

Twelve-round KECCAK for secure hashing

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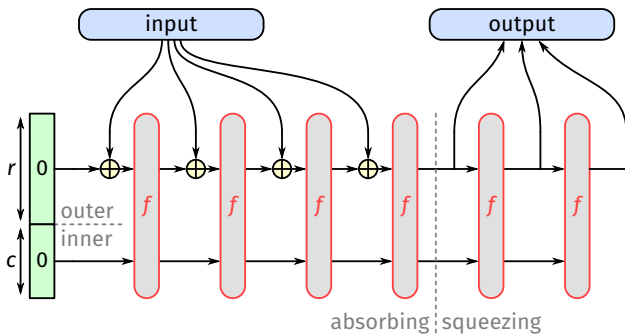
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Outline

- 1 KECCAK, SHA-3, SHAKE and cSHAKE
- 2 Status of cryptanalysis
- 3 Towards defining TurboSHAKE
- 4 Conclusions

The KECCAK sponge function in PQC



Sponge function on top of KECCAK- $f[1600]$, with

- $r + c = 1600$ bits
- KECCAK- $f[1600] = \text{KECCAK-}p[1600, n_r = 24]$

NIST FIPS 202

- Four drop-in replacements to SHA-2
- Two *extendable output functions* (XOF)

XOF	SHA-2 drop-in replacements
KECCAK[c = 256](M 11 11)	
	first 224 bits of KECCAK[c = 448](M 01)
KECCAK[c = 512](M 11 11)	
	first 256 bits of KECCAK[c = 512](M 01)
	first 384 bits of KECCAK[c = 768](M 01)
	first 512 bits of KECCAK[c = 1024](M 01)
SHAKE128 and SHAKE256	SHA3-224 to SHA3-512

- Toolbox for building other functions, including KECCAK-p[1600, n_r]

NIST SP 800-185

Customized SHAKE (**cSHAKE**)

- $H(x) = \text{cSHAKE}(x, \text{name}, \text{customization string})$
- E.g., $\text{cSHAKE128}(x, N, S) = \text{KECCAK}[c = 256](\text{encode}(N, S) || x || 00)$
- $\text{cSHAKE128}(x, N, S) \triangleq \text{SHAKE128}$ when $N = S = ""$

Based on cSHAKE:

- KMAC
- TupleHash
- ParallelHash

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Security assurance of a primitive

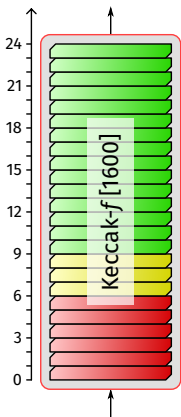
... is based on attacks on **reduced-round** versions!

Example: **AES-128** has 10 rounds

- best attacks break 6 rounds (1998) to 7 rounds (a few years later)
⇒ still 3 rounds of margin against progress in cryptanalysis
- 24 years of cryptanalysis since 1998
⇒ progress in cryptanalysis decreased over time

⇒ KECCAK is in a comparable situation.

Status of KECCAK cryptanalysis



- Preimage attacks up to 4 rounds
[He et al., ToSC 2021] [Wang et al., IACR ePrint 2022/977]
- Collision attacks up to 6 rounds
[Song et al., CRYPTO 2017] [Guo et al., ASIACRYPT 2022]
- Structural distinguishers
 - 7 rounds (practical time)
[Huang et al., EUROCRYPT 2017]
 - 8 rounds (2^{122} time)
[Huang et al., IEICE 2019]
 - 9 rounds (2^{64} time) – SymSum
[Suryawanshi et al., AFRICACRYPT 2020]
- Lots of third-party cryptanalysis available at:
https://keccak.team/third_party.html

What is SymSum?

A SymSum structural distinguisher produces:

- a set S of self-symmetric input strings, i.e.,
 $a||a||b||b||c||c|| \dots$, with $|a| = |b| = |c| = 32$ bits,
- such that

$$\bigoplus_{m \in S} H(m) \quad \text{is self-symmetric}$$

[Saha et al., ToSC 2017] [Suryawanshi et al., AFRICACRYPT 2020]

Preimage attacks

■ 2 rounds

Capacity	Output	Time	Reference
160	80	Practical	[Morawiecki, Crunchy contest, 2011]
512	256	2^{33}	[Naya-Plasencia et al., Indocrypt 2011]
768	384	2^{89}	[Kumar et al., Indocrypt 2018]
768	384	2^{28}	[Le et al., ePrint 2022/788]
1024	512	2^{252}	[Le et al., ePrint 2022/788]

■ 3 rounds

■ 4 rounds

Preimage attacks

- 2 rounds
- 3 rounds

Capacity	Output	Time	Reference
160	80	Practical	[Guo and Liu, Crunchy contest, 2016]
512	256	2^{150}	[Li et al., ToSC 2017]
512	256	2^{81}	[Li et al., Eurocrypt 2019]
512	256	2^{65}	[Lin et al., ToSC 2021]
576	512	2^{506}	[Morawiecki et al., FSE 2013]
1024	512	2^{440}	[Liu et al., ePrint 2020/346]
1024	512	2^{426}	[Le et al., ePrint 2022/788]

- 4 rounds

Preimage attacks

- 2 rounds
- 3 rounds
- 4 rounds

Capacity	Output	Time	Reference
160	80	Practical	[Liu and Guo, Crunchy contest, 2016]
256	128	2^{106}	[Guo et al., Asiacrypt 2016]
448	224	2^{218}	[Wang et al., ePrint 2022/977]
448	224	Q 2^{110}	[Wang et al., ePrint 2022/977]
512	256	2^{239}	[Li et al., Eurocrypt 2019]
512	256	2^{218}	[He et al., ToSC 2021]
512	256	Q 2^{128}	[Wang et al., ePrint 2022/013]
768	384	2^{371}	[Rajasree, Indocrypt 2019]
768	384	2^{366}	[Liu et al., ePrint 2020/346]
1024	512	Q 2^{255}	[Wang et al., ePrint 2022/013]

Collision attacks

■ 4 rounds

Capacity	Output	Time	Reference
160	160	Practical	[Dinur et al., Crunchy contest, 2011]
512	256	Practical	[Dinur et al., FSE 2012]
≤ 640	any	Practical	[Kölbl et al., IMA Int. Conf., 2013]
768	384	2^{147}	[Dinur et al., FSE 2013]
768	384	2^{59}	[Huang et al., ToSC 2022]

■ 5 rounds

■ 6 rounds

Collision attacks

- 4 rounds
- 5 rounds

Capacity	Output	Time	Reference
160	160	Practical	[Qiao et al., Crunchy contest, 2016]
256	256	Practical	[Qiao et al., Eurocrypt 2017]
448	224	2^{101}	[Qiao et al., Eurocrypt 2017]
448	224	Practical	[Song et al., Crypto 2017]
512	256	2^{115}	[Dinur et al., FSE 2013]
512	256	Practical	[Guo et al., JoC 2020]

- 6 rounds

Collision attacks

- 4 rounds
- 5 rounds
- 6 rounds

Capacity	Output	Time	Reference
160	160	2^{70}	[Qiao et al., Eurocrypt 2017]
160	160	2^{50}	[Song et al., Crypto 2017]
256	256	2^{123}	[Guo et al., Asiacrypt 2022]
256	256	$\mathbb{Q} 2^{67} / \sqrt{S}$	[Guo et al., Asiacrypt 2022]
448	224	$\mathbb{Q} 2^{97} / \sqrt{S}$	[Guo et al., Asiacrypt 2022]
512	256	$\mathbb{Q} 2^{104} / \sqrt{S}$	[Guo et al., Asiacrypt 2022]

TurboSHAKE

Goal

Define a XOF based on KECCAK- p [1600, $n_r = 12$]

Requirements:

- Suitable for PQC candidates
- Minimize the number of instances!
 - one for $c = 256$ + one for $c = 512$?
 - easier domain separation
- Multi-string input – $H(A; B; C)$ vs $H(A||B||C)$?
- Parallelism for long inputs?
- ... ?

Conclusions

- Extensive cryptanalysis on KECCAK
- \Rightarrow KECCAK with 12 rounds
 - has plenty of safety margin
 - yields a better performance/security trade-off
- TurboSHAKE to be defined

Thanks for your attention!

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