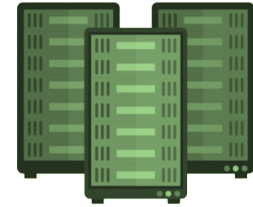


# Challenges and new Features for Anonymous Credentials: Revocation and Decentralization

Foteini Baldimtsi



# Anonymous Authentication



## Credential



**Name:**  
Alice Liddell

**Date of Birth:**  
11/26/1865

**Address:**  
Rabbit Hole

**Country:**  
Wonderland

**ID Number:**  
12345678

## Proof



**Predicate:**  
Age > 21



## Proof'



**Predicate:**  
Age > 21

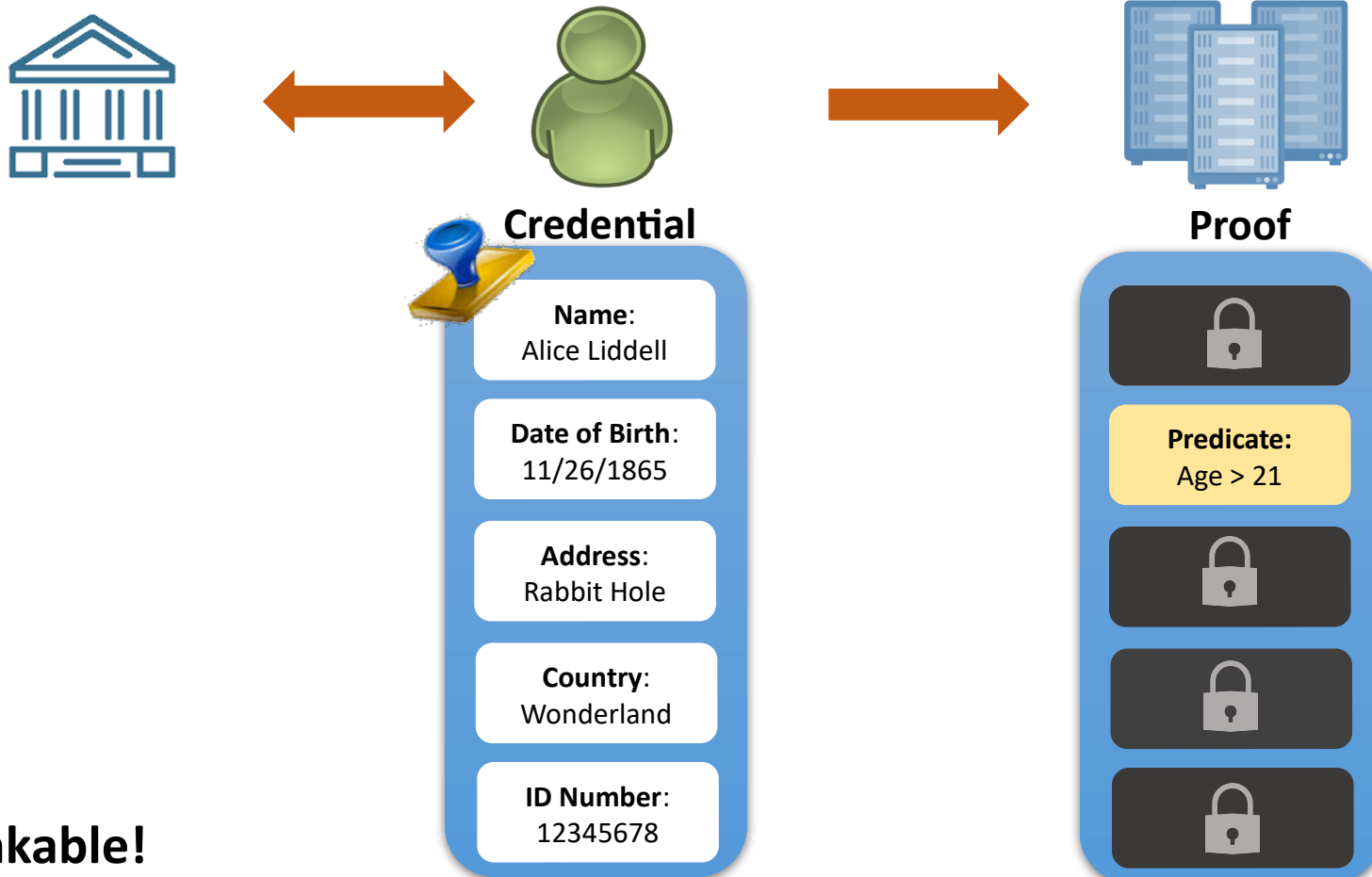


**Unlinkable!**



**Unlinkable!**

# Anonymous Authentication



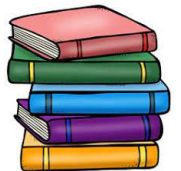
**Unlinkable!**

## Generic construction

- Issuance:  
digital signatures
- Credential showing:  
ZK proofs

Efficiency?\*

"Anonymous  
Credentials"



\* zk-creds: a recent work suggesting anonymous credentials from SNARKs [RWGM'22]

# Anonymous Credentials

**Multi Use**  
Anonymous Credentials  
based on signatures  
and ZK proofs

**Single Use**  
Anonymous Credentials  
based on blind signatures  
(+ optional ZK proofs)



Chaum'81, Chaum'82, Brands'93, CFY'98, CL'01, CL'02, CL'04, CHL'05, CG'08, BCKL'09, FDV'09, IB'12, CNR'12, ...  
BL'13b, RHBP'13, BCHKLN'13, RBHP'15, BCDLRSY'17 ...]



# Anonymous Credentials

**Multi Use**  
Anonymous Credentials  
based on signatures  
and ZK proofs

- Subscription Services
- Digital IDs



**Single Use**  
Anonymous Credentials  
based on blind signatures  
(+ optional ZK proofs)

- Single-use coupons
- E-cash
- E-voting
- ✓ More efficient\*

\*If only to be used a small number of times  
single use credentials are preferable

# Multi-use Anonymous Credentials

Introduced by [CL01,CL04,...]

**Core Primitive:** CL signatures (Signatures on committed values that allow for efficient proofs of signature ownership)

CL signatures are based on RSA

[BBS'04, ASM'06]: BBS+ signatures based on bilinear pairings

Standardization?



# Anonymous Credentials

**Multi Use**  
Anonymous Credentials  
based on signatures  
and ZK proofs

- Subscription Services
- Digital IDs



**Single Use**  
Anonymous Credentials  
based on blind signatures  
(+ optional ZK proofs)

- Single-use coupons
- E-cash
- E-voting
- ✓ More efficient\*

\*If only to be used a small number of times single use credentials are preferable

# Single-Use Credential + Attributes



[BL'13b] "Anonymous Credentials Light"

**Efficiency:** EC based, 3-rounds

Issuance: 13 exponentiations for User + 7 exponentiations of Signer

Verification: 8 exponentiations

**Security:** Unlikability/Blindness under DDH in RO

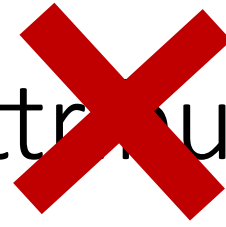
Unforgeability under DL in RO in the sequential setting

[BLLOR'21]: most efficient DL blind signatures (including [BL'13b]) are not secure under parallel issuance

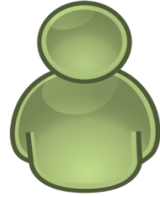




# Single-Use Credential + Attributes



← blind  
signature →

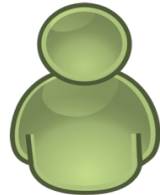


A valid blind signature is a credential/token!

**Avoid double-use?**

# Single-Use Credential + Attributes

## Registration Phase



$C, ZK \pi$



Alice

$C$  = commit (user attributes)

Open account for (Alice,  $C$ )

If you double show your credential,  
(parts of)  $C$  will be disclosed!

**Challenge:** embed  $C$  in the credential  
while maintain unlinkability

## Issuance Phase



Alice

Blind Sign



Alice,  $C$

Accounts: (Alice,  $C$ )

no concurrently secure  
efficient schemes



A valid blind signature is a credential/token!

# (Anonymous) Digital Credentials in the Age of Decentralization

# Decentralized Credentials

**Decentralizing Issuance  
Of  
Anonymous Credentials**

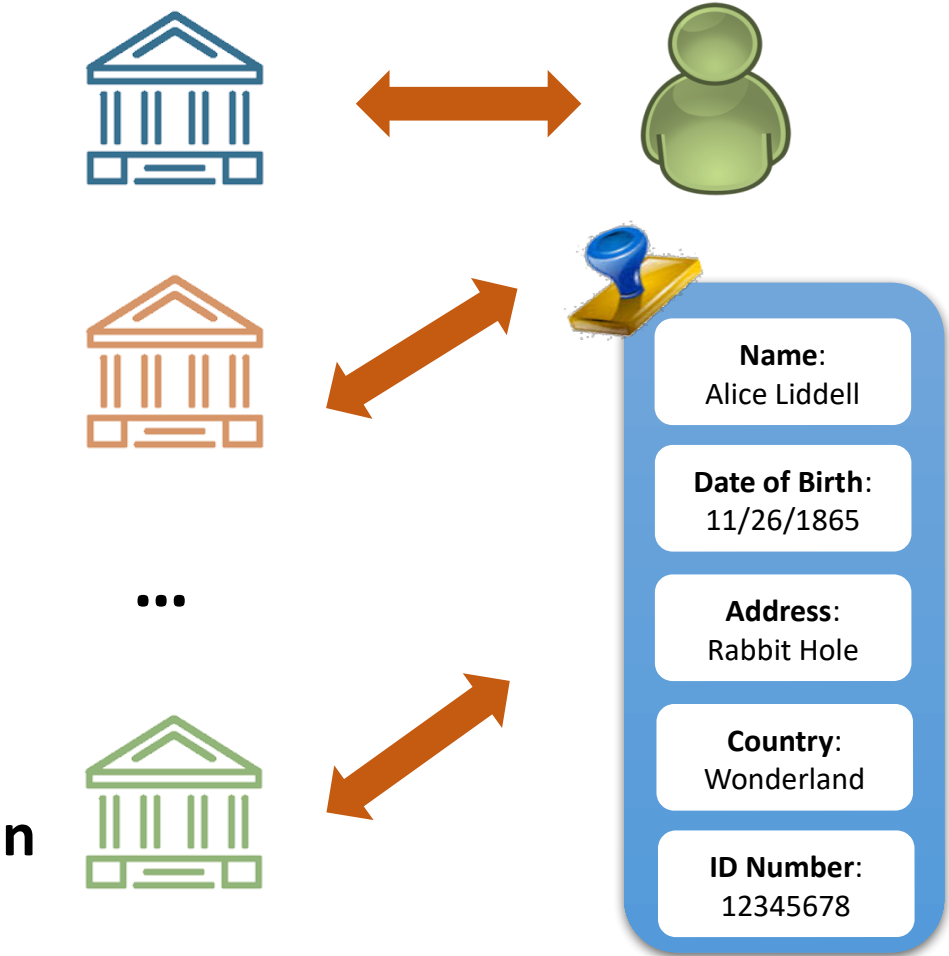
[Coconut'17]



**DID: Decentralized  
Identities  
(anonymity)**

[GGM'13, CanID'21]

# Decentralizing Issuance- Threshold Blind Signs



Use threshold (blind) signatures for the credential issuance [Coconut'17, NYM]

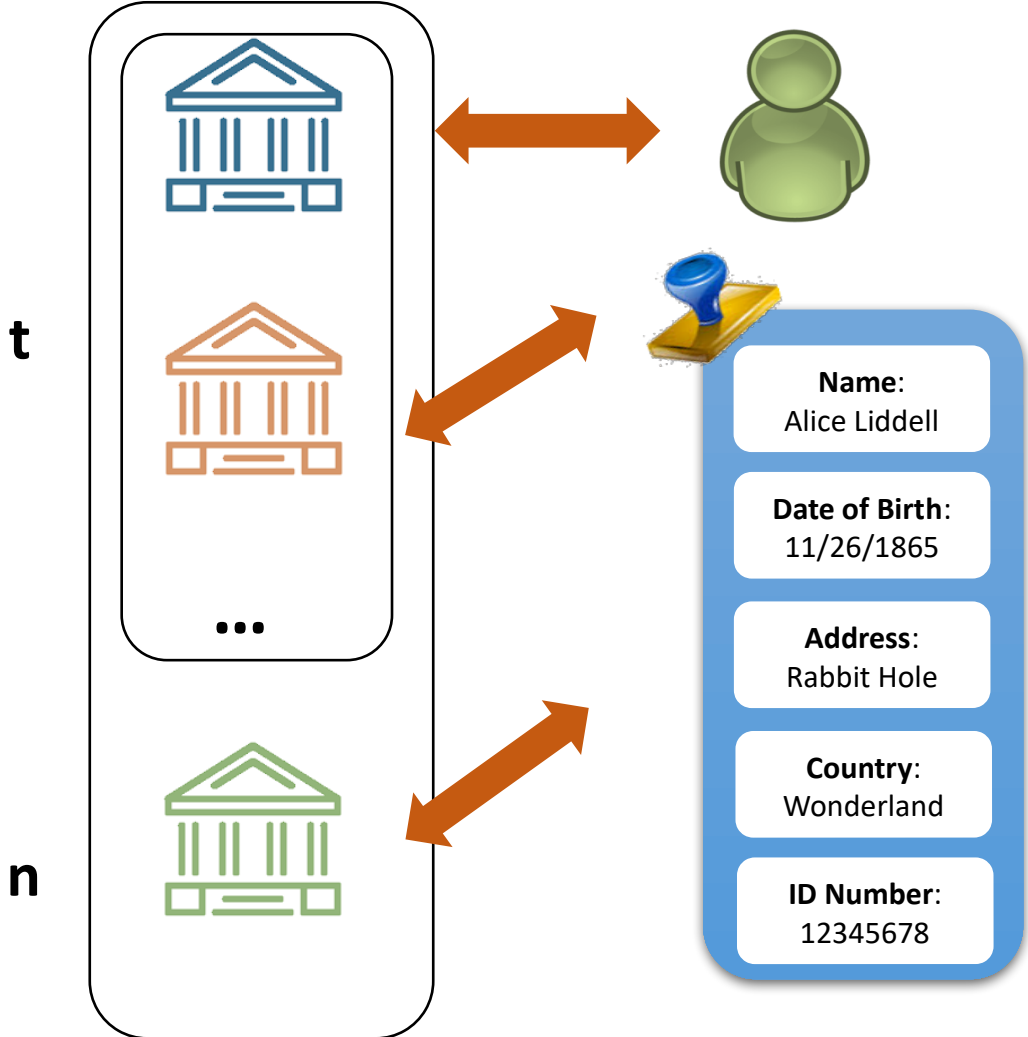


Smart contract

- Blindness** (Icon: eye with slash)
- Unlinkability** (Icon: chain with slash)
- Threshold Authority** (Icon: three people at a table with a star)
- Authorities Non-Interactivity** (Icon: network with slash)
- Efficiency** (Icon: speedometer)

Image: from [Coconut] authors slides

# Decentralizing Issuance- Threshold Blind Signs



Use threshold (blind) signatures for the credential issuance [Coconut, NYM]

- User Requests for a credential
- Authorities Issue (at least  $t$  honest authorities)
- User collects, aggregates and randomizes
- User presents credential

Building blocks: PS'16 randomizable signatures, El Gamal Encryption, DL based ZK proofs

**Multi Use**  
Anonymous Credentials  
based on signatures  
and ZK proofs

# Decentralizing Issuance- Threshold Blind Signs

Use threshold (blind) signatures for the credential issuance [Coconut, NYM]

- Signer privacy, blindness/unlinkability

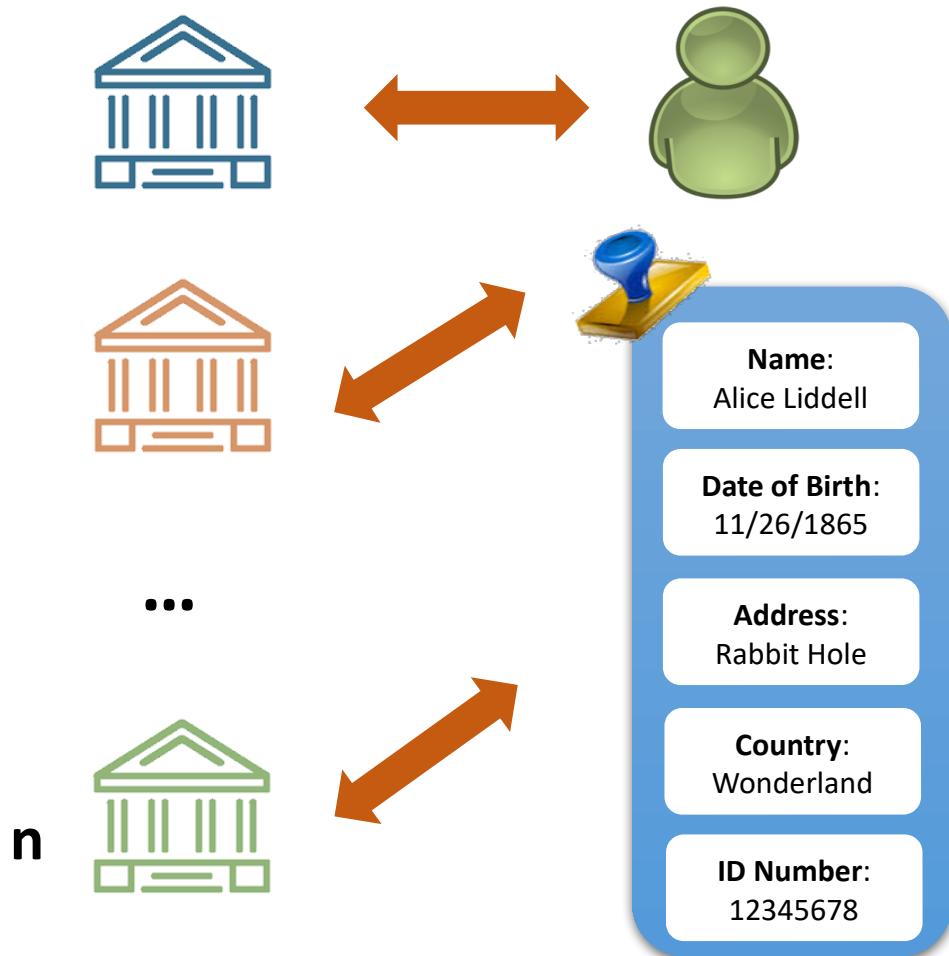


- Interactive, non-flexible threshold key generation phase

- Smart contract relatively expensive (on-chain verification 4.2M ETH gas - \$90 USD Aug'22)
- No support for revocation + auditability



[Zebra'22]: reduces gas costs x10 (uses SNARKs), adds revocation + auditability features



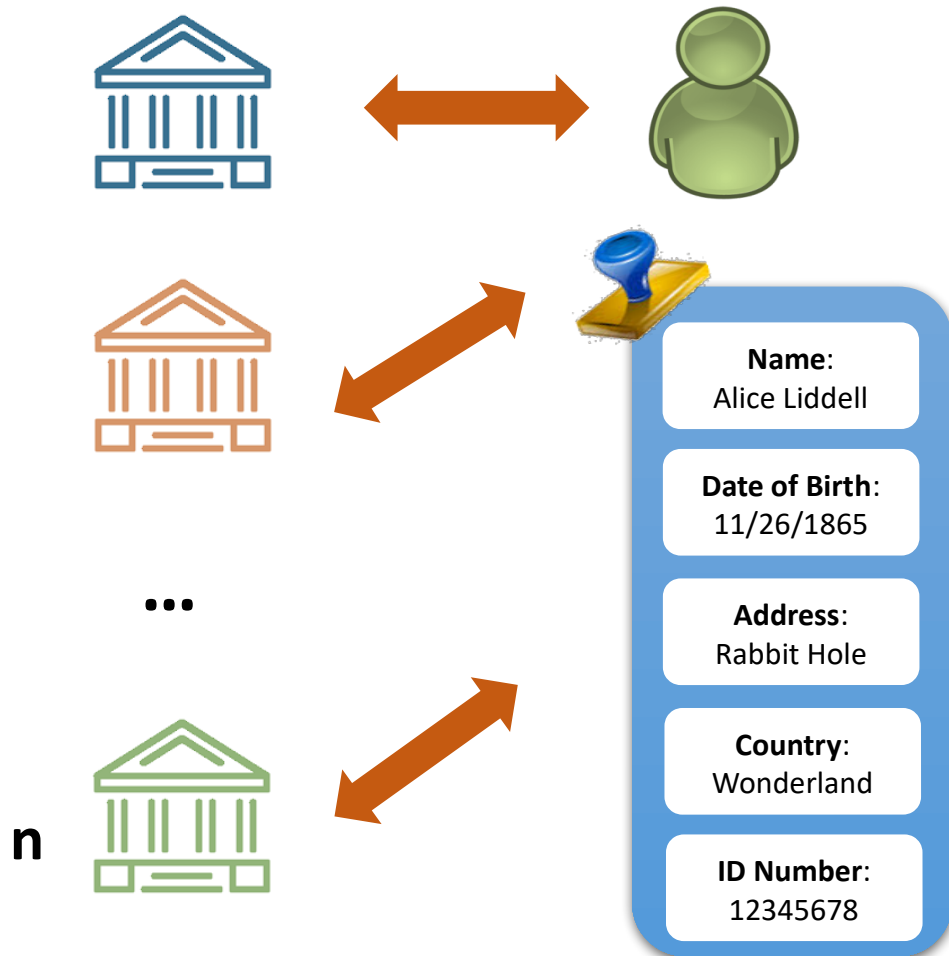
# Decentralizing Issuance – Multi-Blind Signs [BKKL'23]

Use multi (blind) signatures [new approach]

- Signer accountability
- More flexible signing process
- Controlled set anonymity

Constructions for both multi-use and single-user credentials (so much cheaper to verify! no zk proofs!)

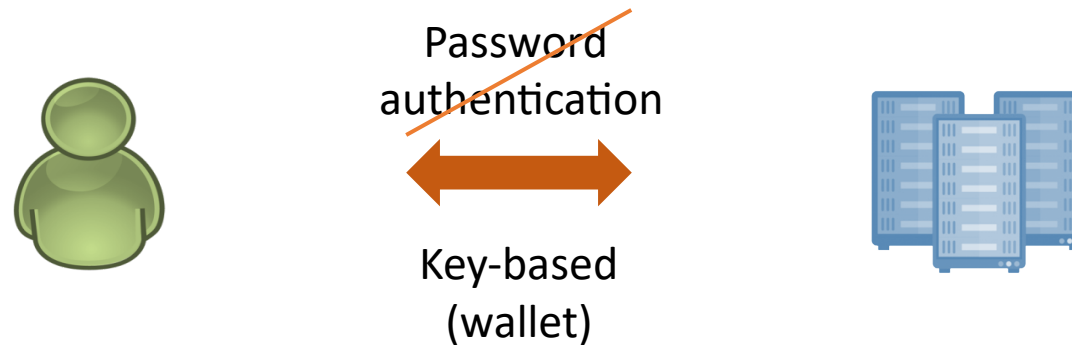
Based on BLS signatures





# Decentralized Identities – Self created

[GGM]: decentralized non general credentials, “self assertion of credential”



- Addresses bootstrapping (using oracles like DECO)
- Accountability (sanction lists)
- Weak privacy (if collusions happen)
- Not efficient revocation (not privately)



# Anonymous Credentials

## Multi Use

### Anonymous Credentials

based on signatures  
and ZK proofs

## Single Use

### Anonymous Credentials

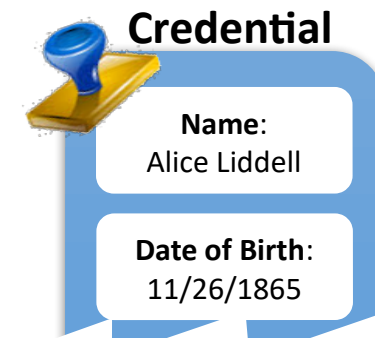
based on blind signatures  
(+ optional ZK proofs)

What about revocation? ?

# Credential Revocation

Revocation of credentials is a hard problem.

- In TLS millions of certificates are revoked per year
- Simultaneous/fast (i.e. due to critical security issues like Heartbleed) revocation is very hard
- More challenges in restricted settings, i.e. web browsers, IoT devices etc



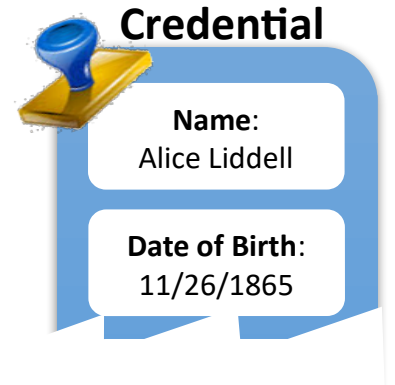
Revocation of *anonymous* credentials is an even harder problem.

# Credential Revocation



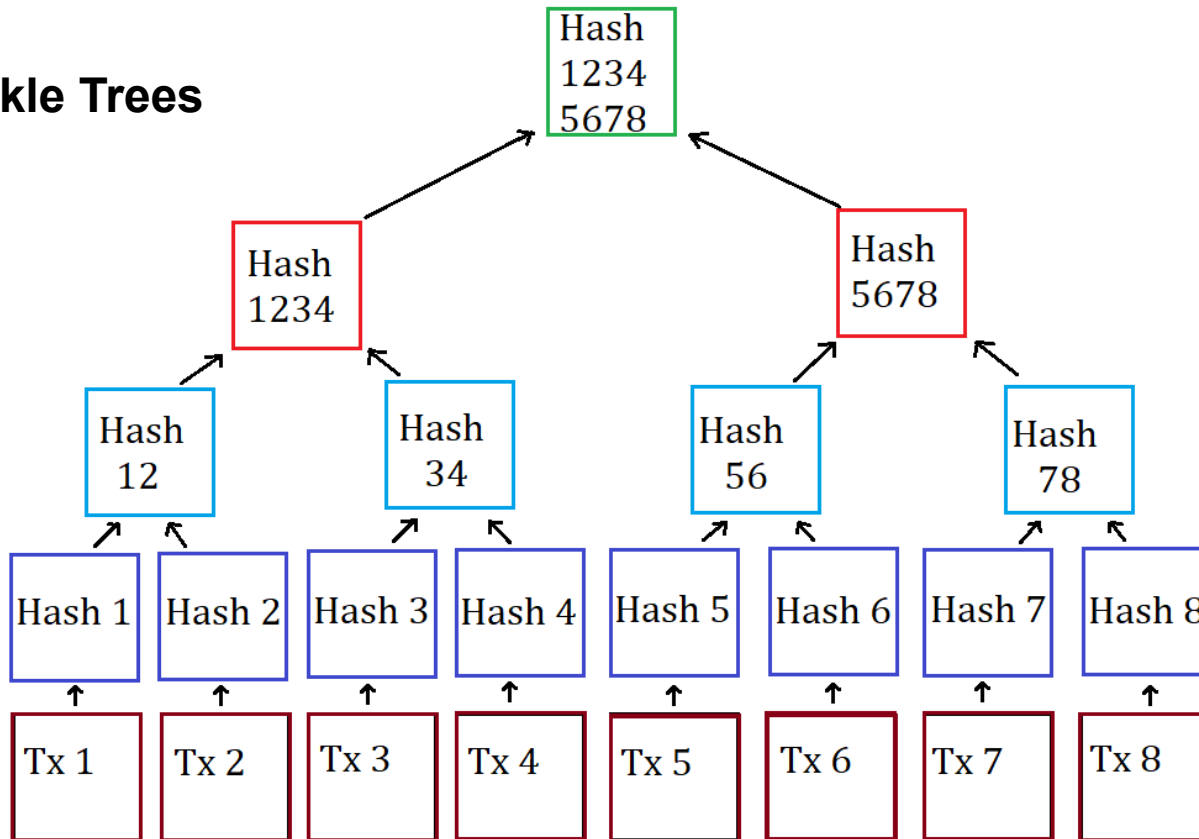
Accept List
Alice
Bob
...
...
Dave

- ✓ additions/deletions  
(under central management)
- ✗ Size of Accept List  $O(n)$
- ✗ User privacy



# Credential Revocation

## Merkle Trees



Digest:  $O(1)$

Proof-of-membership:  $O(\log n)$

## Cryptographic Accumulators

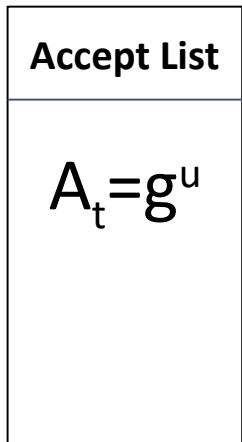
Digest:  $O(1)$

Proof-of-membership:  $O(1)$

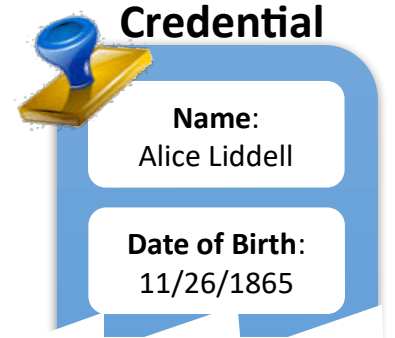
**++ more properties**

(efficient non-membership proofs/updates/deletions)

# Credential Revocation- Accumulators



- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✗ User privacy



## RSA Accumulator

### Setup:

- Choose  $N=pq$  where  $p, q$  are secret primes
- *(initial state)*

### Add()

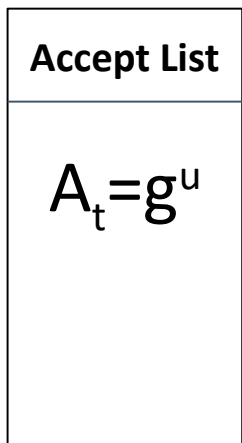
- 

### Del()

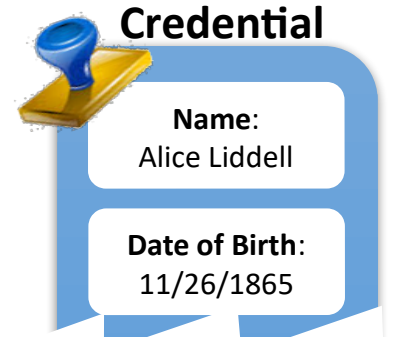
State after set S added:

$$u =$$

# Credential Revocation- Accumulators



- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✗ User privacy



## RSA Accumulator – How to prove membership

### Add x

- $A_{t+1} = A_t^x$
- Witness  $w = A_t$

### Prove membership

- “x is in  $A_{t+1}$ , here is a witness w”
- Verify check:  $A_{t+1} = w^x$

**But what if more updates happen in between Add - Prove?**

- ✗ Users need to update their witness for every single addition/deletion!

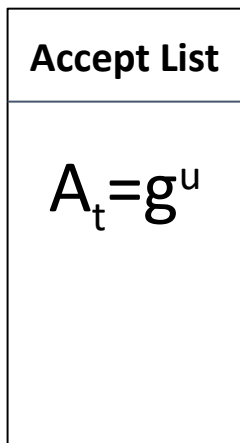
**But do they really?**

State after set S added:

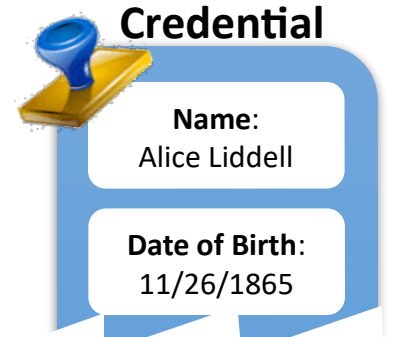
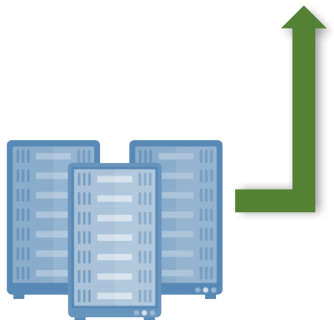
$u =$

# Credential Revocation- Modular Accumulators

[BCDLRSY'17, BK'21]



- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✗ User privacy



## Modular Accumulators

### Basic Idea

- Start with a full accumulator  $A_0$  (includes all domain  $S$ )
- Manager (holding trapdoor) can issue membership witnesses
- No need to update witnesses after additions –  $A$  does not change
- Only changes after deletions!

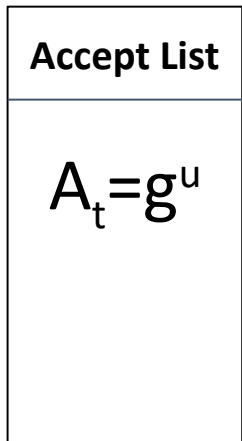
**$O(d)$  updates**

- ✗ **Reduced security (non-adaptive adversaries)**

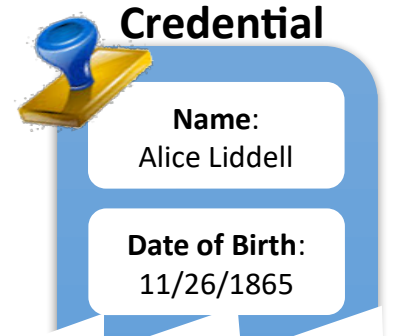
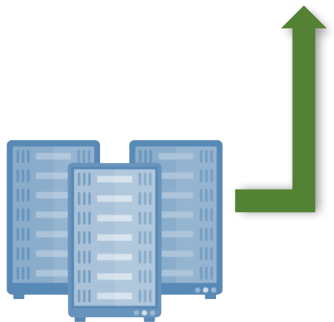
➔ Accumulator  $A$  for additions and  $A'$  for Deletions. Users need to show membership in 1<sup>st</sup> and non-membership in 2<sup>nd</sup>



# Credential Revocation- Modular Accumulators



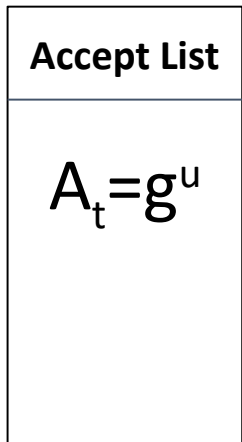
- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✗ User privacy



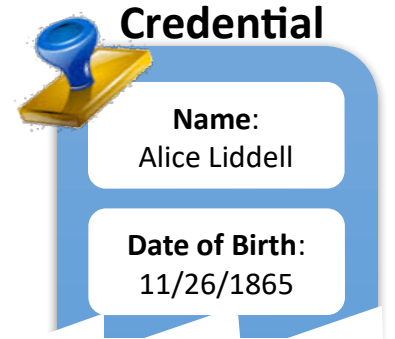
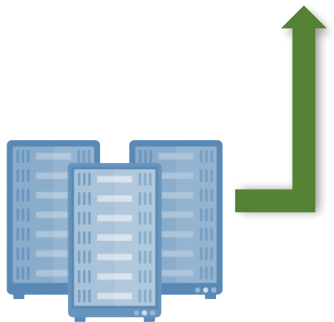
	Add	Del	Updates	soundness
RSA	✓	✓	$O(a + d)$	adaptive
Basic Idea	✓	✓	$O(d)$	non-adaptive
Modular	✓	✓	$O(d)$	adaptive

Join-Revoke unlinkability!

# Credential Revocation- Modular Accumulators



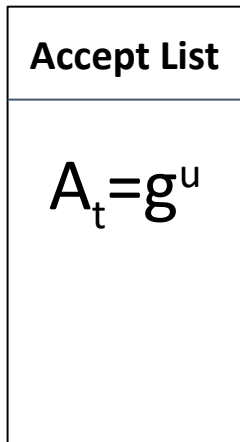
- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✗ User privacy



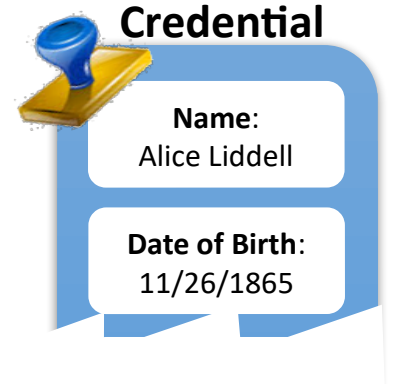
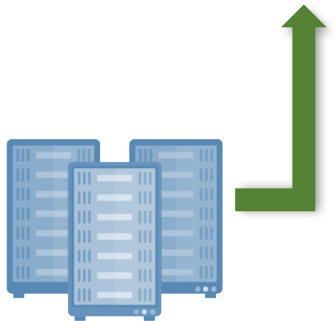
	Add	Del	Updates	soundness	Join-Revoke Unlinkability
RSA	✓	✓	$O(a + d)$	adaptive	✗
Basic Idea	✓	✓	$O(d)$	non- adaptive	✗
Modular	✓	✓	$O(d)$	adaptive	✓

Join-Revoke unlinkability!

# Credential Revocation- Modular Accumulators



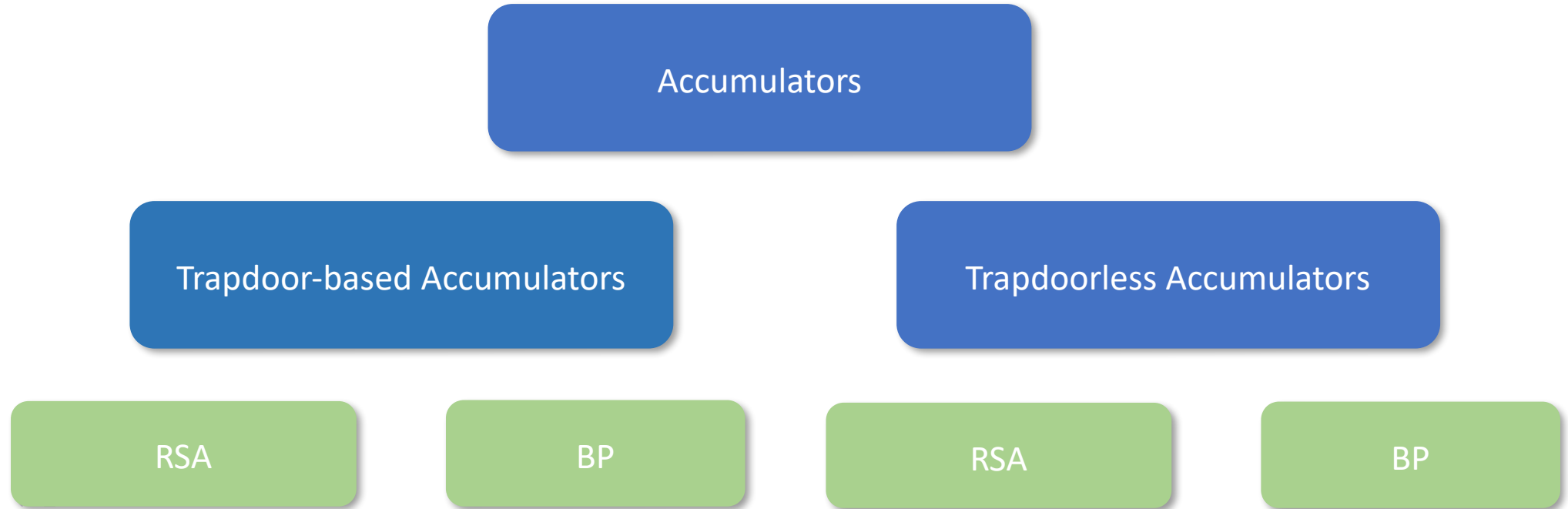
- ✓ additions/deletions  
(under central management)
- ✓ Constant size
- ✓ User privacy



## Prove membership

- “x is in  $A_{t+1}$ , here is a witness w”
- Verify check:  $A_{t+1} = w^x$
- To hide x you need to use ZK proofs which compose efficiently with the accumulator.

# Cryptographic Accumulators



Multiple extensions and challenges: batching + aggregation, need for setup, efficiency in trapdoorless scenario....

# Final Thoughts

## Technology via generic solutions exists

- Efficiency challenges (time-sensitive applications, lightweight devices, gas/storage costs if on blockchain,...)
- Bootstrapping problem
- Accountability without trusted third parties – auto-executed policies
- Back-up, identity restore
- Revocation of identities/credentials
- Efficient Post-quantum secure solutions are basically non-existent