







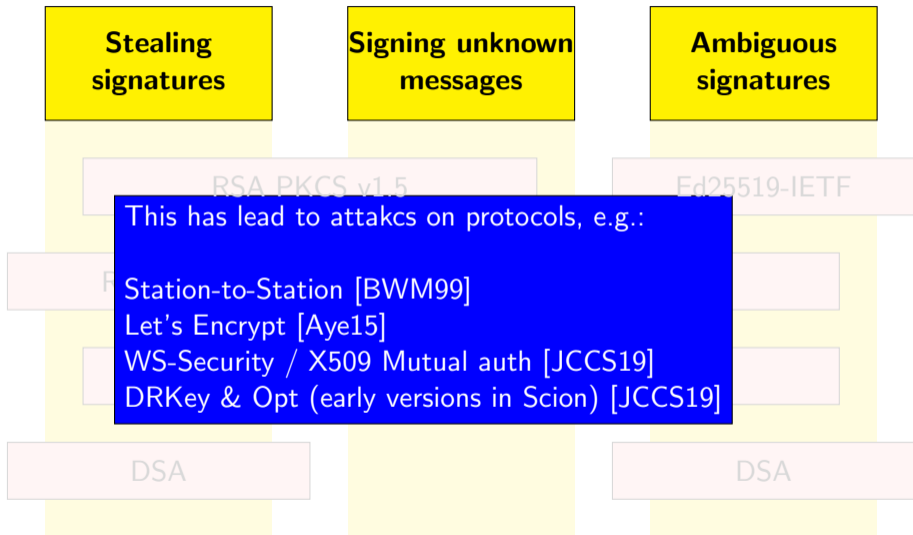




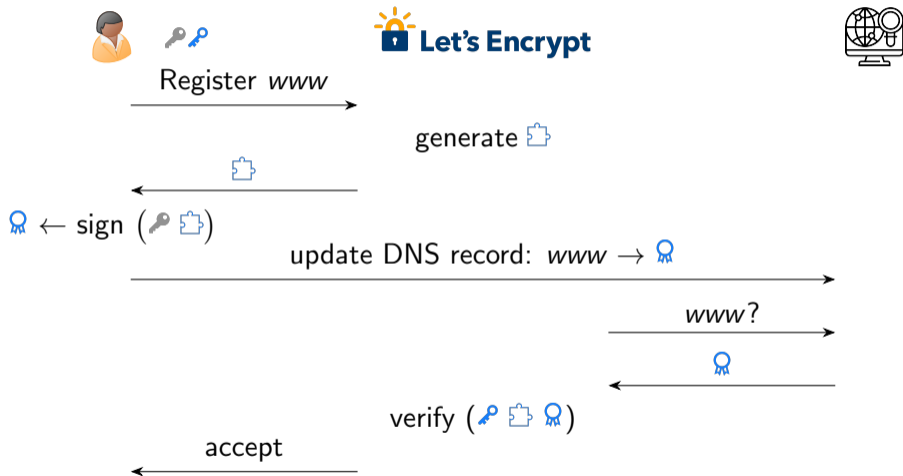


# Unforgeability does not protect from malicious public keys

Examples of affected schemes:

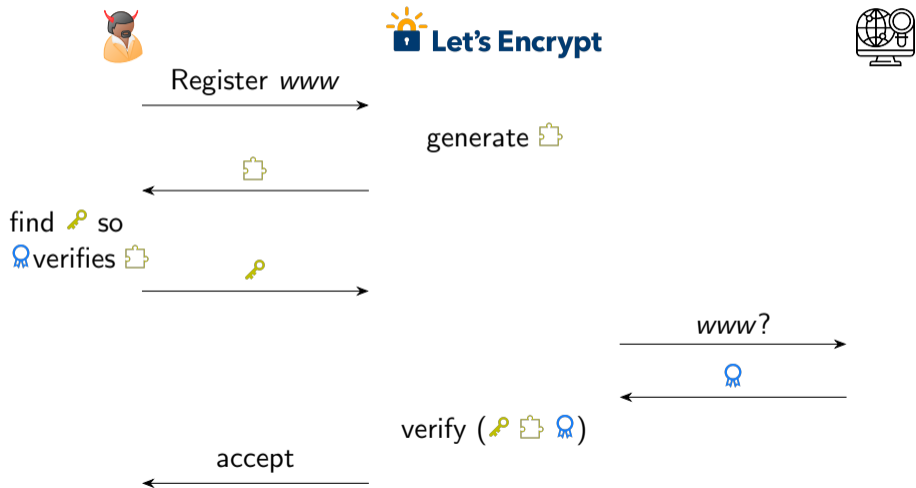


# Attacking real-world protocols with malicious public keys I





# Attacking real-world protocols with malicious public keys II



- ▶ Schemes that offer S-CEO/S-DEO, MBS, and NR provide BUFF:

## Beyond UnForgeability Features

- ▶ and don't have the unexpected behaviors of stealing signatures, signing unknown messages, or ambiguous signatures.

# Several NIST finalists lack BUFF

	Scheme	S-CEO & S-DEO	MBS	NR
main	CRYSTALS-Dilithium	✓	✓	✓
	FALCON	✗	✓	✗
	Rainbow Standard	✗	✓	✗
	Rainbow CZ & Compr.	◆	✓	✗
alternate	GeMSS	✗	✗	✗
	Picnic	✓	✓	✓
	SPHINCS <sup>+</sup>	◆	✓	◆

✓ property holds   ✗ attack given   ◆ inconclusive

# Our generic BUFF transformation

- ▶ Schemes can be transformed to meet BUFF by adding scheme-specific checks
- ▶ or by applying our generic BUFF transformation:
  - ▶ Compute  $H(pk, m)$ . Sign digest. Prepend digest to the signature.

$\begin{aligned} h &\leftarrow H(pk, m) \\ \sigma &\leftarrow \text{Sign}(sk, h) \\ \text{return } &(h, \sigma) \end{aligned}$
--

- ▶ Verification additionally checks the digest

$\begin{aligned} h &= H(pk, m) \\ \wedge \text{Vf}(pk, h, \sigma) \end{aligned}$
--

# Our generic BUFF transformation achieves BUFF

$$\begin{aligned} h &\leftarrow H(\text{pk}, m) \\ \sigma &\leftarrow \text{Sign}(\text{sk}, h) \\ \text{return } (h, \sigma) \end{aligned}$$
$$\begin{aligned} h &= H(\text{pk}, m) \\ \wedge \text{Vf}(\text{pk}, h, \sigma) \end{aligned}$$

- ▶ Hashing in Sign binds to  $(\text{pk}, m)$
- ▶ Checking digest in Vf prevents weak keys (where Vf always returns true)
- ▶ Formally, security reduces to security properties of H

# Our generic BUFF transformation is efficient

```

$$h \leftarrow H(pk, m)$$

$$\sigma \leftarrow \text{Sign}(sk, h)$$

$$\text{return } (h, \sigma)$$

```

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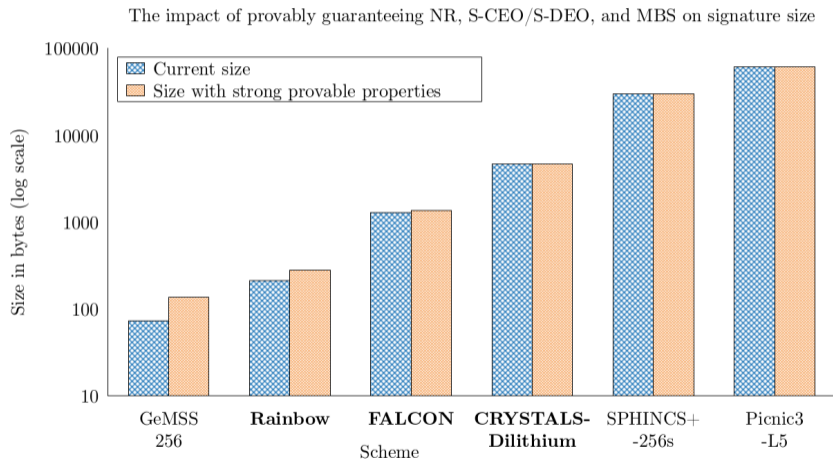
$$h = H(pk, m)$$

$$\wedge \text{Vf}(pk, h, \sigma)$$

```

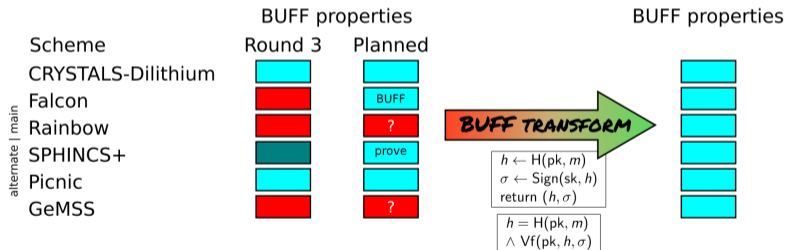
- ▶ One hash function evaluation in Sign and Vf each
- ▶ Signature size increases by the size of one hash digest

# BUFF transformation keeps relative signature sizes



# BUFF finalists now, prevent headaches later!

- ▶ Protect upcoming standard against maliciously generated public keys!
- ▶ Scheme-specific proofs or apply generic BUFF transformation
- ▶ Situation similar to length-extension resilience of SHA3
- ▶ NIST chooses Dilithium or FALCON (and SPHINCS+), all three will have BUFF!



Full paper: <https://eprint.iacr.org/2020/1525> (and IEEE S&P 2021)  
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# References I

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# References II

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# Picture references

- ▶ secret key icon by Yannick Lung
- ▶ public key icon by Yannick Lung
- ▶ "Let's Encrypt Wide" by Let's Encrypt is licensed under CC BY-NC 4.0
- ▶ DNS icon made by Eucalyp from Flaticon
- ▶ puzzle icon by Becris.
- ▶ Signature icon by PINPOINT.WORLD is licensed under CC BY 3.0
- ▶ Message icon by Yannick Lung

# Fiat-Shamir Transform implements BUFF transform

$\text{Sign}(sk, m) :$

$c \leftarrow H(pk, m, a)$

$\dots$

$\sigma \leftarrow (c, \dots)$

{

Dilithium  
(LWE, SIS)

Picnic  
(ZK, MPC-in-the-head)

- ▶ Fiat-Shamir transform implements BUFF transform
- ▶ Dilithium and Picnic provide BUFF

$\text{Vf}_{\text{FALCON}}(\text{pk} = h, m, \sigma = (r, s_2))$

$c \leftarrow H(r, m)$   
 $s_1 \leftarrow c - s_2 h$   
 $d \leftarrow \|(s_1, s_2)\|^2 \leq \lfloor \beta^2 \rfloor$

↓  
 $d$

- ▶ leverage (non-)invertibility of  $s_2$  to break exclusive ownership and NR

# Rainbow (& GeMSS)

$\text{Vf}_{\text{Rainbow}}(\text{pk} = \mathcal{P}, m, \sigma = (z, r))$

$h \leftarrow \text{H}(\text{H}(m), r)$   
 $d \leftarrow \mathcal{P}(z) = h$

$d$

- ▶ Construct tailored public map  $\mathcal{P}$  for fixed digest to break exclusive ownership
- ▶ Re-sign digest under own key to break NR
- ▶ GeMSS has additional input to  $\mathcal{P}$  that allows wiggle room to break MBS

# SPHINCS+

$Vf_{SPHINCS+}(pk = (seed, root), m, \sigma = (r, \sigma_{HT}))$

$digest \leftarrow H_{msg}(r, pk.seed, pk.root, m)$

$root' \leftarrow \text{hash to the root}(digest, pk.seed, \sigma_{HT})$

$d \leftarrow root' = pk.root$

↓  
 $d$

- ▶ Breaking exclusive ownership requires finding  $pk'.root = H(\dots H_{msg}(pk'.root, \dots))$
- ▶ If signature leaks  $digest$ , NR reduces to  $\Phi NM$  of  $H_{msg}$ , otherwise attacker can only guess

# Comparison of transformations

Transform.	Signature	S-CEO	S-DEO	M-S-UEO	MBS	NR
[PS05]-1	$\text{Sig}(\text{sk}, m), H(m)$	✗	✓	✗	✓	✗
[PS05]-2	$\text{Sig}(\text{sk}, m), H(\text{pk})$	✓	✓	✓	✗	✗
[PS05]-3	$\text{Sig}(\text{sk}, H(m, \text{pk}))$	✗ (✓)	✗ (✓)	✗	✗	✗
BUFF	$\text{Sig}(\text{sk}, H(m, \text{pk})), H(m, \text{pk})$	✓	✓	✓	✓	✓

✓ provides property   ✗ vulnerable   (✓) provides property if no weak keys