NIST Call for Multi-Party Threshold Schemes Brief Notes at ICMC 2023

Presented by Lily Chen^{*}at **ICMC 2023** International Cryptographic Module Conference September 22nd @ Ottawa, Canada

Expressed opinions are from the speakers/authors and should not be construed as official NIST views. Slides authored by Luís Brandão[†], based on "*NISTIR 8214C ipd*" (L. Brandão and R. Peralta. January 2023.) ^{*} Lily Chen is at NIST. [†] Luís Brandão is at NIST as a Foreign Guest Researcher (non-employee), contractor from Strativia.

Outline

- 1. NIST Crypto Standardization/Exploratory Projects
- 2. The "Threshold Call" (at a high level)
- 3. Subcategories and Submissions

(Slides will be publicly available)

Legend: Crypto = Cryptography. NIST = National Institute of Standards and Technology.

Outline

1. NIST Crypto Standardization/Exploratory Projects

2. The "Threshold Call" (at a high level)

3. Subcategories and Submissions

Legend: Crypto = Cryptography. NIST = National Institute of Standards and Technology.

- ▶ PQC: [standardization] "Post-Quantum" signatures and key-encapsulation
- **LWC:** [standardization] "LightWeight" auth. enc. w/ assoc. data, and hashing

- ▶ PQC: [standardization] "Post-Quantum" signatures and key-encapsulation
- LWC: [standardization] "LightWeight" auth. enc. w/ assoc. data, and hashing
- ► **PE<u>C</u>:** [exploratory] "**Privacy-Enhancing**" (advanced) features/functionalities
- ▶ MPTC: [exploratory] "Multi-Party Threshold" schemes for crypto primitives

- ▶ PQC: [standardization] "Post-Quantum" signatures and key-encapsulation
- **LWC:** [standardization] "LightWeight" auth. enc. w/ assoc. data, and hashing
- ▶ PEC: [exploratory] "Privacy-Enhancing" (advanced) features/functionalities
- MPTC: [exploratory] "Multi-Party Threshold" schemes for crypto primitives
- ... (various other projects in the NIST "Crypto group" [CTG])

- ▶ PQC: [standardization] "Post-Quantum" signatures and key-encapsulation
- LWC: [standardization] "LightWeight" auth. enc. w/ assoc. data, and hashing
- ▶ PEC: [exploratory] "Privacy-Enhancing" (advanced) features/functionalities
- MPTC: [exploratory] "Multi-Party Threshold" schemes for crypto primitives
- ... (various other projects in the NIST "Crypto group" [CTG])

The "Threshold Call" (from MPTC+PEC): to gather reference material for public analysis ... aiming for recommendations (in a 1st phase), including about PEC.

Cryptography (that can be) used to enhance privacy.

(emphasis on non-standardized tools)

Cryptography (that can be) used to enhance privacy.

(emphasis on non-standardized tools)

Goals:

1. Accompany the progress of emerging *PEC tools*.



Presented at ICMC 2023

Legend: ABE: attribute-based encryption. IBE: identity-based encryption. Inc.: including. PEC: privacy-enhancing cryptography. Symm./pub.: symmetric-key or public-key based.

Cryptography (that can be) used to **enhance privacy**. (emphasis on non-standardized tools)

Goals:

- 1. Accompany the progress of emerging *PEC tools*.
- 2. Promote development of PEC reference material.

PEC tools STPPA (series of talks) PEC use-case suite Threshold schemes ZKProof collaboration Encounter metrics Email list (PEC Forum)

https://csrc.hist.gov/projects/pec

Presented at ICMC 2023



Legend: ABE: attribute-based encryption. IBE: identity-based encryption. Inc.: including. PEC: privacy-enhancing cryptography. Symm./pub.: symmetric-key or public-key based.

Cryptography (that can be) used to **enhance privacy**. (emphasis on non-standardized tools)

Goals:

- 1. Accompany the progress of emerging PEC tools.
- 2. Promote development of PEC reference material.

PEC tools STPPA (series of talks) PEC use-case suite Threshold schemes ZKProof collaboration Encounter metrics Email list (PEC Forum)

Presented at ICMC 2023

3. Exploratory work to assess potential for recommendations, standardization; ...



Legend: ABE: attribute-based encryption. IBE: identity-based encryption. Inc.: including. PEC: privacy-enhancing cryptography. Symm./pub.: symmetric-key or public-key based.

Multi-Party Threshold Cryptography: NIST project

Cryptographic primitives:



Threshold schemes (for cryptographic primitives):



https://csrc.nist.gov/projects/threshold-cryptography

Multi-Party Threshold Cryptography: NIST project

Cryptographic primitives:



Threshold schemes (for cryptographic primitives):

- 1. Split (secret-share) the secret/private-key across multiple parties.
- 2. Use **MPC** to perform needed operation (with split key), e.g., sign. (MPC = secure multiparty computation ... or call it "Threshold Cryptography")



https://csrc.nist.gov/projects/threshold-cryptography

Multi-Party Threshold Cryptography: NIST project

Cryptographic primitives:

Threshold schemes (for cryptographic primitives):

- 1. Split (secret-share) the secret/private-key across multiple parties.
- 2. Use **MPC** to perform needed operation (with split key), e.g., sign. (MPC = secure multiparty computation ... or call it "Threshold Cryptography")
- "Threshold" (f): Operation is secure if number of corrupted parties is $\leq f$.
- Decentralized trust about key (not reconstructed): avoids single-point of failure. https://csrc.nist.gov/projects/threshold-cryptography
 Presented at ICMC 2023





Attraction: Potential applications and feasibility: threshold crypto; privacy apps; ...

Attraction: Potential applications and feasibility: threshold crypto; privacy apps; ...

Hesitations / need for recommendations:

- Which claimed crypto/security is useful and trustworthy?
- Which primitives are threshold-friendlier?

(easier in practice to thresholdize or, amenable to "better" threshold schemes)

Attraction: Potential applications and feasibility: threshold crypto; privacy apps; ...

Hesitations / need for recommendations:

- Which claimed crypto/security is useful and trustworthy?
- Which primitives are threshold-friendlier?

(easier in practice to thresholdize or, amenable to "better" threshold schemes)

Goal: Promote good adoptability (secure, interoperable, best practices; ...)

Attraction: Potential applications and feasibility: threshold crypto; privacy apps; ...

Hesitations / need for recommendations:

- Which claimed crypto/security is useful and trustworthy?
- Which primitives are threshold-friendlier?

(easier in practice to thresholdize or, amenable to "better" threshold schemes)

Goal: Promote good adoptability (secure, interoperable, best practices; ...)

How to explore the threshold space?



Attraction: Potential applications and feasibility: threshold crypto; privacy apps; ...

Hesitations / need for recommendations:

- Which claimed crypto/security is useful and trustworthy?
- Which primitives are threshold-friendlier?

(easier in practice to thresholdize or, amenable to "better" threshold schemes)

Goal: Promote good adoptability (secure, interoperable, best practices; ...)

How to explore the threshold space?

Next section: A public Call for reference material ... toward recommendations



Outline

1. NIST Crypto Standardization/Exploratory Projects

2. The "Threshold Call" (at a high level)

3. Subcategories and Submissions

Legend: Crypto = Cryptography. NIST = National Institute of Standards and Technology.

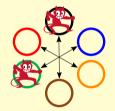
NIST Call for Multi-Party Threshold Schemes

- ▶ NISTIR 8214C: Initial public draft (Jan 2023) ⇒ Revised version (late 2023).
- ► Submission deadline (expected ≈ 2nd-half 2024)

NIST Call for Multi-Party Threshold Schemes

- ▶ NISTIR 8214C: Initial public draft (Jan 2023) ⇒ Revised version (late 2023).
- ► Submission deadline (expected ≈ 2nd-half 2024)

Calling for submissions of threshold schemes



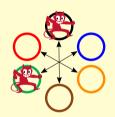
(And gadgets for modular use)

NIST Call for Multi-Party Threshold Schemes

- ▶ NISTIR 8214C: Initial public draft (Jan 2023) ⇒ Revised version (late 2023).
- ► Submission deadline (expected ≈ 2nd-half 2024)

Calling for submissions of threshold schemes for:

▶ [Cat1] Selected NIST-standardized primitives



Presented at ICMC 2023

► [Cat2] Other primitives (including FHE, IBE/ABE, ZKP)

(And gadgets for modular use)

FHE = Fully-homomorphic encryption. IBE/ABE = Identity/Attribute-based encryption ZKP = Zero-knowledge proof.

8/18

Notes about the process

- **Setup:** A gathering of reference material (not a competition for a selection).
- **Expected:** The process will clarify relevant system models, best practices, ...
- Aim: Devise recommendations about advanced cryptography (PEC + MPTC) (Will support future standardization processes.)
 PEC = Privacy-Enhancing Crypto MPTC = Multi-Party Threshold Crypto
- **Ample room for participation:** Give feedback \rightarrow Submit \rightarrow Analyze
- ▶ It's time: Consider starting to organize a future submission (team, scope, ...)

Notes about the process

- **Setup:** A gathering of reference material (not a competition for a selection).
- **Expected:** The process will clarify relevant system models, best practices, ...
- Aim: Devise recommendations about advanced cryptography (PEC + MPTC) (Will support future standardization processes.)
 PEC = Privacy-Enhancing Crypto MPTC = Multi-Party Threshold Crypto
- **Ample room for participation:** Give feedback \rightarrow Submit \rightarrow Analyze
- ▶ It's time: Consider starting to organize a future submission (team, scope, ...)

The call is not aimed at directly selecting a standard, but is part of a longer process toward possible standardization.

Community participation

Various areas / possible synergies:

- Scope of the call is of interest to various crypto communities: MPC, ZKP, FHE, ...
- ▶ Work developed with other SDOs and in community efforts is also welcome.

(SDO = Standards Development Organization)

Community participation

Various areas / possible synergies:

- Scope of the call is of interest to various crypto communities: MPC, ZKP, FHE, ...
- Work developed with other SDOs and in community efforts is also welcome. (SDO = Standards Development Organization)

Some variables:

- How will the community compose teams? (How to avoid effort duplication?)
- ▶ How will the scope of the call be covered? (primitives / models / approaches)

Community participation

Various areas / possible synergies:

- Scope of the call is of interest to various crypto communities: MPC, ZKP, FHE, ...
- Work developed with other SDOs and in community efforts is also welcome. (SDO = Standards Development Organization)

Some variables:

- How will the community compose teams? (How to avoid effort duplication?)
- ▶ How will the scope of the call be covered? (primitives / models / approaches)

ICMC 2023

MPTS 2023: (Sep 26–28) NIST Workshop on Multi-Party Threshold Schemes http://csrc.nist.gov/events/2023/mpts2023

Outline

1. NIST Crypto Standardization/Exploratory Projects

2. The "Threshold Call" (at a high level)

3. Subcategories and Submissions

Legend: Crypto = Cryptography. NIST = National Institute of Standards and Technology.

Subcategory: Type
C1.1: Signing
C1.2: PKE
C1.3: 2KA
C1.4: Symmetric
C1.5: Keygen

Too many acronyms, we know. (Legend further below)

Subcategory: Type	Families of specifications	NIST references
C1.1: Signing	EdDSA sign, ECDSA sign, RSADSA sign	FIPS 186-5 (see also NISTIR 8214B)

Legend: 2KA: pair-wise key-agreement. 2KE: pair-wise key-establisment. AES: Advanced Encryption Standard. CDH: cofactor Diffie-Hellman. ECC: Elliptic-curve cryptography (or, if used as an adjective, EC-based). ECDSA: Elliptic-curve Digital Signature Algorithm. EdDSA: Edwards-curve Digital Signature Algorithm. Elliptic-curve based Key-Establishment. FIPS: Federal Information Processing Standard. KC: Key-confirmtion. KDM: Key-derivation mechanism. Keygen: Key-generation. MQV: Menzes-Qu-Vanstone. PKE: public-key encryption. RSA: Rivest-Shamir-Adleman (signature and encryption schemes). RSADSA: RSA digital signature algorithm. SP 800: Special Publication (in Computer Security). Note: In the 2nd column, each item within a subcategory is itself called a family of specifications, since it may include diverse primitives or modes/variants.

Too many acronyms, we know. (Legend further below)

Subcategory: Type	Families of specifications	NIST references
C1.2: PKE	RSA decrypt, RSA encrypt (a secret value)	SP 800-56B Rev2

Legend: 2KA: pair-wise key-agreement. 2KE: pair-wise key-establisment. AES: Advanced Encryption Standard. CDH: cofactor Diflie-Hellman. ECC: Elliptic-curve cryptography (or, if used as an adjective, EC-based). ECDSA: Elliptic-curve Digital Signature Algorithm. EdDSA: Edwards-curve Digital Signature Algorithm. Elliptic-curve based Key-Establishment. FIPS: Federal Information Processing Standard. KC: Key-confirmtion. KDM: Key-derivation mechanism. Keygen: Key-generation. MQV: Menzes-Qu-Vanstone. PKE: public-key encryption. RSA: Rivest-Shamir–Adleman (signature and encryption schemes). RSADSA: RSA digital signature algorithm. SP 800: Special Publication (in Computer Security). Note: In the 2nd column, each item within a subcategory is itself called a family of specifications, since it may include diverse primitives or modes/variants.

Too many acronyms, we know. (Legend further below)

Subcategory: Type	Families of specifications	NIST references
-------------------	----------------------------	-----------------

C1.4: Symmetric AES encipher/decipher, KDM/KC (for 2KE) FIPS 197, SP 800-56C Rev2, ...

Legend: 2KA: pair-wise key-agreement. 2KE: pair-wise key-establisment, AES: Advanced Encryption Standard. CDH: cofactor Diffie-Hellman. ECC: Elliptic-curve cryptography (or, if used as an adjective, EC-based). ECDSA: Elliptic-curve Digital Signature Algorithm. EdDSA: Edwards-curve Edwards-Curv

Too many acronyms, we know. (Legend further below)

Subcategory: Type	Families of specifications	NIST references
C1.1: Signing	EdDSA sign, ECDSA sign, RSADSA sign	FIPS 186-5 (see also NISTIR 8214B)
C1.2: PKE	RSA decrypt, RSA encrypt (a secret value)	SP 800-56B Rev2
C1.3: 2KA	ECC-CDH, ECC-MQV	SP 800-56A Rev3
C1.4: Symmetric	AES encipher/decipher, KDM/KC (for 2KE)	FIPS 197, SP 800-56C Rev2,
C1.5: Keygen	ECC keygen, RSA keygen, bitstring keygen	(corresponding references above)

Legend: 2KA: pair-wise key-agreement. 2KE: pair-wise key-establisment. AES: Advanced Encryption Standard. CDH: cofactor Diffie-Hellman. ECC: Elliptic-curve cryptography (or, if used as an adjective, EC-based). ECDSA: Elliptic-curve Digital Signature Algorithm. EdDSA: Edwards-curve Digital Signature Algorithm. Elliptic-curve based Key-Establishment. FIPS: Federal Information Processing Standard. KC: Key-confirmtion, KDM: Key-derivation mechanism. Keygen: Key-generation. MQV: Menezes-Qu-Vanstone. PKE: public-key encryption. RSA: Rivest-Shamir-Adleman (signature and encryption schemes). RSADSA: RSA digital signature algorithm. SP 800: Special Publication (in Computer Security). Note: In the 2nd column, each item within a subcategory is itself called a family of specifications, since it may include diverse primitives or modes/variants. Presented at

ICMC 2023

Also to be added to Category Cat1

Primitives from NIST draft standards emerging from the PQC and LWC projects:

- ► ML-KEM (based on KYBER) Draft FIPS 203: Module-Lattice-Based KEM Standard
- ML-DSA (based on DILITHIUM) Draft FIPS 204: Module-Lattice-Based DSA
- SLH-DSA (based on SPHINCS) Draft FIPS 205: Stateless Hash-Based DSA
- FN-DSA (based on Falcon): Upcoming Draft FIPS
- AEAD and XOF standards (based on ASCON): Upcoming Special Publication(s)

Legend: AEAD = Authenticated Encryption with Associated Data. DSA = Digital Signature Algorithm. FIPS = Federal Information Processing Standard [Publication]. KEM = Key-Encapsulation Mechanism. ML = Module Lattice. SLH = StateLess hash. XOF = extendable Output Function.

Subcategory: Type

C2.1: Signing

C2.2: PKE

C2.3: Key-agreem.

C2.4: Symmetric

C2.5: Keygen

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

TF = threshold friendly. QR = quantum resistant.

Subcategory: Type	Example types of schemes	Example primitives
C2.1: Signing	TF succinct & verifiably-deterministic signatures TF-QR signatures	Sign Sign

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

Subcategory: Type

C2.6: Advanced C2.7: ZKPoK C2.8: Gadgets

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

TF = threshold friendly. QR = quantum resistant.

Subcategory: Type Example types of schemes Example primitives

C2.6: Advanced TF-QR fully-homomorphic encryption Decryption; Keygen TF identity-based and attribute-based encryption Decryption; Keygens

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

ernutation

14/18

Subcategory: Type Example types of schemes

Example primitives

C2.7: **ZKPoK** Zero-knowledge proof of knowledge of private key ZKPoK.Generate

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

Subcategory: Type	Example types of schemes	Example primitives
-------------------	--------------------------	--------------------

C2.8: **Gadgets** Garbled circuit (GC)

GC.generate; GC.evaluate

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

TF = threshold friendly. QR = quantum resistant.

Subcategory: Type	Example types of schemes	Example primitives
C2.1: Signing	TF succinct & verifiably-deterministic signatures	Sign
	TF-QR signatures	Sign
C2.2: PKE	TF-QR p ublic- k ey e ncryption (PKE)	Decrypt/Encrypt (a secret value)
C2.3: Key-agreem.	TF Low-round multi-party key-agreement	Single-party primitives
C2.4: Symmetric	TF blockcipher/PRP	Encipher/decipher
	TF key-derivation / key-confirmation	PRF and hash function
C2.5: Keygen	Any of the above	Keygen
C2.6: Advanced	TF-QR fully-homomorphic encryption	Decryption; Keygen
	TF identity-based and attribute-based encryption	Decryption; Keygens
C2.7: ZKPoK	Zero-knowledge proof of knowledge of private key	ZKPoK.Generate
C2.8: Gadgets	Garbled circuit (GC)	GC.generate; GC.evaluate

Note: While TF-QR is desired for any type of scheme, some examples show just TF to highlight that it is welcome even if not QR.

Legend: agreem. = agreement. Keygen = key-generation. PKE = public-key encryption. PRF = pseudorandom function [family]. PRP = pseudorandom permutation [family]. QR = quantum resistant. TF = threshold-friendly. ZKPoK = zero knowledge proof of knowledge.

Main components of a submission package

Check	#	ltem
	M1	Written specification (S1–S16)
	M2	Reference implementation (Src1–Src4)
	M3	Execution instructions (X1–X7)
	M4	Experimental evaluation (Perf1–Perf5)
	M5	Additional statements

Main components of a submission package

Check	#	ltem
	M1	Written specification (S1–S16)
	M2	Reference implementation (Src1–Src4)
	М3	Execution instructions (X1–X7)
	M4	Experimental evaluation (Perf1–Perf5)
	M5	Additional statements

The revised version of the call will detail better each **component**.

A submission package can propose various objects (schemes/gadgets).

Each **component** will then map all such **objects**.

Some technical notes

- 1. Submission focuses
- 2. Threshold profile
- 3. Active security
- 4. Adaptive security
- 5. Modularity
- 6. Post-vs-Pre quantum crypto

Some technical notes

- 1. Submission focuses: can specify a family of schemes (in various subcategories).
- 2. Threshold profile: open to choice (number of parties; dishonest proportion; ...)
- 3. Active security: is required, though open to diverse security formulations.
- 4. Adaptive security: at least "argued for" for major safety properties.
- 5. Modularity: modularize gadgets; encouraged proactive resharing module; ...
- 6. Post-vs-Pre quantum crypto: both in scope; pre-quantum needs justification.

Concluding remarks

Selected takeaways

- ► The "Threshold Call" has a **wide scope** of subcategories for submission
- Enables an **exploration** of advanced cryptography, before promising standards
- ► The initial process will devise **recommendations** for subsequent processes
- Community participation is essential (feedback; submissions; analyses)

Thank you for your attention! Questions?

NIST Call for Multi-Party Threshold Schemes Brief Notes at ICMC 2023

Presented at ICMC 2023 | September 22nd @ Ottawa, Canada

We appreociate followup comments: luis.brandao@nist.gov



Threshold Call (Draft)



MPTS 2023 (Sept. 26–28)



MPTC-Forum (email list)



PEC-Forum (email list)