

# DISE: DISTRIBUTED SYMMETRIC-KEY ENCRYPTION

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# Threshold Crypto

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- Has focused on public-key crypto
- Symmetric-key encryption got less attention
  - Symmetric keys don't stay around long
- Secure communication over internet (TLS)
  - Signing keys are long-term
  - Encryption keys change with every session

# Symmetric-key Encryption (SKE)

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- Encrypt data at rest
  - AWS, MS Azure, Google Cloud provide client-side, server-side, disk encryption
  - Keys managed by cloud service or client
- Authentication on web, enterprises, ...
  - JSON web tokens, TGT in Kerberos, etc.
- Securing PIN in credit/debit transactions

# Threshold SKE

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- Threshold PRFs [MS95, NPR99, Nie02, Dod03, DY05, DYY06, BLMR13]
- MPC: Evaluate AES-GCM [DK10, GRRSS16, RSS17]
  - Good: Backward-compatibility, standard schemes
  - Bad:
    - Communication complexity linear in circuit size, number of parties
    - All parties interact with each other

Build a threshold SKE that works well in practice:

- Fast encryption/decryption
- Requires minimal interactivity
- Provides strong security guarantees

# Our Contributions

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- Formally study threshold SKE
  - Message privacy & ciphertext integrity in the distributed setting
- Simple and light-weight protocols
  - Initiator sends one message, gets one message (challenge-response style)
  - Support arbitrary threshold  $t$ 
    - Contact  $t-1$  other parties
    - Resilient to  $t-1$  corruption
- Implement & evaluate
  - A million enc/dec per second, sub millisecond latency with upto 18 parties

# Outline

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- Security properties
- DiSE: main protocol
- Implementation
- Future work

# Threshold SKE

# Notation & Model

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- $n$  – total number of parties
- Initiator: Party who initiates an enc/dec session
- $t$  – threshold
  
- Attack model
  - Corrupt  $t-1$  parties maliciously
  - Static model
  
- Communication model: Point-to-point secure channels

# Traditional vs Modern

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- Inspired by traditional game-based notions [BN00, KY01, RS06]
- More advanced notions studied for non-threshold [Rog02, RS06, FFL12, PW12 Rog13, GL15, HRRV15, HKR15, BT16, BHT18]
- Extending traditional notions to threshold already non-trivial

# Protocols

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- **Setup**  $(n, t) \rightarrow (sk_1, sk_2, \dots, sk_n), pp$
- **DistEnc**  $(j, msg, S) \rightarrow ctxt$ 
  - Parties involved don't learn ciphertext
- **DistDec**  $(j, ctxt, S) \rightarrow msg$ 
  - Parties involved don't learn message
- Consistency (all parties honest):
  - DistEnc  $(j, msg, S) \rightarrow ctxt$
  - DistDec  $(j^*, ctxt, S^*) \rightarrow msg$

# Correctness

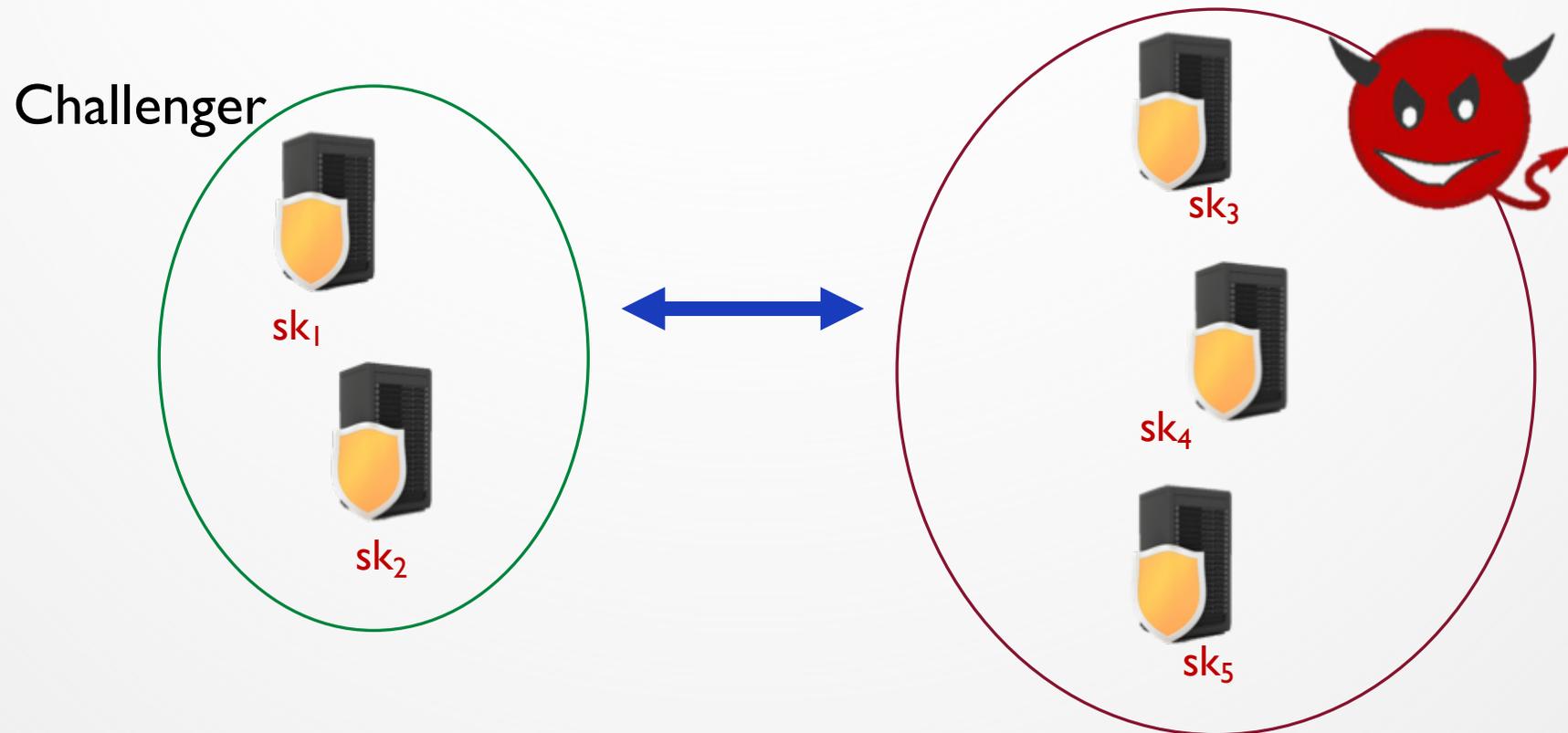
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- DistEnc session fails even if initiated by honest party
- DistEnc succeeds but DistDec fails
- **Basic:** *if* DistEnc ( $msg$ )  $\rightarrow$   $ctxt \neq \perp$ , *then* DistDec ( $ctxt$ )  $\rightarrow$   $msg$  or  $\perp$
- **Strong:** *if* DistEnc ( $msg$ )  $\rightarrow$   $ctxt \neq \perp$ , *then* DistDec ( $ctxt$ )  $\rightarrow$   $msg$  if parties honest

# Security Games

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- Message privacy & ciphertext integrity
- Games between Challenger *Chal* and Adversary *Adv*



# Message Privacy

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- Ciphertexts do not reveal message
- Non-threshold:  $\text{Enc}(m_0) \approx \text{Enc}(m_1)$
- Adv is allowed to:
  - Encryption: Initiated by corrupt/honest party
  - Decryption: Initiated by honest party
- Challenge: Adv outputs  $(j, m_0, m_1, S)$

# Ciphertext Integrity (Authenticity)

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- New valid ciphertexts cannot be generated
- Non-threshold: Can keep track of ciphertexts
- **C** – set of corrupt parties
- $g = t - |C|$
- **cnt** – count #messages Adv sends to honest parties
- **L** – list of ciphertexts

# Ciphertext Integrity (Authenticity)

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- Variables:  $C, g, cnt, L$
- Adv allowed to:
  - **(Encryption,  $j, msg, S$ )**
    - $j$  is corrupt: increment  $cnt$  by #honest parties in  $S$
    - $j$  is honest: add  $ctxt$  to  $L$
  - **(Decryption,  $j, ctxt, S$ )**
    - $j$  is corrupt: increment  $cnt$  by #honest parties in  $S$
  - **(Targeted Decryption,  $j, k, S$ )** with  $j$  honest
- Maximum ciphertexts:  $cnt / g$  (rounded down)

Counter incremented

The diagram consists of three red callout boxes with white text. The top box, labeled 'Counter incremented', has two lines pointing to the 'j is corrupt' bullet points under the 'Encryption' and 'Decryption' sections. The bottom box, labeled 'Decryption!!', has one line pointing to the 'j is corrupt' bullet point under the 'Decryption' section.

Decryption!!

# Ciphertext Integrity (Authenticity)

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- Forgery: Adv outputs  $(j_1, S_1, \text{ctxt}_1), (j_2, S_2, \text{ctxt}_2), \dots, (j_k, S_k, \text{ctxt}_k)$
- Adv wins if:
  - $k > \text{cnt} / g$
  - Dec sessions output valid messages
- **Basic**: Dec sessions are honest
- **Strong**: Corrupt parties can misbehave

# Summary

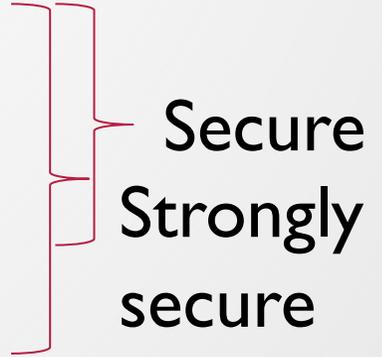
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- Correctness: Basic & Strong
- Message privacy
- Ciphertext integrity: Basic & Strong

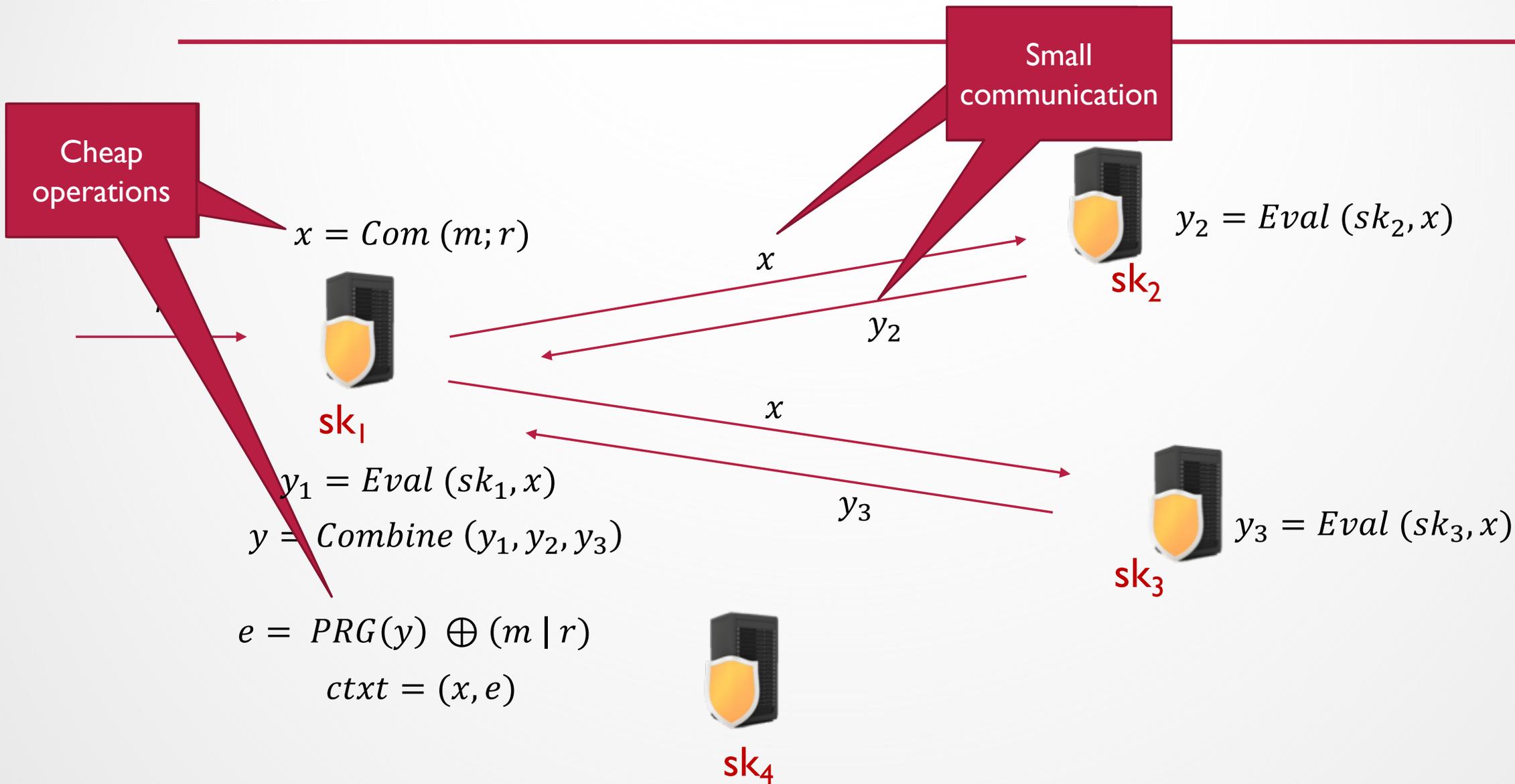
# DiSE: Threshold SKE Scheme

# Distributed PRF (DPRF)

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- Introduced by Naor et al. [NPR99]
  - Several constructions/variations [Nie02, Dod03, DY05, DYY06, BLMR13]
  - **Setup**  $(n, t) \rightarrow (sk_1, sk_2, \dots, sk_n)$
  - **Eval**  $(sk_j, x) \rightarrow y_j$
  - **Combine**  $(y_1, y_2, \dots) \rightarrow y$
  - *Consistency*: Same output irrespective of the set
  - *Pseudorandomness*: Final output should be pseudorandom
  - *Correctness*: Final output either correct or  $\perp$
- 
- Secure  
Strongly  
secure

# DiSE



# Security

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- If DPRF is (strongly) secure, then DiSE satisfies
  - (strong) correctness
  - message-privacy
  - (strong) ciphertext-integrity

# DPRF instantiations [MS95, NPR99]

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- DDH assumption (ROM)
  - Setup  $(n, t) \rightarrow (sk_1, sk_2, \dots, sk_n)$
  - Eval  $(sk_j, x) \rightarrow \text{Hash}(x)^{sk_j}$
  - DPRF  $(x) = \text{Hash}(x)^{sk}$
- Any PRF like AES
  - Setup  $\rightarrow$  Exponential number of keys
  - DPRF  $(x) = \text{PRF}_{k_1}(x) \oplus \text{PRF}_{k_2}(x) \oplus \text{PRF}_{k_3}(x) \oplus \dots$

# Compare

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	DDH	PRF
Choice of $n, t$	Arbitrary	${}^n C_t$ should be small
Type of operations	Expensive public-key	Cheap symmetric-key
Strong security	Easy	Difficult
Change of $n, t$	Master key unaffected	Master key affected

# Implementation & Evaluation

# Implementation

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- Three instantiations: PRF, DDH, DDH-NIZK
- Tested on many values of  $n$ , but  $n = 18$  here
- Tested on both LAN, WAN, but only LAN here
- Choices:
  - Hash function: Blake2
  - PRF/PRG: AES
  - ECC curve: p256k1
- Benchmarking on a single server with two 18-core Intel Xeon CPUs @2.3 GHz, 256GB RAM
- LAN: 10 Gbps bandwidth, 0.1 ms latency

# Performance

## Throughput (Enc/sec)

Threshold (T)	PRF		DDH		DDH-NIZK	
	Enc/sec	Mbps	Enc/sec	Mbps	Enc/sec	Mbps
2	<b>1,037,703</b>	253	553	0.14	226	0.28
6	<b>45,434</b>	55	297	0.77	64	0.40
9	<b>10,194</b>	20	231	0.45	42	0.50
16	<b>524,109</b>	1919	135	0.49	23	0.43

## Latency (ms/Enc)

Threshold (T)	PRF	DDH	DDH-NIZK
2	0.1	4.6	9.6
6	0.6	5.4	21.5
9	1.1	8.0	31.3
16	2.2	12.6	55.2

# Conclusion & Future Directions

# Conclusion

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- SKE widely used, secret keys need protection (MPC expensive)
- Formalization of threshold SKE
- New very efficient scheme
- Promising performance

# Future Directions

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- DiSE lacks concrete security treatment
- Ciphertext integrity definition counts decryption towards encryption
- **ParaDiSE**: Addresses these issues – and more

# THANK YOU!

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QUESTIONS...