

# Introduction to MPTS 2023

Presented\* on September 26<sup>th</sup> @ MPTS 2023 (Virtual)  
NIST Workshop on **M**ulti-**P**arty **T**hreshold **S**chemes 2023

Hosted by the Cryptographic Technology Group @ NIST  
**N**ational **I**nstitute of **S**tandards and **T**echnology

\* Luís Brandão (NIST/Strativia: Foreign Guest Researcher [non-employee] at NIST, contractor from Strativia).  
Expressed opinions are those of the speaker/author and should not be construed as official views of NIST.

# Outline

1. High-level context: MPTC, PEC, the Threshold Call
2. MPTS 2023 (schedule, topics, statistics)
3. Online resources

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## Two NIST-Crypto projects related to today's event

(i.e., projects in the Cryptographic Technology Group at NIST)

- ▶ **MPTC: “multi-party threshold cryptography”** (threshold schemes for crypto primitives)
- ▶ **PEC: “privacy-enhancing cryptography”** (advanced features/functionality)

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### The “Threshold Call” (from MPTC+PEC):

*NIST First Call for Multi-Party Threshold Schemes*

[see [NISTIR 8214C](#)] to gather **reference material** for public analysis ...  
aiming for **recommendations** (in a 1st phase), including about PEC.

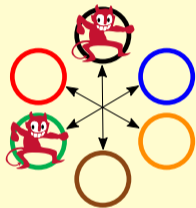
# NIST Call for Multi-Party Threshold Schemes

- ▶ NISTIR 8214C: Initial public **draft** (**Jan 2023**)  $\Rightarrow$  Revised version (**late 2023**).
- ▶ Submission deadline (expected  $\approx$  **2nd-half 2024**)

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**Calling for submissions of threshold schemes**



(And gadgets for modular use)

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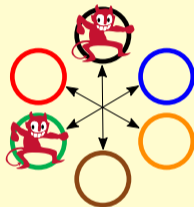
## Calling for submissions of threshold schemes for:

- ▶ **[Cat1] Selected NIST-standardized primitives**
- ▶ **[Cat2] Other primitives (including FHE, IBE/ABE, ZKP)**  
(And gadgets for modular use)

FHE = Fully-homomorphic encryption.

IBE/ABE = Identity/Attribute-based encryption.

ZKP = Zero-knowledge proof.





## Main components of a submission package

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Check	#	Item
<input type="checkbox"/>	M1	Written specification (S1–S16)
<input type="checkbox"/>	M2	Reference implementation (Src1–Src4)
<input type="checkbox"/>	M3	Execution instructions (X1–X7)
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The revised version of the call will detail better each **component**.

A submission package can propose various **objects** (schemes/gadgets).

Each **component** will then map all such **objects**.

## Selected notes about the “Threshold Call”

1. It has a **wide scope** of subcategories for submission (next slides)
2. Enables an **exploration** of advanced cryptography, before promising standards
3. The initial process will devise **recommendations** for subsequent processes
4. Both **post-and-pre quantum** primitives are in scope.
5. **Active security** is required, though open to diverse security formulations.
6. **Modularity** is strongly encouraged (gadgets)
7. Community **participation** is essential (feedback; submissions; analyses)

## Category Cat1 of NIST Call for Multi-Party Threshold Schemes

Subcategory: Type	Families of specifications
C1.1: <b>Signing</b> (preQ)	EdDSA sign, ECDSA sign, RSADSA sign
C1.2: <b>PKE</b> (preQ)	RSA decrypt, RSA encrypt (a secret value)
C1.3: <b>2KA</b>	ECC-CDH, ECC-MQV
C1.4: <b>Symmetric</b>	AES encipher/decipher, KDM/KC (for 2KE)
C1.5: <b>Keygen</b>	ECC keygen, RSA keygen, bitstring keygen

Too many acronyms, we know. Legend: 2KA: pair-wise key-agreement. 2KE: pair-wise key-establishment. AEAD = Authenticated Encryption with Associated Data. AES: Advanced Encryption Standard. CDH: cofactor Diffie-Hellman. DSA = Digital Signature Algorithm. ECC: Elliptic-curve cryptography (or, if used as an adjective, EC-based). ECDSA: Elliptic-curve Digital Signature Algorithm. EdDSA: Edwards-curve Digital Signature Algorithm. Elliptic-curve based Key-Establishment. KC: Key-confirmation. KDM: Key-derivation mechanism. KEM: Key-Encapsulation Mechanism. Keygen: Key-generation. ML = Module Lattice. MQV: Menezes-Qu-Vanstone. PKE: public-key encryption. postQ: Post-Quantum. preQ: Pre-Quantum. RSA: Rivest-Shamir-Adleman (signature and encryption schemes). RSADSA: RSA digital signature algorithm. SLH = StateLess hash. XOF = extendable Output Function. Note: In the 2nd column, each item within a subcategory is itself called a family of specifications, since it may include diverse primitives or modes/variants.

## Category Cat1 of NIST Call for Multi-Party Threshold Schemes

Subcategory: Type	Families of specifications
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C1.2: <b>PKE</b> (preQ) (postQ)	RSA decrypt, RSA encrypt (a secret value) ML-KEM
C1.3: <b>2KA</b>	ECC-CDH, ECC-MQV
C1.4: <b>Symmetric</b>	AES encipher/decipher, KDM/KC (for 2KE) [upcoming] (“lightweight”) ASCON-related AEAD and XOF
C1.5: <b>Keygen</b>	ECC keygen, RSA keygen, bitstring keygen

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# Category Cat2 of the NIST “Threshold” Call

TF = threshold friendly. QR = quantum resistant.

Subcategory: Type	Example types of schemes	Example primitives
C2.1: <b>Signing</b>	TF succinct & verifiably-deterministic signatures	Sign
	TF-QR signatures	Sign
C2.2: <b>PKE</b>	TF-QR public-key encryption (PKE)	Decrypt/Encrypt (a secret value)
C2.3: <b>Key-agreem.</b>	TF Low-round multi-party key-agreement	Single-party primitives
C2.4: <b>Symmetric</b>	TF blockcipher/PRP	Encipher/decipher
	TF key-derivation / key-confirmation	PRF and hash function
C2.5: <b>Keygen</b>	Any of the above	Keygen

**Note:** While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

**Legend:** agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

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C2.4: <b>Symmetric</b>	TF blockcipher/PRP	Encipher/decipher
	TF key-derivation / key-confirmation	PRF and hash function
C2.5: <b>Keygen</b>	Any of the above	Keygen
C2.6: <b>Advanced</b>	TF-QR fully-homomorphic encryption	Decryption; Keygen
	TF identity-based and attribute-based encryption	Decryption; Keygens
C2.7: <b>ZKPoK</b>	Zero-knowledge proof of knowledge of private key	ZKPoK.Generate
C2.8: <b>Gadgets</b>	Garbled circuit (GC)	GC.generate; GC.evaluate

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## Why this workshop (MPTS 2023)

**Community feedback and participation are essential!**

Thank you in particular (speakers and attendees) for joining MPTS 2023

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## What is MPTS 2023?

- ▶ “NIST Workshop on Multi-Party Threshold Schemes 2023”
- ▶ 3 half-days;  $\approx$  30 talks;  $\approx$  300 registered attendees

# MPTS 2023 Schedule of Sessions

Date	Session	Time	Session title	# talks
Sep. 26th	—	10:00–10:20	Welcome/Intro to MPTS 2023	—
	<b>1a</b>	10:20–12:00	Generic considerations on MPC/MPTC	4
	<b>1b</b>	13:00–15:00	Threshold Signatures over Elliptic Curves	5
Sep. 27th	<b>2a</b>	10:00–12:00	FHE+ZKP+ABE	5
	<b>2b</b>	13:00–14:00	More on Threshold Signatures	3
	<b>2c</b>	14:00–15:00	NIST Standards	4
Sep. 28th	<b>3a</b>	10:00–11:40	Some Gadgets	4
	<b>3b</b>	11:40–12:00	Focused Feedback	—
	<b>3c</b>	13:00–14:50	More Gadgets	5
	—	14:50–15:00	Concluding remarks	—

**Legend:** ABE = Attribute-based encryption. FHE = Fully-homomorphic encryption. MPC = (Secure) Multiparty Computation. MPTC = Multi-party threshold cryptography. MPTS = Multi-party threshold schemes. NIST = National Institute of Standards and Technology. Sep. = September. ZKP = Zero-knowledge proof.

**Event details:** <https://csrc.nist.gov/events/2023/mpts2023>

**Contact email:** [workshop-mpts2023@nist.gov](mailto:workshop-mpts2023@nist.gov)

# Suggested Topics in the Call for Presentations

1. **Scope of the Threshold Call:** refinements to the description of subcategories.
2. **Submission requirements** in the Threshold Call: needed clarifications.
3. **Expressions of interest:** intended concrete submissions (and possible submitter team).
4. **Need and adoptability:** special features and primitives useful for specific applications.
5. **Inspiration:** suggestions to the community, for submission of concrete threshold schemes.
6. **Frameworks:** pertinent system models, security formulations, and threshold parameters.
7. **Pre/post quantum:** concrete pre-quantum versus post-quantum cases worth focusing on.
8. **Technicalities:** challenges about concrete primitives / threshold schemes / assumptions.
9. **External efforts:** other processes developing related reference material or specifications.

# Video-conference Webinar (registrations and logistics)

▶ **Virtual registrations:** 304\*

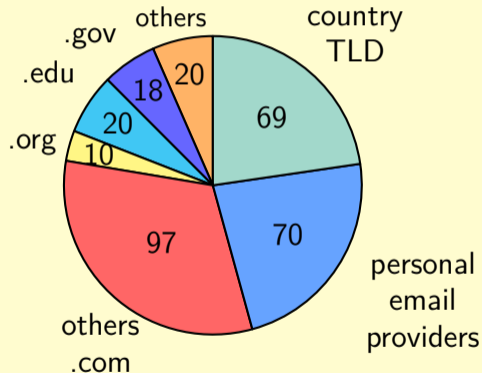
(Not counting speakers and hosts)

**Across 40 countries:** US (124); IN (25); FR (17); CA (16), DE (11), UK (11), IL (9), CN (8), ...

▶ **Audio and video:** being recorded (posting will be announced in the PEC and MPTC forums)

▶ **Questions:** Attendees can use the virtual Q&A (to be considered as time permits)

**Per registered email address:**



Registrations for 1st day of webinar, as of 8am EDT. Actual number is expected to increase until the workshop starts, and thereafter. Legend: CA = Canada; CN = China; DE = Germany; FR = France; IL = Israel; IN = India; Q&A = Questions and answers; TLD = top-level domain; UK = United Kingdom; US = United States.

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**Thank you for your attention!**

***Introduction to MPTS 2023:***

September 26<sup>th</sup> @ Virtual

We appreciate followup comments: [workshop-mpts2023@nist.gov](mailto:workshop-mpts2023@nist.gov)



MPTS 2023  
(Sept. 26–28)



Threshold Call  
(Draft)



MPTC-Forum  
(email list)



PEC-Forum  
(email list)