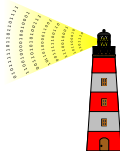


# Randomness Beacons as Enablers of Public Auditability

Luís Brandão

Cryptographic Technology Group  
National Institute of Standards and Technology



Presentation at [STPPA 01](#)  
Special Topics on Privacy and Public Auditability  
January 27, 2020 @ Gaithersburg, Maryland, USA

Some slides are based on previous presentations ([IMFD Oct 2019](#), [ICMC May 2019](#)).

The Reference for Randomness Beacons is joint work with John Kelsey, Rene Peralta and Harlod Booth.

The [Interoperable Randomness Beacons](#) project is joint work with others in the [Cryptographic Technology Group](#).

# Outline

1. Introduction
2. Randomness Beacons (format and operations)
3. Usages of beacon randomness
4. Concluding remarks

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## **Goals of this presentation:**

- ▶ Brief overview of the NIST Reference for Randomness Beacons
- ▶ Allude to possible public-auditability applications

# Outline 1

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At a high level (from Wikipedia):

**Randomness**

**Public Good**

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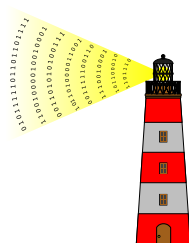
## Audit

- ▶ "a systematic and independent examination [...] to ascertain how far the [...] statements [...] present a true and fair view [...]"

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*A service that produces timed outputs of fresh **public randomness***  
(The idea goes back at least till 1983 — proposed by Rabin to aid crypto operations.)



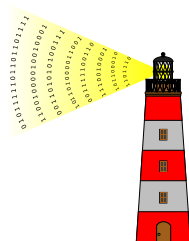
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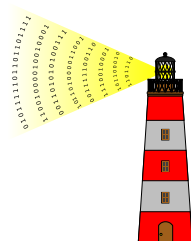
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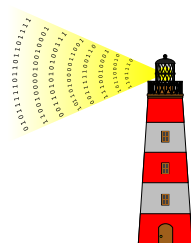
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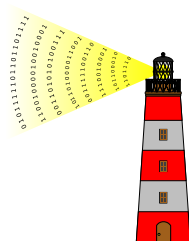
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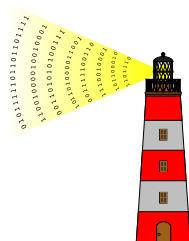
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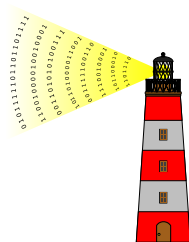
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- ▶ public auditability of randomized processes
- ▶ coordination between multiple parties (e.g., who does/wins something)
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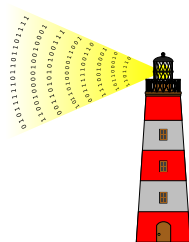
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**NOT good for:** selecting your secret keys

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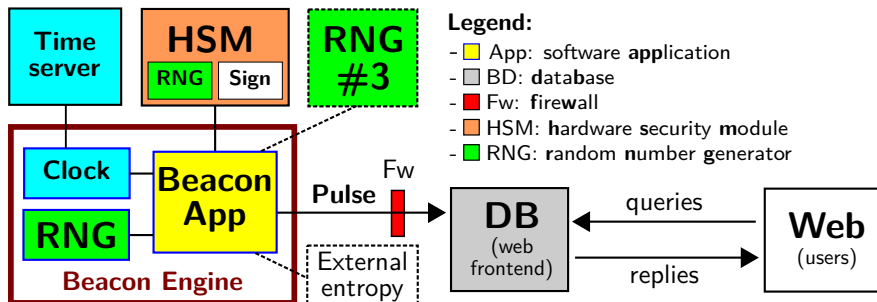
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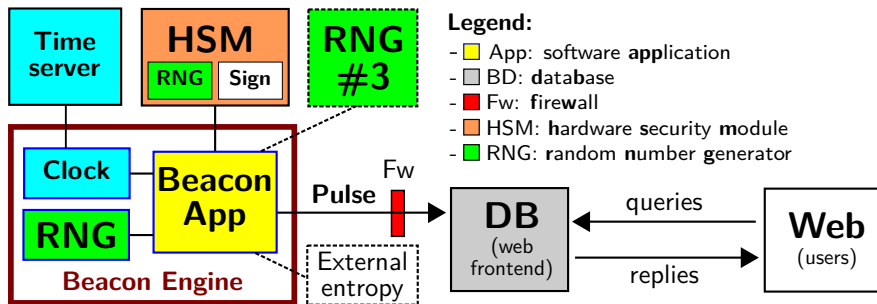
- ▶ Can the beacon be influenced to select (or not select) a particular official?
- ▶ Can an attacker learn in advance which officials will be selected?
- ▶ What interests are at stake? What resources does an adversary have?

# Architecture of the Beacon service



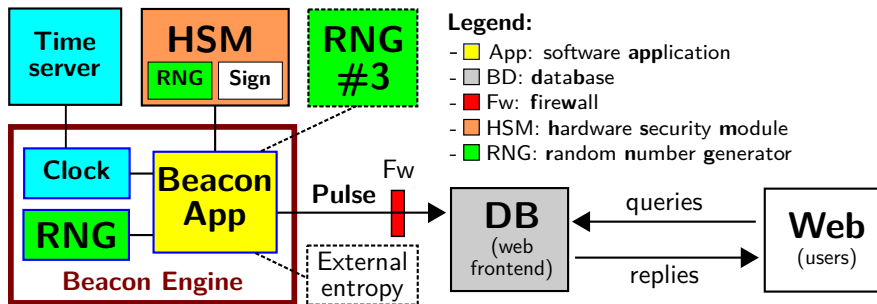


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But, what exactly is a *pulse*? where does its randomness come from?, ...

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A **Reference** for Randomness Beacons:  
Format and Protocol Version 2

<https://doi.org/10.6028/NIST.IR.8213-draft>



# NIST project: Interoperable Randomness Beacons

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The project has four main tracks:

- **A.** promote a [reference for randomness beacons](#);
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Also interested in assisting initiatives about trusted randomness, e.g., quantum RNGs and certifiable randomness.

The screenshot shows a sidebar navigation menu for the NIST project. It includes sections for PROJECT LINKS, CONTACTS, GROUP, and TOPICS. The CONTACTS section lists several individuals: Rene Perle, Daniel J. Bernstein, Michael Bartack, Lawrence Bossman, Harold Booth, Luis T. A. N. Brandão, Tyler Diamond, John Kelsey, and Carl Miller. The GROUP section lists Cryptographic Technology. The TOPICS section lists Security and Privacy: cryptogpsshy.

PROJECT LINKS

- Overview
- Presentations

CONTACTS

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[rene.perle@nist.gov](mailto:rene.perle@nist.gov)  
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Michael Bartack  
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GROUP

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## Some milestones:

- ▶ 2013: Prototype NIST beacon v1.0
- ▶ 2018: Quantum RNG by Physics Measurement Lab
- ▶ 2018: Deployment of NIST beacon v2.0
- ▶ 2019: Publication of Reference for randomness beacons

# Outline 2

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## Some concepts useful in this talk

- ▶ **Hash:**



- ▶ **Commitment:**



- ▶ **[Digital] Signature:**



## Some concepts useful in this talk

### ▶ **Hash:**

- like a fingerprint of data ('unique' string 512 of bits)
- looks random if its originator data is unknown



### ▶ **Commitment:**

- like a vault that hides data, until it is opened
- once closed, cannot change what is inside



### ▶ **[Digital] Signature:**

- like a physical signature, but cannot be forged
- a signature copied to another document is invalid





## A pulse (simplified example)

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- ▶ Other features: **signed**

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- ▶ Two main random values (“rands”): randLocal and randOut.
- ▶ Other features: signed, committed randLocal, **chained randOut**, ...



# The two “rands” in a pulse

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**randLocal** (local random value):

**randOut** (output value):

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- ▶ **What:** Hash of randomness produced by  $\geq 2$  RNGs
- ▶ **How:** **Pre-committed** 1 minute in advance of release
- ▶ **Why:** Randomness contribution to combine with randomness of other beacons

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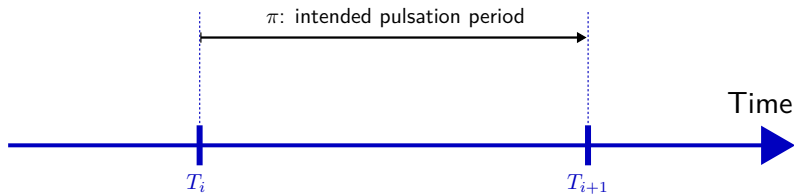
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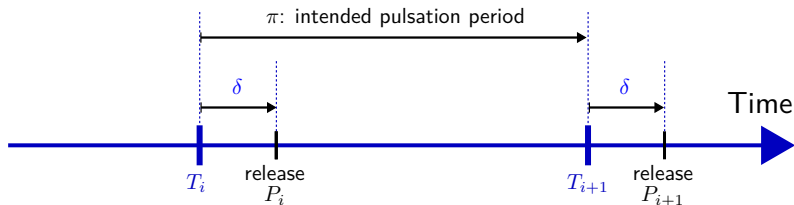
- ▶ **What:** Hash of all other fields
- ▶ **How:** **Fresh** at the time of release
- ▶ **Why:** Randomness seed for applications that completely trust this beacon

# Timing for generation and release



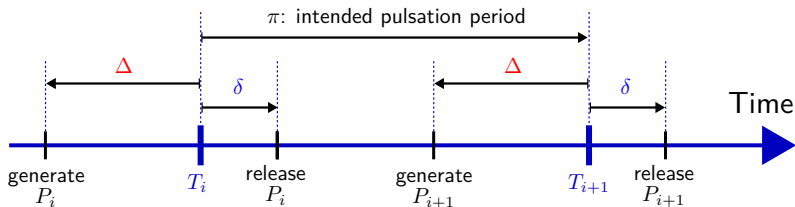
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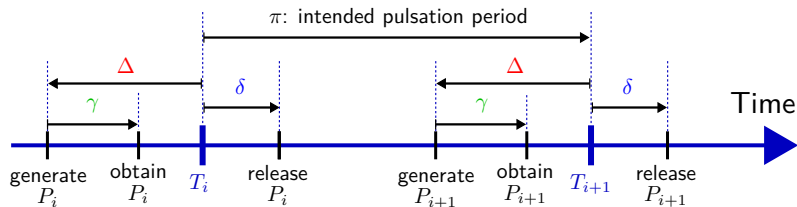
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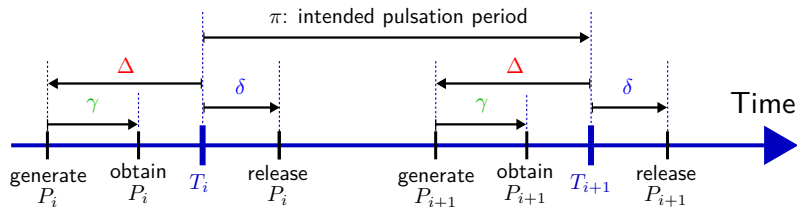
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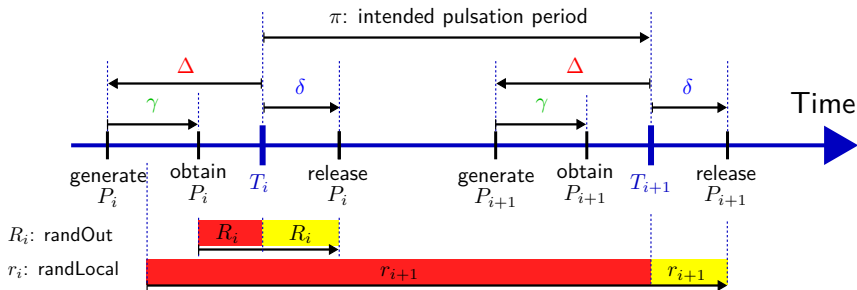
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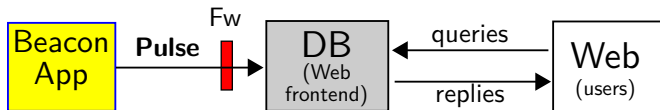


(The actual requirements specify allowed intervals for  $\delta$  and  $\Delta$ )

# Fetching pulses

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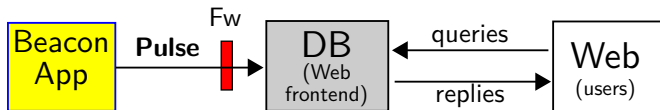
Beacon App: a pulse release means sending it to the database



Legend: App: **a**pplication; DB: **d**atabase; Fw: **f**irewall.

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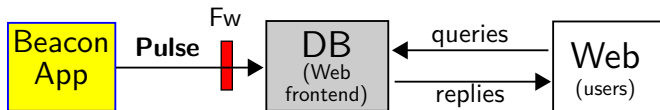
Legend: App: **application**; DB: **database**; Fw: **firewall**.

The users request a pulse from the database through a URI/URL:

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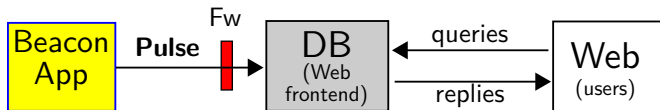
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Example: URL for the latest pulse in chain 1 of the NIST randomness Beacon (version 2)



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Other queries exist: by pulselid; skiplists; certificates; external values...





# Outline 3

1. Introduction
2. Randomness Beacons (format and operations)
3. Usages of beacon randomness
4. Concluding remarks

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- ▶ Combine randomness from various beacons
  - No single beacon can affect the randomness that will be used
- ▶ Combine a local secret (and committed) value
  - The beacon cannot predict which seed the application will get

## Some Beacons in development

Three countries are developing Beacons to match the current reference:



- ▶ (United States) NIST Randomness Beacon  
<https://beacon.nist.gov/home>
- ▶ (Chile) Random UChile  
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We would like others to join



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*“You have been randomly selected for additional screening”*

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### **Example applications:**

- ▶ Select random test vs. control groups for clinical trials
- ▶ Select random government officials for financial audits
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**Advanced features:** zero-knowledge proofs (ZKP) to enable auditability with privacy

# Use case: public auditability with privacy

**Challenge: random selection depending on private attributes**

Public		Private initial			Private derivative	
# ( $i$ )	Rand id	Name ( $N$ )	$a$	$b$	Weight ( $w$ )	Acc. ( $W$ )
1	371	<b>C</b> ai	1	2	0.1	0.1
2	942	<b>E</b> ve	2	7	0.3	0.4
3	107	<b>B</b> ob	1	5	0.2	0.6
4	527	<b>A</b> nn	1	9	0.3	0.9
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1.  $a_i \in A$  (e.g., annual salary);  $b_i \in B$  (e.g., years in position);
2.  $w_i = f(a_i, b_i)$  (correct probability weight);
3.  $\sum_i w_i = 1$  (correct sum of weights);
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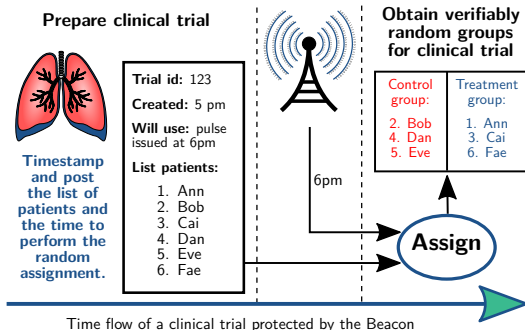
Derive  $R$ :  $0 < R \leq 1$  (random) from the Beacon and determine #  $j$ :  $W_{\max(1, j-1)} < R \leq W_j$

- **Prove in ZK** that  $j$  is consistent with  $R$  and the table of commitments



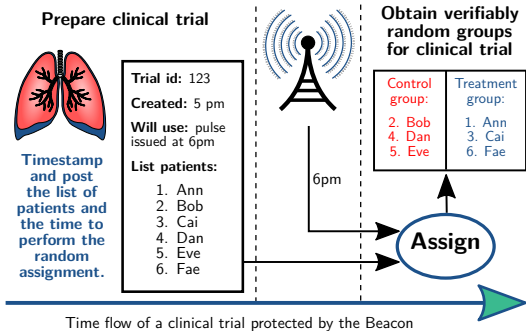
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Apply commitments and zero-knowledge proofs to hide private data while proving correctness.

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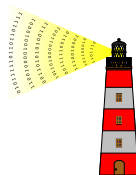
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- ▶ **We would like to have your collaboration!**

- ▶ NISTIR 8213: <https://doi.org/10.6028/NIST.IR.8213-draft>
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## Randomness Beacons as Enablers of Public Auditability



Presentation at Special Topics on Privacy and Public Auditability  
January 27, 2020 @ Gaithersburg, Maryland, USA

[luis.brandao@nist.gov](mailto:luis.brandao@nist.gov)

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4. Some concepts in this presentation
5. A Randomness Beacon
6. An example/conceivable application
7. Architecture of the Beacon service
8. NIST project: Interoperable Randomness Beacons
9. Outline 2
10. Some concepts useful in this talk
11. A pulse (simplified example)
12. The two “rands” in a pulse
13. Timing for generation and release
14. Fetching pulses
15. A possible diagram of pulse generation
16. Outline 3
17. Using Beacon randomness
18. Do you need to trust the Beacon?
19. Some Beacons in development
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21. Use case: public auditability with privacy
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