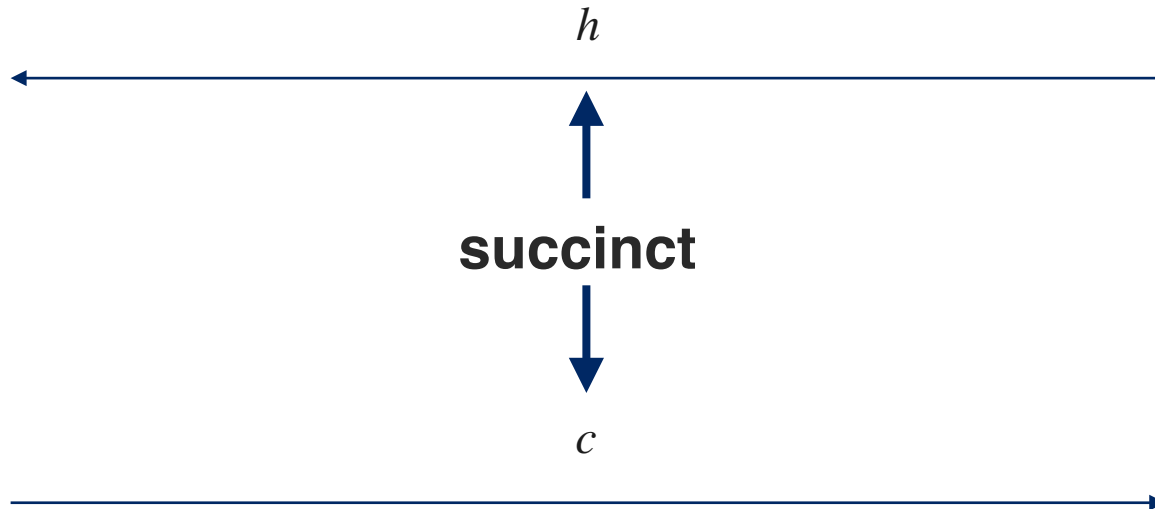


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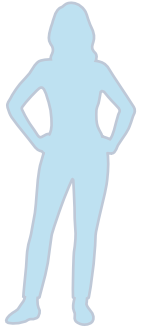
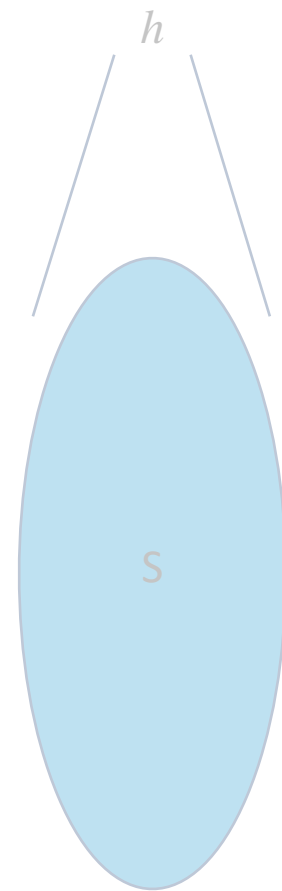
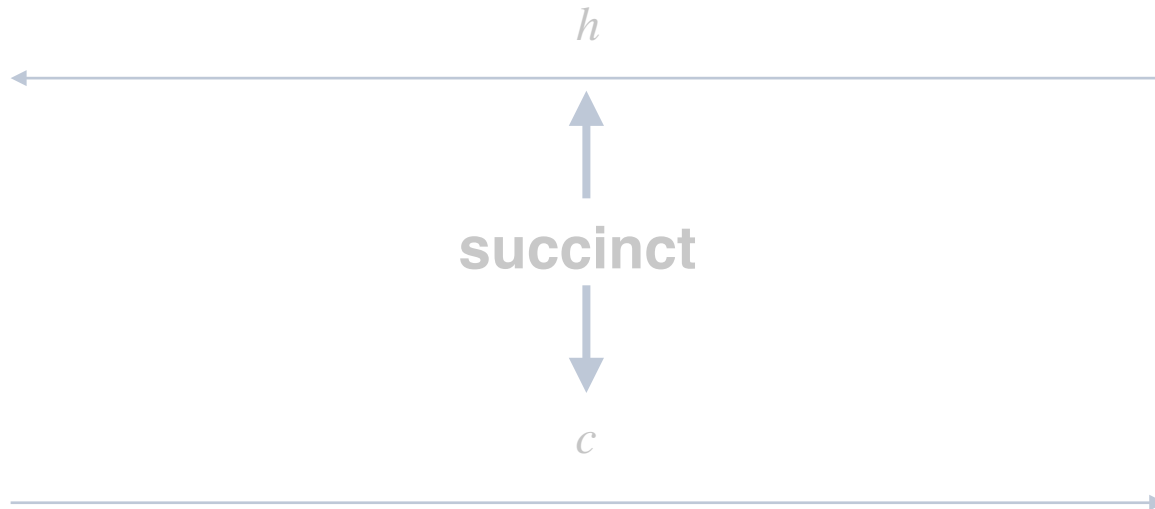


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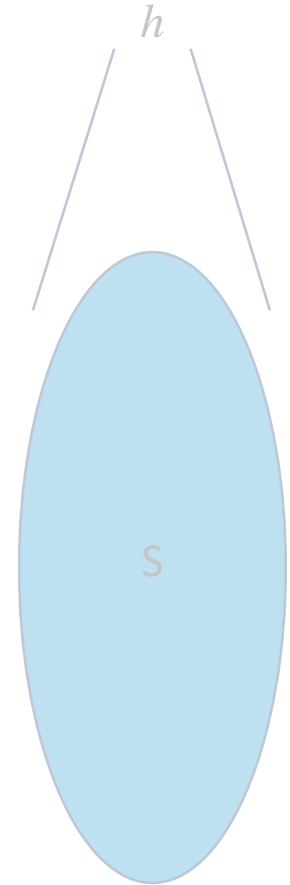
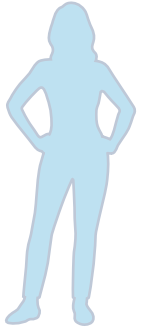
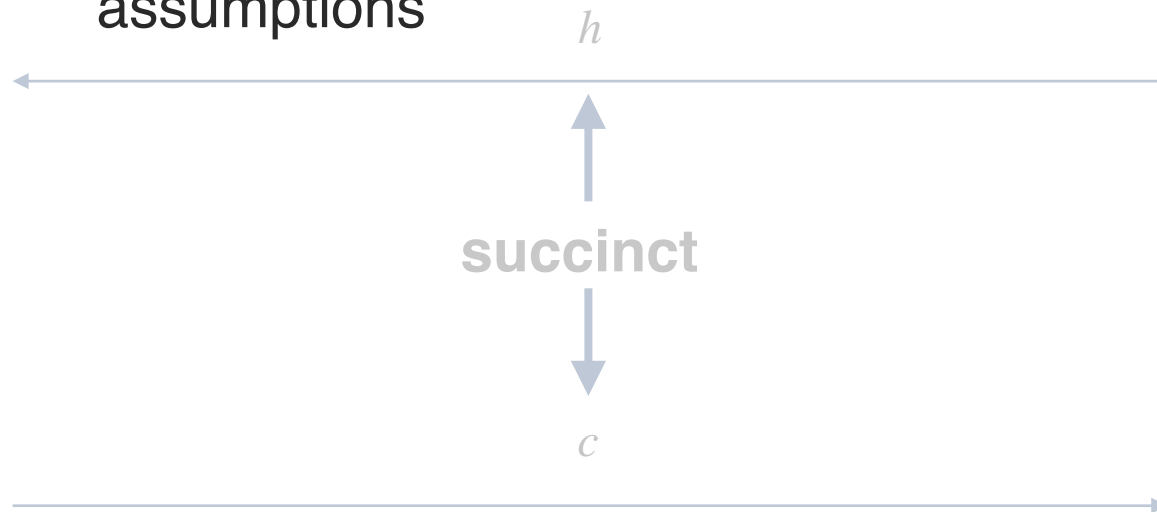
Laconic Private Set Intersection (LPSI) [ABDGHP21]



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- [ABDGHP21] provides an efficient black-box construction of LPSI from number-theoretic assumptions

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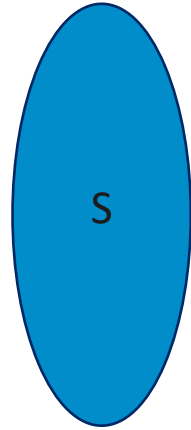


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Application of LPSI: Self-Revealing Encryption

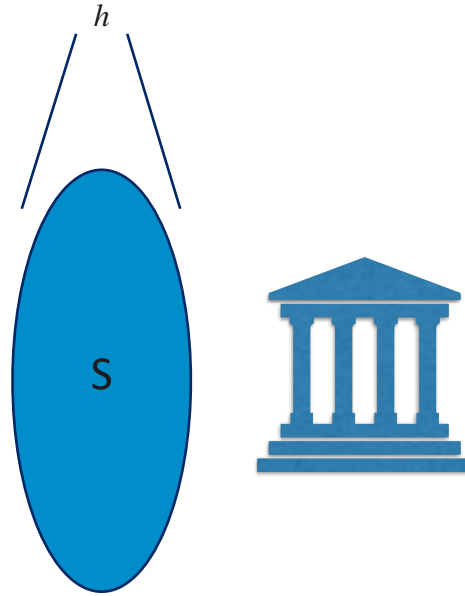


pk, sk





Application of LPSI: Self-Revealing Encryption

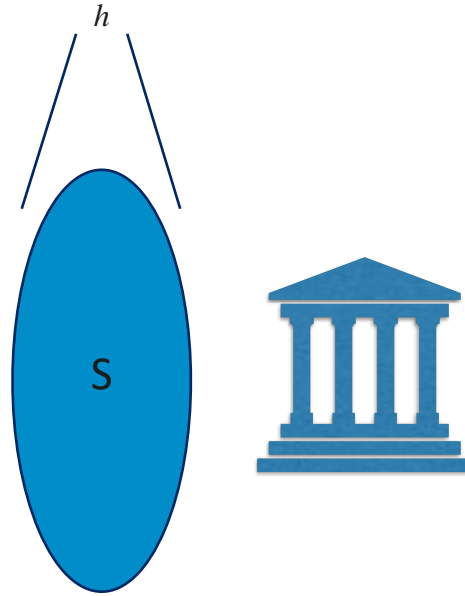


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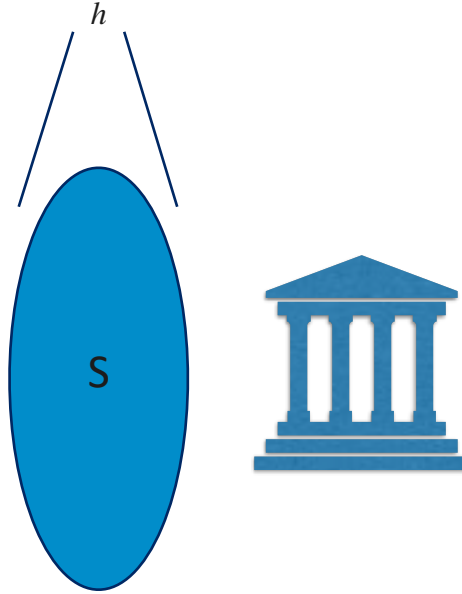
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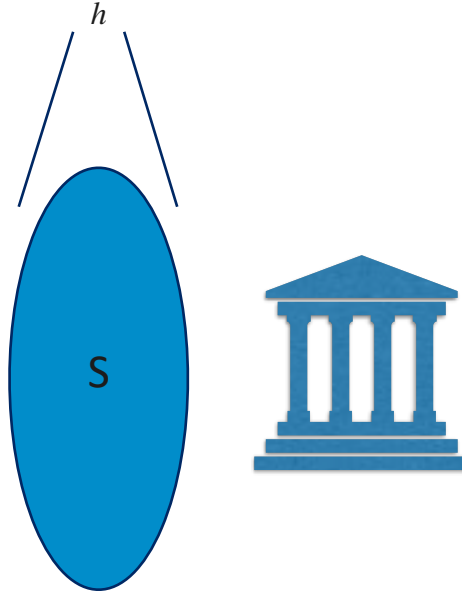
c



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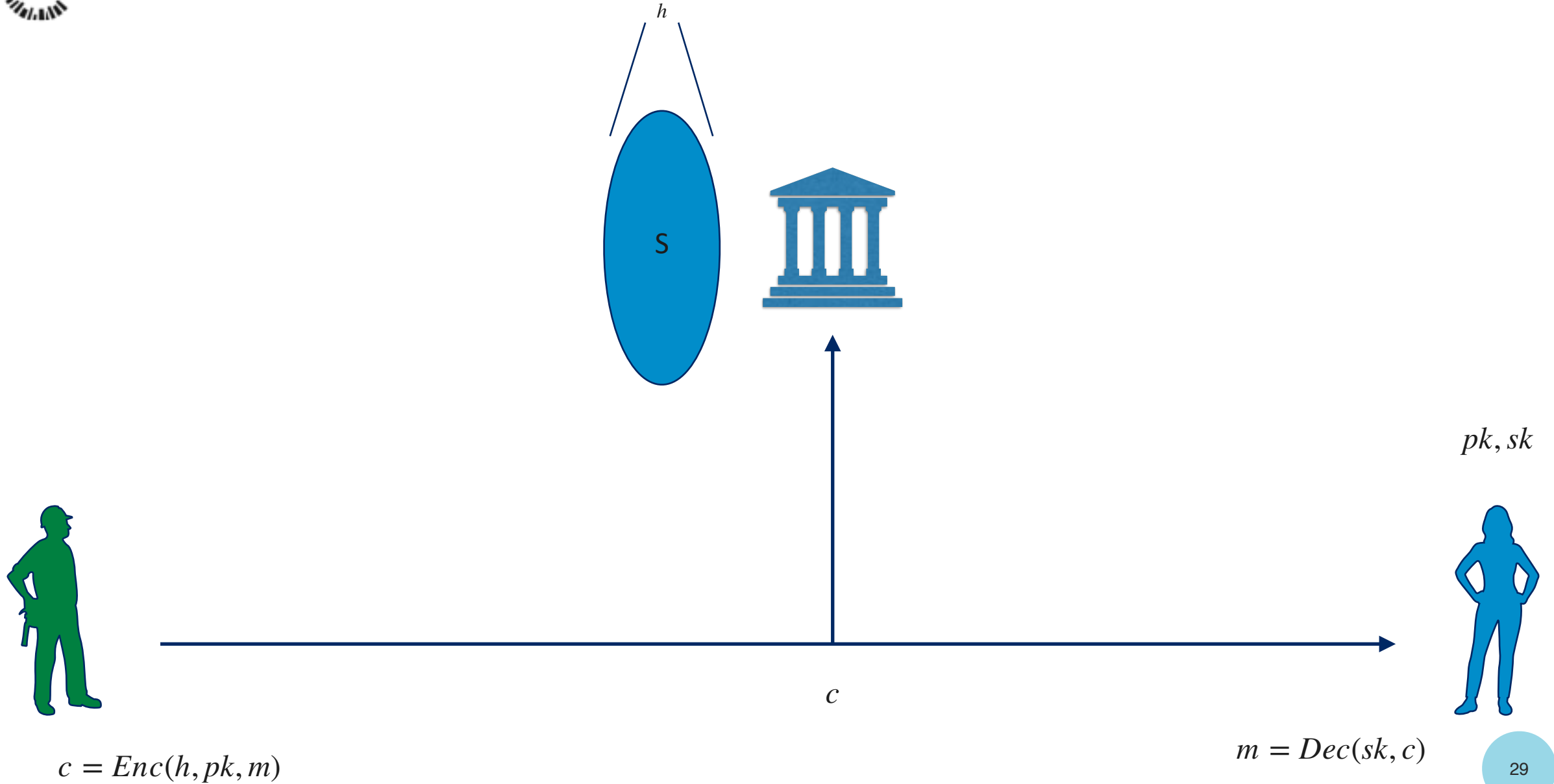


pk, sk

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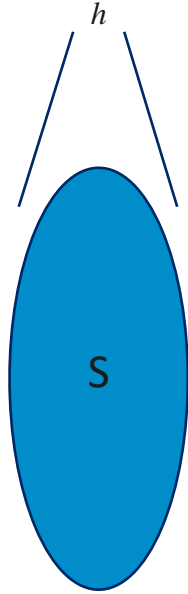


Application of LPSI: Self-Revealing Encryption





Application of LPSI: Self-Revealing Encryption



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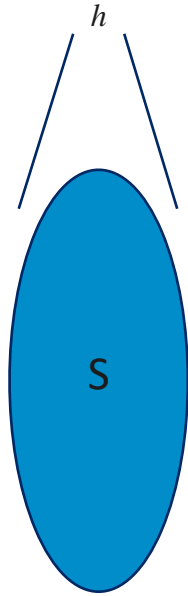


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Application of LPSI: Self-Revealing Encryption



- Can decrypt m if $m \in S$
- Otherwise learns nothing about m



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- [DKLLMR'22]: First Laconic Crypto Schemes **without** bootstrapping
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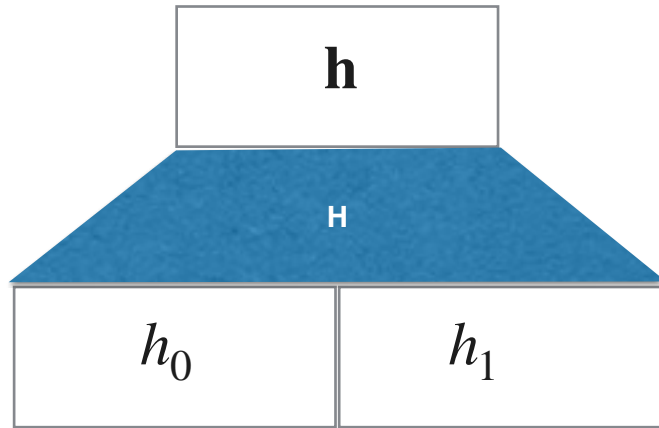
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- Applications: Registration-based Encryption, Laconic Oblivious Transfer, Private Set Intersection



Bootstrapping/Recryption

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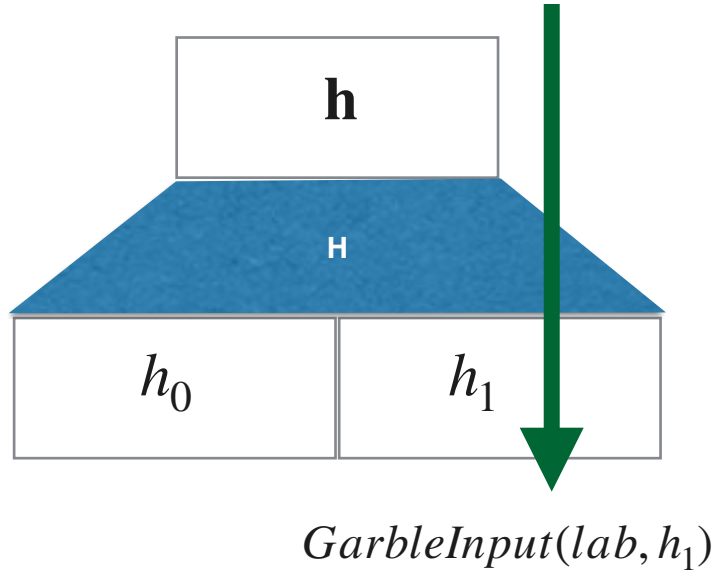


$\text{GarbleInput}(lab, h_1)$

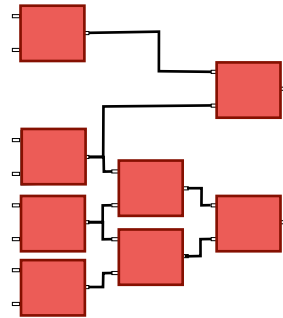


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GC

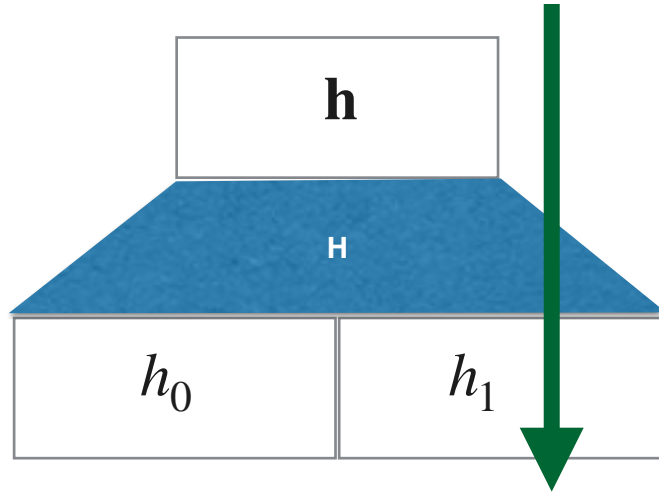


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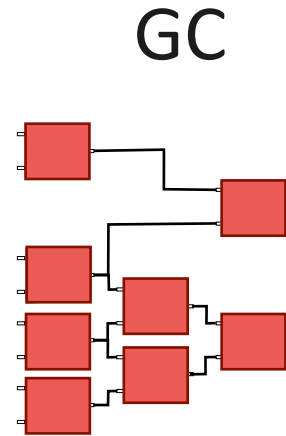


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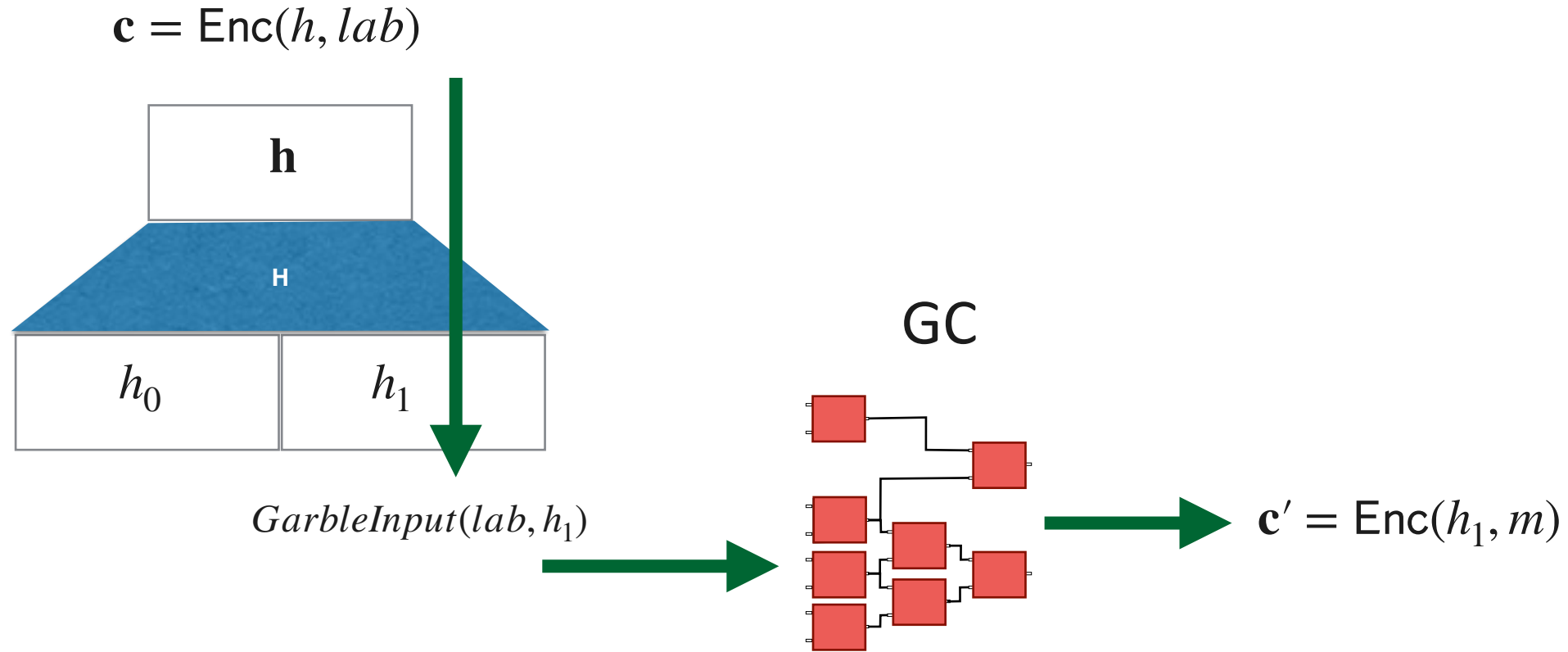
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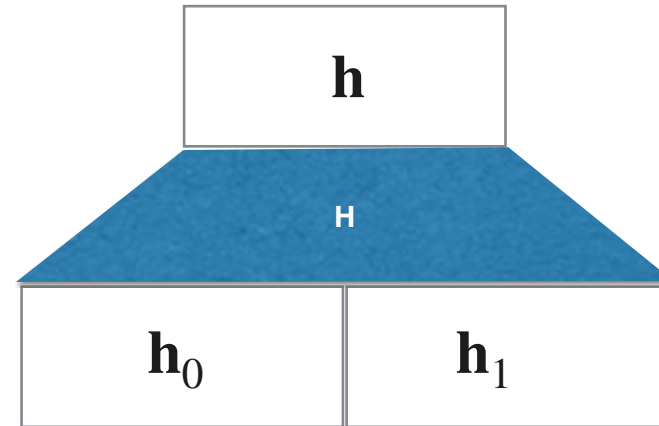


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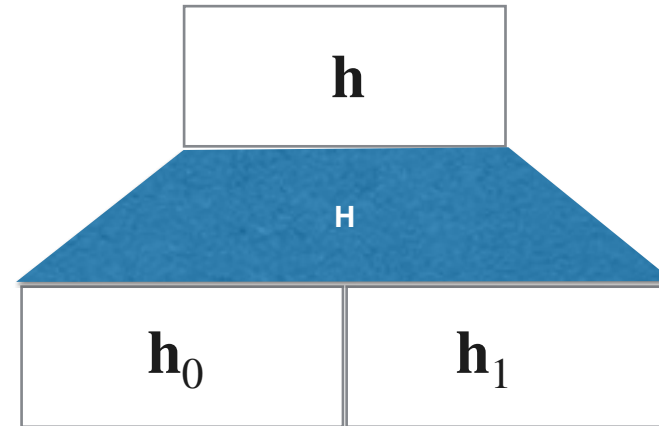
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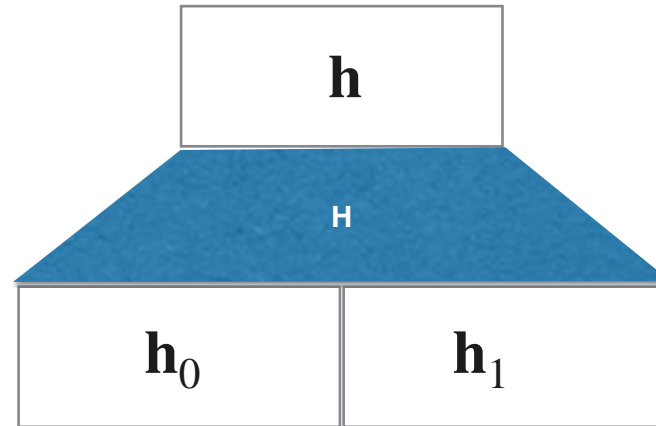
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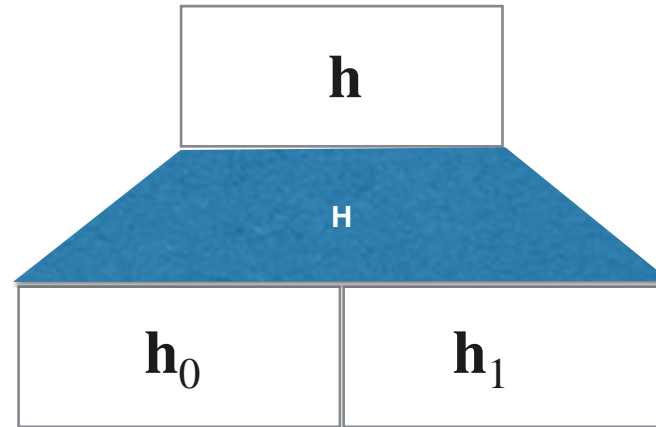
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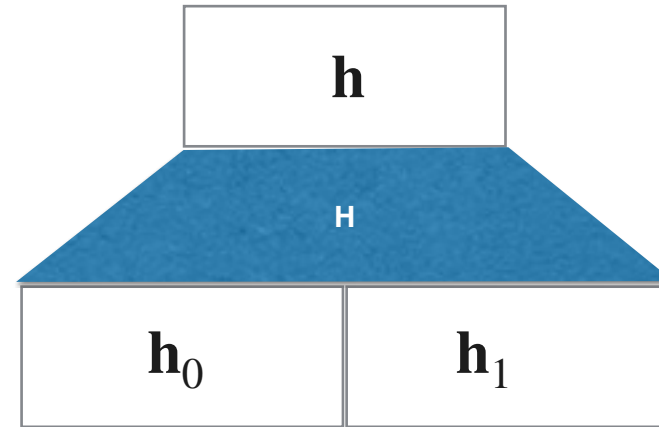
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$$c'_1 = c_1 - \mathbf{c} \begin{pmatrix} \mathbf{G}^{-1}(\mathbf{h}_0) \\ \mathbf{G}^{-1}(\mathbf{h}_1) \end{pmatrix} \approx \mathbf{s} \cdot \mathbf{h}_0 + \frac{q}{2}m$$



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- [DHMW24]: Private laconic OT (hiding query index i) and polylogarithmic decryption complexity
- Leverages recent breakthrough on doubly efficient private information retrieval [LMW23]



Private Laconic OT with Preprocessing



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- Very efficient, online phase uses only symmetric key crypto
- [BDHL24]: private laconic OT with preprocessing. Also only using symmetric key crypto in online phase



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- Beyond succinct communication: sublinear computation
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- Now: Breaking the wall to practical usefulness, new ideas such as preprocessing