

Lattice-based digital signature scheme: qTESLA



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Introduction

- qTESLA is a family of lattice-based signature schemes
- Based on decisional ring-LWE problem
- The result of a long line of research (selected):

Introduction

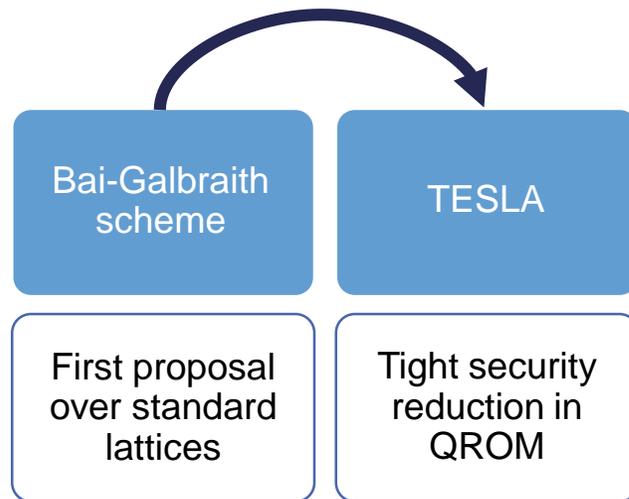
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Bai-Galbraith
scheme

First proposal
over standard
lattices

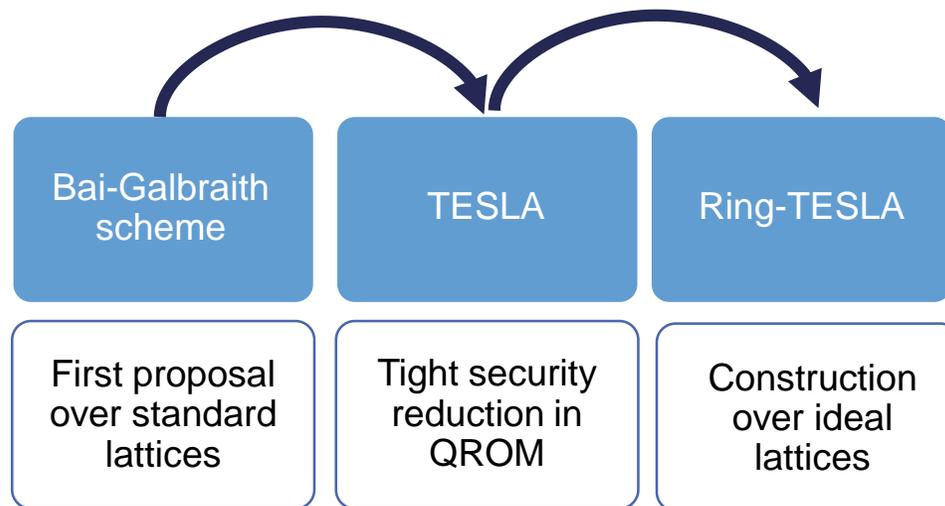
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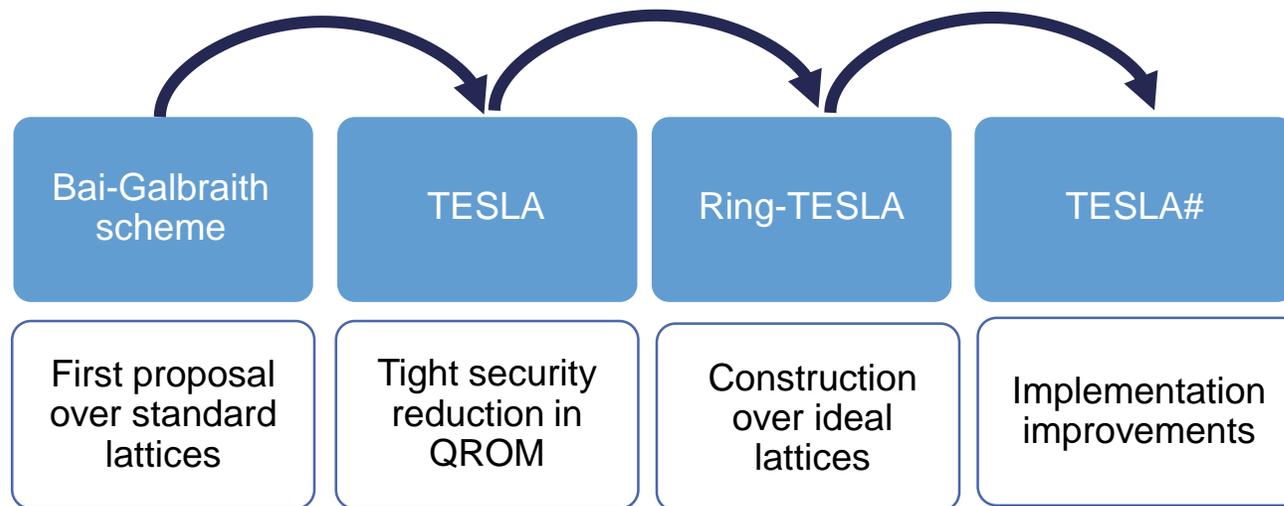
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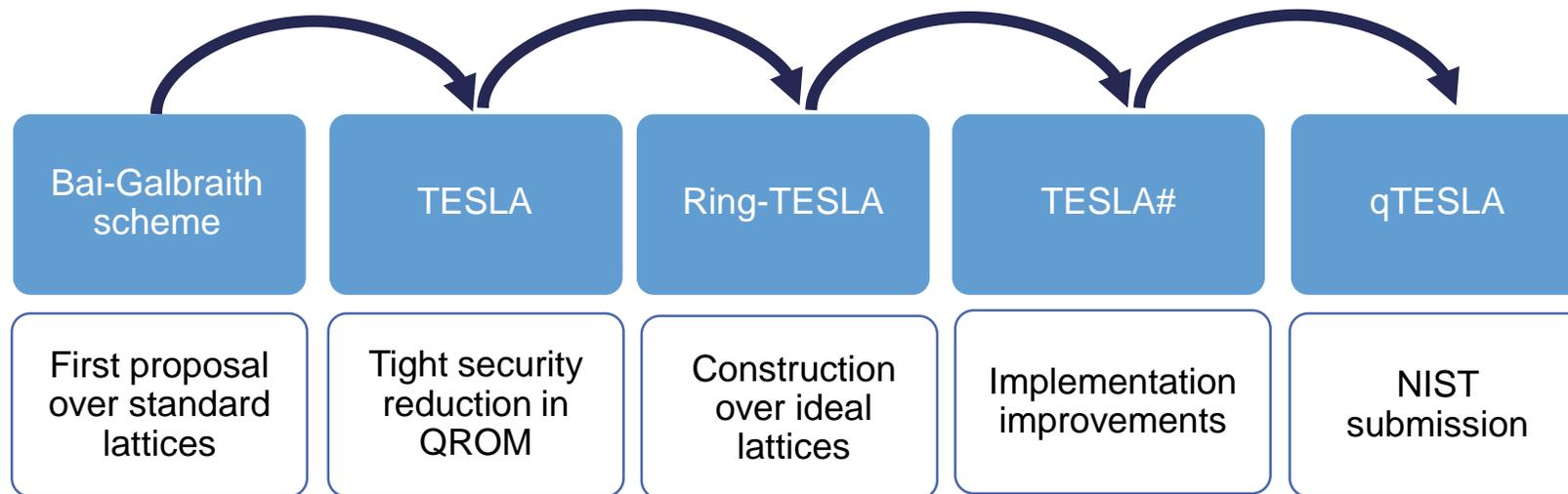
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qTESLA – Key generation

□ Secret key:

- $s, e_1, \dots, e_k \xleftarrow{\sigma} \mathbb{Z}[x]/\langle x^n + 1 \rangle$, “small enough”
- $seed_a, seed_y$

□ Public key:

- $t_1 \leftarrow a_1 s + e_1 \bmod q, \dots, t_k \leftarrow a_k s + e_k \bmod q$ with $a_1, \dots, a_k \leftarrow GenA(seed_a)$
- $seed_a$

qTESLA – Signing

Require: message m , and secret key $sk = (s, e_1, \dots, e_k, \text{seed}_a, \text{seed}_y)$

Ensure: signature (c', z)

```
1: counter  $\leftarrow 0$ 
2: rand  $\leftarrow \text{PRF}_1(\text{seed}_y, m)$ 
3:  $y \leftarrow \text{PRF}_2(\text{rand}, \text{counter})$ 
4:  $a_1, \dots, a_k \leftarrow \text{GenA}(\text{seed}_a)$ 
5: for  $i = 1, \dots, k$  do
6:    $v_i = a_i y \pmod q$ 
7: end for
8:  $c' \leftarrow H([v_1]_M, \dots, [v_k]_M, m)$ 
9:  $c \leftarrow \text{Enc}(c')$ 
10:  $z \leftarrow y + sc$ 
11: if  $z \notin \mathcal{R}_{q, [B-L_S]}$  then
12:   counter++
13:   Restart at step 3
14: end if
15: for  $i = 1, \dots, k$  do
16:    $w_i \leftarrow v_i - e_i c \pmod q$ 
17:   if  $\|[w_i]_L\|_\infty > 2^d - L_E \vee \|w_i\|_\infty > \lfloor q/2 \rfloor - L_E$  then
18:     counter++
19:     Restart at step 3
20:   end if
21: end for
22: return  $(c', z)$ 
```

qTESLA – Signing

Require: message m , and secret key $sk = (s, e_1, \dots, e_k, \text{seed}_a, \text{seed}_y)$

Ensure: signature (c', z)

```
1: counter  $\leftarrow$  0
2: rand  $\leftarrow$  PRF1(seedy, m)
3: y  $\leftarrow$  PRF2(rand, counter)
4: a1, ..., ak  $\leftarrow$  GenA(seeda)
5: for i = 1, ..., k do
6:   vi = aiy mod q
7: end for
8: c'  $\leftarrow$  H([v1]M, ..., [vk]M, m)
9: c  $\leftarrow$  Enc(c')
10: z  $\leftarrow$  y + sc
11: if z  $\notin$   $\mathcal{R}_{q, [B-L_S]}$  then
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Pseudo-randomness
expansion

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5: for $i = 1, \dots, k$ do 6: $v_i = a_i y \pmod q$ 7: end for 8: $c' \leftarrow H([v_1]_M, \dots, [v_k]_M, m)$ 9: $c \leftarrow \text{Enc}(c')$ 10: $z \leftarrow u + sc$	Computing sparse polynomial c and candidate signature z
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qTESLA – Signing

Require: message m , and secret key $sk = (s, e_1, \dots, e_k, \text{seed}_a, \text{seed}_y)$

Ensure: signature (c', z)

<pre> 1: counter \leftarrow 0 2: rand \leftarrow PRF₁(seed_y, m) 3: y \leftarrow PRF₂(rand, counter) 4: a₁, ..., a_k \leftarrow GenA(seed_a) </pre>	Pseudo-randomness expansion
<pre> 5: for $\iota = 1, \dots, k$ do 6: v_{ι} = a_{ι}y mod q 7: end for 8: c' \leftarrow H([v₁]_M, ..., [v_k]_M, m) 9: c \leftarrow Enc(c') 10: z \leftarrow u + sc </pre>	Computing sparse polynomial c and candidate signature z
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Advantages of qTESLA

- Flexible choice of parameters
 - 2 approaches to instantiate qTESLA
 - Heuristic
 - Provable-secure
- Ease of implementation
 - Structurally simple
 - Easy-to-implement underlying arithmetic
 - Gaussian sampling is not required for signing, only for key generation
- Security against implementation attacks
 - Cache-side-channel free for signature generation
 - Isochronous Gaussian sampling and arithmetic operations
 - Countermeasures against fault attacks (by-product of checking the candidate signature)

Parameter sets

- Two parameter sets

- Provably-secure

- Enabling tight security reduction from R-LWE in the quantum random oracle model
 - More conservative

- Heuristic

- Extrapolation of the concrete complexity of solving the underlying lattice problem, without targeting a tight formal security
 - Suitable for applications where performance or signature/key sizes are the main concern

Quick background story

- Initially, exclusively provably-secure parameters
 - Choose parameters guided by the security reduction

- A mistake was found by V. Lyubashevsky (thanks!)
 - Security reduction still holds
 - Bit security estimates unchanged
 - But “provable-security” property is lost for those parameters

Potential tweaks

- Tweak 1: include “provably-secure” parameters, as originally intended
- Tweak 2: fine-tune current “heuristic” parameters to get better performance

Preliminary results

Key and signature sizes (in bytes) – NIST security category 3

Parameter set	Approach	Public key	Secret key	Signature
qTESLA-128	Heuristic	2 976	1 856	2 720
qTESLA-p-128	Provable	19 872	7 744	3 104

Performance (in kilocycles) of the reference implementation on a 2.40 GHz Intel Core i5-6300U (Skylake) processor – NIST security category 3

Parameter set	Approach	keygen	sign	verify
qTESLA-128	Heuristic	2 234	1 279	229
qTESLA-p-128	Provable	4 334	2 420	732

Coming soon!

- Updated version of the specs document
- Optimized implementations for heuristic and provable-secure parameters

Thanks!

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qTESLA website:
<https://tesla.informatik.tu-darmstadt.de/de/tesla>

Nina says hi!

