

KINDI

Key EncapsulatioN and Encryption baseD on Lattices

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KINDI - Introduction

- **IDEA:** Use trapdoor-based construction and inject data into the error term [EDB15,EI17]
- Trapdoor construction: Allows to retrieve secret \mathbf{s} and error \mathbf{e} from (Module- or Ring-)LWE instances:

$$\mathbf{c} = \mathbf{A} \cdot \mathbf{s} + \mathbf{e}$$



- Error Term \mathbf{e} contains all encrypted data m
 - Secret \mathbf{s} contains a key
 - Security based on pseudorandomness of \mathbf{c}
- } „simplified“ KEM and Encryption scheme simultaneously

KINDI

CPA-secure Encryption Scheme

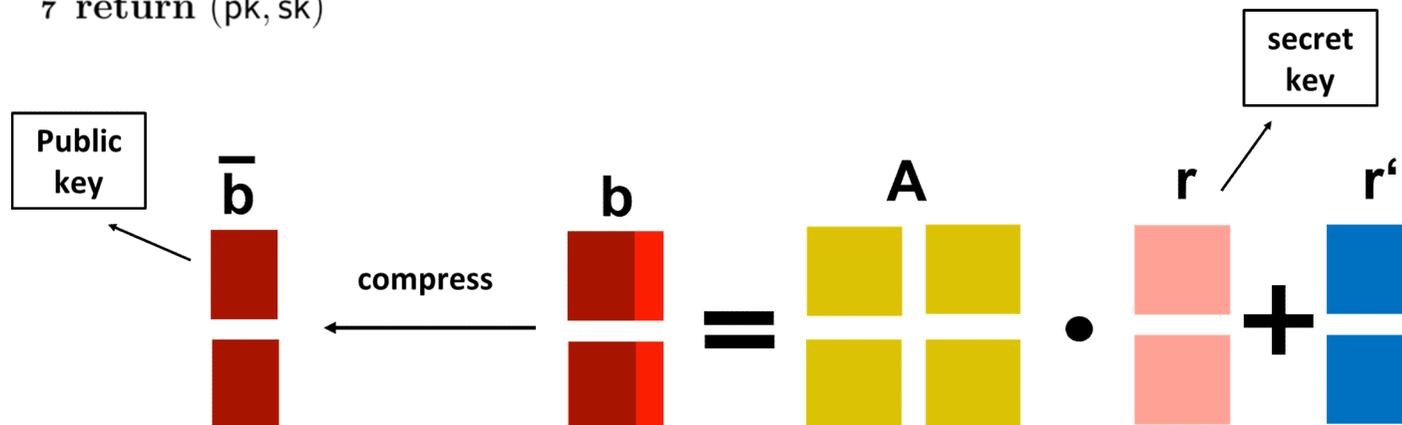
KINDI - Encryption

$\text{KINDI}_{\text{CPA}}.\text{KeyGen}(1^n, p, k, t, \ell) :$

- 1 $\gamma, \mu \leftarrow \{0, 1\}^n$
- 2 $\mathbf{A} \in \mathcal{R}_q^{\ell \times \ell} \leftarrow \text{Shake}(\mu)$
- 3 $\mathbf{r}, \mathbf{r}' \in \mathcal{R}_q^\ell \leftarrow \text{Shake}_p(\gamma)$
- 4 $\mathbf{b} = \mathbf{A} \cdot \mathbf{r} + \mathbf{r}'$
- 5 $\bar{\mathbf{b}} = \text{Compress}(\mathbf{b}, t)$
- 6 $\text{pk} := (\bar{\mathbf{b}}, \mu), \text{sk} := (\mathbf{r}, \bar{\mathbf{b}}, \mu)$
- 7 return (pk, sk)

$\mathcal{R}_q = \mathbb{Z}_q[x] / \langle x^n + 1 \rangle$

Drop t least significant bits



KINDI - Encryption

$\text{KINDI}_{\text{CPA}}.\text{Encrypt}(\text{pk}, \text{msg} = \{0, 1\}^{n(\ell+1)\log 2p}; \text{coins} = \perp \text{ or } s_1 \in \mathcal{R}_2) :$

1 $s_1 \leftarrow \mathcal{R}_2$

2 $\mathbf{A} \leftarrow \text{Shake}(\mu)$

3 $\bar{\mathbf{p}} = \text{Decompress}(\bar{\mathbf{b}}, t)$

Shift t bits:
Multiply with 2^t

4 $\mathbf{p} = (\bar{\mathbf{p}}_1 + \mathbf{g}, \bar{\mathbf{p}}_2, \dots, \bar{\mathbf{p}}_\ell)$

$\mathbf{g} = 2^{k-1}$

5 $\bar{u}, \bar{s}_1, (s_2, \dots, s_\ell) \in \{0, 1\}^{n(\ell+1)\log 2p} \times \mathcal{R}_p \times \mathcal{R}_{2p}^{\ell-1} \leftarrow G(s_1) := \text{Shake}(s_1)$

6 $\mathbf{s} = (s_1 + 2 \cdot \bar{s}_1 - [p], s_2 - [p], \dots, s_\ell - [p])^\top$

7 $u = \bar{u} \oplus \text{msg}$

8 $\mathbf{u} = \text{Encode}(u)$

9 $\mathbf{e} = (\mathbf{u}_1 - [p], \dots, \mathbf{u}_\ell - [p])^\top, e = \mathbf{u}_{\ell+1} - [p]$

Centralization to
 $\{-p, \dots, p-1\}$

10 $(\mathbf{c}, c)^\top = (\mathbf{A}^\top \cdot \mathbf{s} + \mathbf{e}, \mathbf{p} \cdot \mathbf{s} + \mathbf{g} \cdot [p] + e) \in \mathcal{R}_q^{\ell+1}$

The diagram shows the encryption equations with syringes injecting 'data' into the error terms \mathbf{e} and e .

$$\left(\begin{array}{l} \mathbf{c}^\top \\ \mathbf{c} \end{array} = \begin{array}{cc} \mathbf{A}^\top & \\ & \mathbf{p} \end{array} \cdot \begin{array}{c} \mathbf{s} \\ \mathbf{s} \end{array} + \begin{array}{c} \mathbf{e} \\ e \end{array} \right)$$

KINDI - Encryption

Algorithm 6: $\text{KINDI}_{\text{CPA}}.\text{Decrypt}(\text{sk}, (c, c))$:

- 1 $\mathbf{A} \leftarrow \text{Shake}(\mu)$
- 2 $\bar{\mathbf{p}} = \text{Decompress}(\bar{\mathbf{b}}, t)$
- 3 $\mathbf{p} = (\bar{\mathbf{p}}_1 + \mathbf{g}, \bar{\mathbf{p}}_2, \dots, \bar{\mathbf{p}}_\ell)$
- 4 $\mathbf{v} = c - \mathbf{c} \cdot \mathbf{r}^\top$
- 5 $s_1 = \text{Recover}(\mathbf{v}) \in \mathcal{R}_2$
- 6 $\bar{u}, \bar{s}_1, (s_2, \dots, s_\ell) \in \{0, 1\}^{n(\ell+1) \log 2p} \times \mathcal{R}_p \times \mathcal{R}_p^{\ell-1} \leftarrow \text{Shake}(s_1)$
- 7 $\mathbf{s} = (s_1 + 2 \cdot \bar{s}_1 - [p], s_2 - [p], \dots, s_\ell - [p])^\top$
- 8 $(\mathbf{e}, e) = (\mathbf{u}_1 - [p], \dots, \mathbf{u}_{\ell+1} - [p]) = (\mathbf{c} - \mathbf{A}^\top \cdot \mathbf{s}, c - \mathbf{p} \cdot \mathbf{s}) \bmod q$
- 9 $\text{msg} = \text{Decode}(\mathbf{u}) \oplus \bar{u}$

Divide by 2^{k-1}
and round

- Decryption retrieves secret and the error term back.
- Use message **msg** or s_1 as a key or both simultaneously.

KINDI

CCA-secure KEM

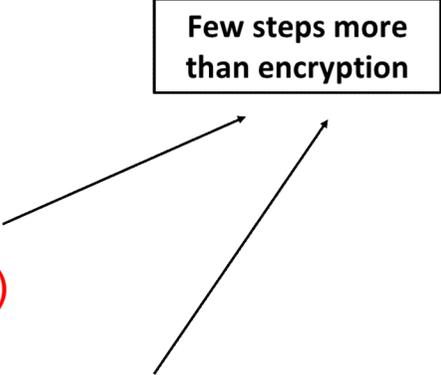
KINDI - CCA2-secure KEM

$\text{KINDI}_{\text{CCA-KEM}}.\text{Encaps}(\text{pk}) :$

- 1 $s_1 \leftarrow \{0, 1\}^n$
- 2 $d \leftarrow H(s_1)$
- 3 $(\mathbf{c}, c)^\top \leftarrow \text{KINDI}_{\text{CPA}}.\text{Encrypt}(\text{pk}, d; s_1)$
- 4 $K \leftarrow H'(s_1, (\mathbf{c}, c))$

- In the random oracle model: $\mathbf{d}=\mathbf{0}$.
Essentially: $(\mathbf{c}, c) = \text{Encrypt}(\text{pk}, \mathbf{0})$, $\mathbf{K} = H'(s_1, (\mathbf{c}, c))$
- In the quantum random oracle model: $\mathbf{d} = H(s_1)$
Essentially: $(\mathbf{c}, c) = \text{Encrypt}(\text{pk}, \mathbf{d} = H(s_1))$, $\mathbf{K} = H'(s_1, (\mathbf{c}, c))$
- Note: \mathbf{d} can be encrypted, too

Few steps more
than encryption



KINDI - CCA2-secure KEM

$\text{KINDI}_{\text{CCA-KEM}}.\text{Decaps}(\text{sk}, (\mathbf{c}, c)) :$

- 1 $(d', s'_1) \leftarrow \text{KINDI}_{\text{CPA}}.\text{Decrypt}(\text{sk}, (\mathbf{c}, c))$
- 2 **if** $d' = d := H(s'_1)$
- 3 **return** $H'(s'_1, (\mathbf{c}, c))$
- 4 **else**
- 5 **return** $H'(s, (\mathbf{c}, c))$

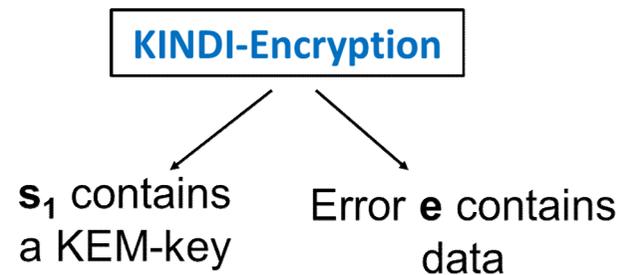
- Due to trapdoor design ciphertext computation/check not required
- RO: Few steps more than Decryption:
 Check $d=0$ & compute $\mathbf{K}=H'(s_1, (\mathbf{c}, c))$
- qRO: Few steps more than Decryption:
 Check $d=H(s_1)$ & compute $\mathbf{K}=H'(s_1, (\mathbf{c}, c))$

KINDI - Design Features

- Trapdoor construction - recovery of secret and error vectors for inspection:
 - Message recovery
 - Have errors and secrets correct format?
 - Has ciphertext been altered?
- Security: Constructions based on module-LWE [LS15] in the (quantum-)RO
 - For module rank equal to 1: ring-LWE
 - Fine grained usage of dimensions for better security-efficiency tradeoffs
 - Higher protection against dense sub-lattice attacks [KF17] etc.

KINDI - Design Features

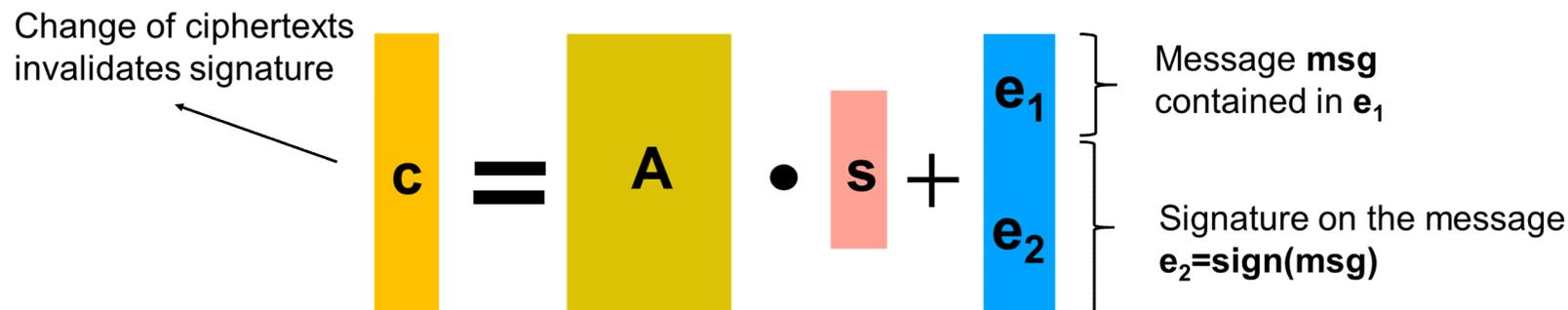
- Simplicity of design for encryption and KEM
- KINDI-Encryption scheme always by design encrypts a message and key simultaneously



- Thus, few steps needed to obtain CCA2-secure KEMs [HHK17]

KINDI - Design Features

- Huge amount of data can be encrypted at small ciphertext sizes
 - $(l+1) \cdot n \cdot \log 2p$ bits of data or $\log 2p$ bits per coefficient
 - Low message expansion $\log 2p / \log q$, e.g. 4 or lower possible
 - Increasing parameters l, n, p  more data and security
 - Allows to encrypt bundles of session keys, signatures, etc.
 - Suitable for sign-then-encrypt scenarios



KINDI - Design Features

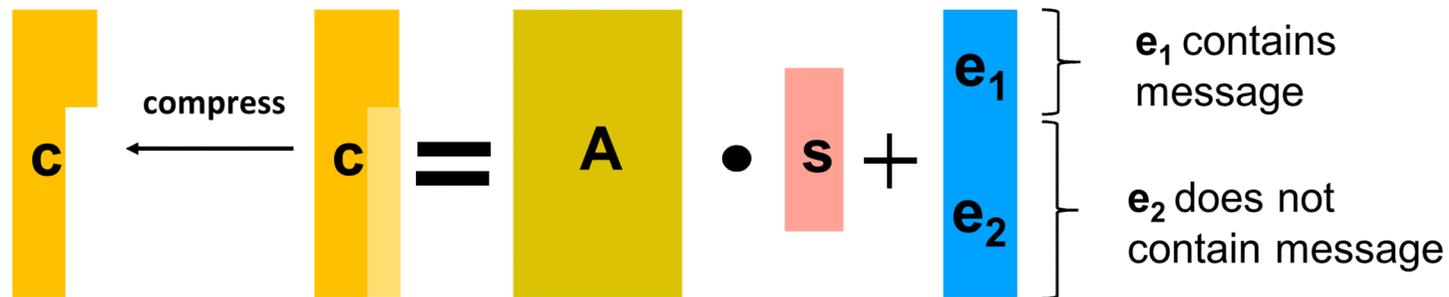
- KINDI encryption scheme can easily be turned to be CCA2-secure beside the proposed KEM variant:
 - Slightly larger parameters
 - Essentially check size of coefficients
 - Add $F(s_1, e)$ to the ciphertext with $F=RO$
- Authenticated key exchange is obtained via generic transformations



- Trapdoor constructions are used in many advanced primitives ranging from group signatures to attribute-based encryption

KINDI - Design Features

- Possible Modifications: Ciphertext can also be compressed in case the complete bandwidth is not used



- Secret and public keys can be generated from small seeds, if sizes are critical

KINDI - Technical Features

- Highly efficient implementation even at a high security level, also suitable for IoT
- Use of power-of-two modulo and domain size, e.g. for error distrib.:
 - No rejection sampling and no waste of random bits
 - No expensive modulo operations, one use of „AND“
- Polynomial multiplication: FFT multiplication in cyclotomic ring x^n+1 for small $n=2^k$ such as $n=256, 512$. Reusage of the FFT subroutine for any change of parameters l, p, q . Extendable to NTT case.
- Usage of FIPS 202 standardized Shake for random bit generation and random oracle instantiations

KINDI - Technical Features

- Constant time implementation:
Computations independent from secret elements
- Additional implementation: Improved running times via parallelization, e.g.
 - AVX parallelization of the FFT
 - Vectorized Keccak: faster generation of random bits and key derivation

KINDI - Results

Scheme	Sizes (bytes)	Timings (Spec. AVX Impl.)	Timings (Spec. Ref. Impl.)	Bit Security (conservative)	NIST Category
Encryption KINDI-256-3	PK 1184 SK 1472 CT 1792	Keygen 104308 Encrypt 122648 Decrypt 151723	Keygen 203096 Encrypt 247793 Decrypt 312211	>160	3
KEM KINDI-256-3	PK 1184 SK 1472 CT 1792	Encaps 133888 Decaps 162070	Encaps 260137 Decaps 323947	>160	3
Encryption KINDI-512-2	PK 1456 SK 1712 CT 2496	Keygen 113082 Encrypt 142950 Decrypt 187097	Keygen 214064 Encrypt 280420 Decrypt 377962	>220	5
KEM KINDI-512-2	PK 1456 SK 1712 CT 2496	Encaps 160150 Decaps 202458	Encaps 306043 Decaps 397147	>220	5

KINDI - Design Features

- Current implementation and documentation at: <http://kindi-kem.de/>
- [HHK17] Dennis Hofheinz, Kathrin Hövelmanns, and Eike Kiltz. A Modular Analysis of the Fujisaki-Okamoto Transformation. IACR Cryptology ePrint Archive, 2017:604. 2017.
- [LS15] Adeline Langlois and Damien Stehlé. Worst-case to Average-case Reductions for Module Lattices. Designs, Codes and Cryptography. 2015
- [EDB15] Rachid El Bansarkhani, Ozgür Dagdelen, and Johannes A. Buchmann. Augmented Learning with Errors: The Untapped Potential of the Error Term. Financial Cryptography and Data Security. 2015.
- [EI17] El Bansarkhani Rachid. Lara - A Design Concept for Lattice-based Encryption. Cryptology ePrint Archive, Report 2017/049. 2017.

KINDI - Design Features

- [KF17] Paul Kirchner and Pierre-Alain Fouque. Revisiting Lattice Attacks on overstretched NTRU Parameters. EUROCRYPT. 2017